

# Comparison tables: BBOB 2012 noisy testbed in 20-D

The BBOBies

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## Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2010, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2012>. 4 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [4, 2]. The experimental set-up is described in [3].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [1]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [3] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values. Table 1 gives an overview on all algorithms submitted to the noise-free testbed in 2012.

Table 1: Names and references of all algorithms submitted for the noise-free testbed

algorithm name	short	paper	reference
IPOPsaACM		Black-box Optimization Benchmarking of IPOP-saACM-ES on the BBOB-2012 Noisy Testbed (Page 261)	[8]
SNES		Benchmarking Separable Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 205)	[7]
xNES		Benchmarking Exponential Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 213)	[5]
xNESas		Benchmarking Natural Evolution Strategies with Adaptation Sampling on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 229)	[6]
SNES, xNES, xNESas		Comparing Natural Evolution Strategies to BIPOP-CMA-ES on Noiseless and Noisy Black-Box Optimization Testbeds (Page 237)	[9]

Table 2: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f101</b>	59	425	571	700	739	783	15/15
IPOPsaACM	4.7(1)	<b>0.86</b> <sub>(0.2)</sub> <sup>*4</sup>	<b>0.73</b> <sub>(0.1)</sub> <sup>*4</sup> <sub>↓2</sub>	<b>0.78</b> <sub>(0.1)</sub> <sup>*4</sup> <sub>↓3</sub>	<b>0.88</b> <sub>(0.1)</sub> <sup>*4</sup> <sub>↓</sub>	<b>0.99</b> <sub>(0.1)</sub> <sup>*4</sup>	15/15
SNES	<b>4.1</b> <sub>(0.7)</sub>	1.5(0.2)	1.9(0.1)	2.8(0.2)	3.9(0.1)	4.7(0.2)	15/15
xNES	5.5(2)	7.1(0.9)	10(0.7)	17(0.6)	24(0.4)	30(0.6)	15/15
xNESas	4.8(2)	5.1(0.8)	5.7(2)	6.7(2)	7.7(3)	8.4(2)	30/30

Table 3: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f102</b>	231	399	579	921	1157	1407	15/15
IPOPsaACM	1.2(0.2)	<b>0.93</b> (0.2) <sup>*3</sup>	<b>0.75</b> (0.1) <sub>↓3</sub> <sup>*4</sup>	<b>0.61</b> (0.1) <sub>↓4</sub> <sup>*4</sup>	<b>0.60</b> (0.0) <sub>↓4</sub> <sup>*4</sup>	<b>0.60</b> (0.0) <sub>↓4</sub> <sup>*4</sup>	15/15
SNES	<b>1.1</b> (0.2)	1.6(0.3)	1.9(0.1)	2.1(0.1)	2.5(0.1)	2.7(0.1)	15/15
xNES	1.5(0.7)	7.7(0.9)	10(0.5)	13(0.3)	15(0.2)	17(0.4)	15/15
xNESas	1.5(0.5)	5.8(2)	6.2(2)	5.6(2)	5.4(2)	5.4(2)	30/30

Table 4: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f103</b>	65	417	629	1313	1893	2464	14/15
IPOPsaACM	3.9(0.8)	<b>0.83</b> (0.2) $\downarrow_2^{*4}$	<b>0.66</b> (0.1) $^{*4}$	<b>0.52</b> (0.1) $\downarrow_4^{*4}$	<b>0.55</b> (0.1) $\downarrow_4^{*4}$	<b>0.58</b> (0.1) $\downarrow_3^{*4}$	15/15
SNES	<b>3.8</b> (0.9)	1.5(0.2)	1.7(0.1)	1.6(0.1)	1.7(0.1)	3.4(2)	15/15
xNES	6.2(2)	7.4(0.8)	10(0.4)	9.4(0.3)	10(0.4)	11(0.3)	15/15
xNESas	5.0(2)	5.0(1)	4.9(2)	4.1(2)	5.5(2)	6.8(2)	30/30

Table 5: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{104}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f104</b>	23690	85656	1.7e5	1.8e5	1.9e5	2.0e5	15/15
IPOPsaACM	<b>3.5</b> (2)	<b>1.1</b> (0.6) <sup>*4</sup>	<b>0.55</b> (0.3) <sup>*4</sup>	<b>0.52</b> (0.3) <sup>*4</sup>	<b>0.50</b> (0.3) <sup>*4</sup>	<b>0.49</b> (0.3) <sup>*4</sup>	15/15
SNES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	8.1(10)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>8e6</i>	0/15
xNESas	24(29)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e7</i>	0/30

Table 6: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{105}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f105</b>	1.9e5	6.1e5	6.3e5	6.5e5	6.6e5	6.7e5	15/15
IPOPsaACM	<b>1.0</b> <sup>(0.4)*2</sup>	<b>0.36</b> <sup>(0.1)↓3</sup>	<b>0.35</b> <sup>(0.1)↓3</sup>	<b>0.34</b> <sup>(0.1)↓3</sup>	<b>0.34</b> <sup>(0.1)↓3</sup>	<b>0.33</b> <sup>(0.1)↓3</sup>	15/15
SNES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	17(16)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>7e6</i>	0/15
xNESas	24(33)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e7</i>	0/21

Table 7: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{106}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f106</b>	11480	21668	23746	25470	26492	27360	15/15
IPOPsaACM	<b>0.28</b> <sub>(0.1)</sub> <sup>*4</sup> <sub>↓4</sub>	<b>0.37</b> <sub>(0.3)</sub> <sup>*4</sup> <sub>↓4</sub>	<b>0.39</b> <sub>(0.2)</sub> <sup>*4</sup> <sub>↓4</sub>	<b>0.45</b> <sub>(0.2)</sub> <sup>*4</sup> <sub>↓4</sub>	<b>0.46</b> <sub>(0.2)</sub> <sup>*4</sup> <sub>↓4</sub>	<b>0.47</b> <sub>(0.2)</sub> <sup>*4</sup> <sub>↓4</sub>	15/15
SNES	123 <sub>(138)</sub>	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	1.3 <sub>(0.1)</sub>	1.2 <sub>(0.1)</sub>	1.3 <sub>(0.1)</sub>	1.3 <sub>(0.1)</sub>	1.5 <sub>(0.1)</sub>	1.7 <sub>(0.1)</sub>	15/15
xNESas	1.2 <sub>(0.2)</sub>	1.4 <sub>(0.3)</sub>	1.5 <sub>(0.5)</sub>	1.7 <sub>(0.9)</sub>	1.8 <sub>(0.7)</sub>	2.0 <sub>(0.7)</sub>	30/30

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Table 8: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{107}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f107</b>	8571	13582	16226	27357	52486	65052	15/15
IPOPsaACM	<b>0.83</b> (0.5)	<b>1.3</b> (0.8) <sup>*3</sup>	<b>1.4</b> (0.7) <sup>*4</sup>	<b>1.3</b> (0.8) <sup>*4</sup>	<b>1.0</b> (0.5) <sup>*4</sup>	<b>0.94</b> (0.4) <sup>*4</sup>	15/15
SNES	2.6(3)	14(15)	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	1.7(0.4)	69(69)	879(893)	$\infty$	$\infty$	$\infty$ <i>7e6</i>	0/15
xNESas	1.6(0.9)	44(41)	786(1027)	$\infty$	$\infty$	$\infty$ <i>1e7</i>	0/15

Table 9: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f108</b>	58063	97228	2.0e5	4.5e5	6.3e5	9.0e5	15/15
IPOPsaACM	<b>0.72</b> <sub>(0.3)</sub> <sup>*4</sup>	<b>1.2</b> <sub>(0.6)</sub> <sup>*4</sup>	<b>1.1</b> <sub>(0.6)</sub>	<b>1.2</b> <sub>(0.7)</sub>	<b>1.6</b> <sub>(0.3)</sub>	<b>1.4</b> <sub>(0.3)</sub>	15/15
SNES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>6e6</i>	0/15
xNESas	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e7</i>	0/15

Table 10: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f109</b>	333	632	1138	2287	3583	4952	15/15
IPOPsaACM	0.93(0.3)	<b>0.78</b> <sub>(0.2)↓<sup>2</sup></sub>	<b>0.78</b> <sub>(0.2)↓<sup>2</sup></sub> <sup>*3</sup>	<b>0.89</b> <sub>(0.3)↓<sup>4</sup></sub> <sup>*4</sup>	<b>0.79</b> <sub>(0.2)↓<sup>4</sup></sub>	<b>0.75</b> <sub>(0.2)↓<sup>2</sup></sub> <sup>*4</sup>	15/15
SNES	<b>0.77</b> <sub>(0.1)↓<sup>2</sup></sub>	1.1(0.1)	1.3(0.2)	3.8(3)	15(13)	103(111)	3/15
xNES	0.94(0.3)	5.5(0.7)	7.7(0.4)	10(0.5)	10(0.5)	10(0.3)	15/15
xNESas	1.0(0.2)	4.7(0.6)	6.9(0.8)	9.4(0.7)	10(0.5)	13(8)	15/15





Table 13: 20-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{112}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f112</b>	25552	64124	69621	73557	76137	78238	15/15
IPOPsaACM	<b>0.89</b> <sub>(0.3)</sub>	<b>0.79</b> <sub>(0.1)</sub> <sup>*4</sup>	<b>0.84</b> <sub>(0.1)</sub> <sup>*4</sup>	<b>0.88</b> <sub>(0.1)</sub> <sup>*4</sup>	<b>0.88</b> <sub>(0.1)</sub> <sup>*4</sup>	<b>0.88</b> <sub>(0.1)</sub> <sup>*4</sup>	15/15
SNES	113 <sub>(122)</sub>	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	0.93 <sub>(0.2)</sub>	52 <sub>(64)</sub>	1454 <sub>(1519)</sub>	$\infty$	$\infty$	$\infty$ <i>7e6</i>	0/15
xNESas	0.99 <sub>(0.2)</sub>	59 <sub>(67)</sub>	952 <sub>(948)</sub>	3878 <sub>(4383)</sub>	3747 <sub>(3875)</sub>	3646 <sub>(3690)</sub>	1/15

Table 14: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{113}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f113</b>	50123	3.6e5	5.6e5	5.9e5	5.9e5	5.9e5	15/15
IPOPsaACM	<b>0.54</b> (0.2)	<b>0.35</b> (0.2) $\downarrow_2^{*4}$	<b>0.31</b> (0.1) $\downarrow_4^{*4}$	<b>0.32</b> (0.1) $\downarrow_4^{*4}$	<b>0.32</b> (0.1) $\downarrow_4^{*4}$	<b>0.32</b> (0.1) $\downarrow_4^{*4}$	15/15
SNES	4.5(5)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	5.0(5)	137(150)	$\infty$	$\infty$	$\infty$	$\infty$ <i>7e6</i>	0/15
xNESas	1.4(1)	179(204)	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e7</i>	0/15

Table 15: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f114</b>	2.1e5	1.1e6	1.4e6	1.6e6	1.6e6	1.6e6	15/15
IPOPsaACM	<b>0.71</b> <sub>(0.3)</sub> <sup>*4</sup>	<b>0.39</b> <sub>(0.3)</sub> ↓ <sub>3</sub>	<b>0.40</b> <sub>(0.2)</sub> ↓ <sub>3</sub>	<b>0.50</b> <sub>(0.3)</sub> ↓ <sub>2</sub>	<b>0.50</b> <sub>(0.3)</sub> ↓ <sub>2</sub>	<b>0.55</b> <sub>(0.3)</sub> ↓	15/15
SNES	∞	∞	∞	∞	∞	∞ <i>2e5</i>	0/15
xNES	∞	∞	∞	∞	∞	∞ <i>6e6</i>	0/15
xNESas	∞	∞	∞	∞	∞	∞ <i>1e7</i>	0/15



Table 16: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{115}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f115</b>	2405	30268	91749	1.3e5	1.3e5	1.3e5	15/15
IPOPsaACM	<b>0.75</b> (2)	0.67(0.3)	0.31(0.2)	4.8(15)	4.8(15)	4.7(14)	15/15
SNES	1.2(1)	29(33)	$\infty$	$\infty$	$\infty$	$\infty$ 2e5	0/15
xNES	1.0(0.2)	0.25(0.0) $\downarrow$ 4	0.14(9e-3) $\downarrow$	0.62(0.8)	0.62(0.8)	0.69(0.8)	15/15
xNESas	1.0(0.1)	<b>0.24</b> (0.0) $\downarrow$ 4	<b>0.14</b> (0.0) $\downarrow$	<b>0.37</b> (0.3)	<b>0.37</b> (0.3)	<b>0.46</b> (0.5)	15/15

Table 17: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{116}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f116</b>	5.0e5	6.9e5	8.9e5	1.0e6	1.1e6	1.1e6	15/15
IPOPsaACM	<b>0.46</b> <sub>(0.1)</sub>	<b>0.35</b> <sub>(0.1)</sub>	<b>0.30</b> <sub>(0.1)</sub>	<b>0.28</b> <sub>(0.1)↓4</sub>	<b>0.29</b> <sub>(0.1)↓4</sub>	<b>0.30</b> <sub>(0.1)↓4</sub>	15/15
SNES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	101 <sub>(116)</sub>	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>7e6</i>	0/15
xNESas	39 <sub>(42)</sub>	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e7</i>	0/15

Table 18: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{117}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f117</b>	1.8e6	2.5e6	2.6e6	2.9e6	3.2e6	3.6e6	15/15
IPOPsaACM	<b>0.29</b> <sub>(0.1)↓3</sub>	<b>0.26</b> <sub>(0.1)↓4</sub>	<b>0.29</b> <sub>(0.1)↓4</sub>	<b>0.35</b> <sub>(0.2)↓4</sub>	<b>0.42</b> <sub>(0.2)↓3</sub>	<b>0.48</b> <sub>(0.4)↓2</sub>	15/15
SNES	∞	∞	∞	∞	∞	∞ <i>2e5</i>	0/15
xNES	∞	∞	∞	∞	∞	∞ <i>5e6</i>	0/15
xNESas	∞	∞	∞	∞	∞	∞ <i>8e6</i>	0/30

Table 19: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f118</b>	6908	11786	17514	26342	30062	32659	15/15
IPOPsaACM	<b>0.42</b> <sub>(0.2)</sub> <sup>*4</sup> <sub>↓4</sub>	<b>0.49</b> <sub>(0.1)</sub> <sup>*3</sup> <sub>↓4</sub>	<b>0.54</b> <sub>(0.1)</sub> <sup>*3</sup> <sub>↓3</sub>	<b>0.54</b> <sub>(0.2)</sub> <sup>*4</sup> <sub>↓4</sub>	<b>0.56</b> <sub>(0.1)</sub> <sup>*4</sup> <sub>↓4</sub>	<b>0.58</b> <sub>(0.1)</sub> <sup>*4</sup> <sub>↓4</sub>	15/15
SNES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	<i>2e5</i>	0/15
xNES	1.0(0.0)	0.90(0.0)	0.90(0.0)	1.1(0.1)	1.5(0.1)	1.8(0.0)	15/15
xNESas	0.94(0.1)	0.77(0.1)	0.80(0.1)	1.1(0.1)	1.7(0.7)	2.1(0.7)	15/15

Table 20: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{119}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f119</b>	2771	29365	35930	4.1e5	1.4e6	1.9e6	15/15
IPOPsaACM	1.5(2)	<b>0.74</b> (0.3) <sup>*2</sup>	<b>0.88</b> (0.3) <sup>*3</sup>	<b>0.33</b> (0.1) <sub>↓3</sub> <sup>*3</sup>	<b>0.25</b> (0.1) <sub>↓4</sub>	<b>0.37</b> (0.3) <sub>↓3</sub>	15/15
SNES	1.4(2)	22(24)	∞	∞	∞	∞ <i>2e5</i>	0/15
xNES	0.54(0.3) <sub>↓2</sub>	14(13)	2741(3347)	∞	∞	∞ <i>7e6</i>	0/15
xNESas	<b>0.53</b> (0.4) <sub>↓</sub>	10(10)	851(808)	∞	∞	∞ <i>1e7</i>	0/13

Table 21: 20-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f120</b>	36040	1.8e5	2.8e5	1.6e6	6.7e6	1.4e7	13/15
IPOPsaACM	<b>0.65</b> <sub>(0.5)</sub>	<b>0.80</b> <sub>(0.4)</sub> <sup>*4</sup>	<b>1.2</b> <sub>(0.6)</sub>	<b>0.87</b> <sub>(0.5)</sub>	<b>0.42</b> <sub>(0.1)</sub> ↓ <sub>3</sub>	<b>0.39</b> <sub>(0.2)</sub> ↓ <sub>3</sub>	15/15
SNES	10 <sub>(11)</sub>	∞	∞	∞	∞	∞ <i>2e5</i>	0/15
xNES	14 <sub>(23)</sub>	∞	∞	∞	∞	∞ <i>6e6</i>	0/15
xNESas	6.9 <sub>(7)</sub>	∞	∞	∞	∞	∞ <i>1e7</i>	0/15

Table 22: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b><i>f121</i></b>	249	769	1426	9304	34434	57404	15/15
IPOPsaACM	1.2(0.4)	<b>0.85</b> (0.2)	<b>0.92</b> (0.3) <sup>*2</sup>	<b>0.69</b> (0.1) <sub>↓3</sub> <sup>*4</sup>	<b>0.58</b> (0.1) <sub>↓4</sub> <sup>*4</sup>	<b>0.71</b> (0.1) <sub>↓3</sub> <sup>*4</sup>	15/15
SNES	0.83(0.2)	0.89(0.2)	1.3(0.2)	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	<b>0.74</b> (0.2)	3.4(0.6)	6.7(0.4)	2.9(0.2)	1.3(0.1)	1.1(0.1)	15/15
xNESas	0.81(0.3)	2.8(0.6)	6.3(0.5)	2.9(0.2)	1.7(0.6)	1.7(1)	15/15

Table 23: 20-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{122}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f122</b>	692	52008	1.4e5	7.9e5	2.0e6	5.8e6	15/15
IPOPsaACM	2.5(3)	<b>0.94</b> (0.6) <sup>*3</sup>	<b>0.81</b> (0.3) <sup>*3</sup>	<b>0.53</b> (0.1) <sub>↓</sub>	<b>0.51</b> (0.2) <sub>↓</sub>	<b>0.57</b> (0.3)	15/15
SNES	1.9(2)	∞	∞	∞	∞	∞ <i>2e5</i>	0/15
xNES	0.91(0.8)	∞	∞	∞	∞	∞ <i>6e6</i>	0/15
xNESas	<b>0.81</b> (0.9)	∞	∞	∞	∞	∞ <i>1e7</i>	0/13



Table 24: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{123}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f123</b>	1063	5.3e5	1.5e6	5.3e6	2.7e7	1.6e8	0
IPOPsaACM	<b>7.6</b> (8)	<b>0.77</b> (0.5)	<b>0.81</b> (0.5)	<b>1.1</b> (0.7)	<b>0.63</b> (0.4)	<b>0.92</b> (1)	0/15
SNES	7.7(9)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	9.0(9)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>6e6</i>	0/15
xNESas	11(14)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e7</i>	0/15

Table 25: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{124}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f124</b>	192	1959	40840	1.3e5	3.9e5	8.0e5	15/15
IPOPsaACM	0.86(0.4)	3.0(0.8)	2.2(2)	<b>1.4</b> (0.5)	<b>0.76</b> (0.3)	<b>4.0</b> (5)	14/15
SNES	<b>0.58</b> (0.4) $\downarrow$	<b>0.69</b> (0.2) $\downarrow$	0.66(0.5)	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	0.63(0.3)	2.7(0.3)	<b>0.58</b> (0.1)	6.4(7)	$\infty$	$\infty$ <i>7e6</i>	0/15
xNESas	0.84(0.3)	2.7(0.5)	0.59(0.1)	4.0(3)	$\infty$	$\infty$ <i>2e7</i>	0/15

Table 26: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f125</b>	1	1	1	2.5e7	8.0e7	8.1e7	4/15
IPOPsaACM	<b>1</b> (0)	1083(1766)	<b>3.3e6</b> (2e6)	<b>0.61</b> (0.5)	<b>1.1</b> (1)	<b>1.1</b> (1)	3/15
SNES	1.3(0.5)	625(509)	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	1.5(1)	<b>451</b> (271)	$\infty$	$\infty$	$\infty$	$\infty$ <i>6e6</i>	0/30
xNESas	1.7(1)	470(238)	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e7</i>	0/15

Table 27: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best}} 2009$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f126</b>	1	1	1	$\infty$	$\infty$	$\infty$	0
IPOPsaACM	<i>1(0)</i>	<b>7156</b> (4580)	$\infty$	.	.	.	0/15
SNES	1.3(0.5)	2.3e4(2e4)	$\infty$	.	.	.	0/15
xNES	1.2(0.5)	2.5e4(6e4)	$\infty$	.	.	.	0/30
xNESas	1.4(1)	2.7e4(5e4)	$\infty$	.	.	.	0/15

Table 28: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f127</b>	1	1	1	4.4e6	7.3e6	7.4e6	15/15
IPOPsaACM	<b>1</b> (0)	238(106)	<b>3.3e5</b> (4e5)	<b>0.75</b> (0.6)	<b>0.93</b> (0.5)	<b>0.97</b> (0.6)	14/15
SNES	1.2(0.5)	167(80)	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	1.4(1)	<b>128</b> (63)	$\infty$	$\infty$	$\infty$	$\infty$ <i>6e6</i>	0/30
xNESas	1.5(0.5)	131(87)	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e7</i>	0/15

Table 29: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{128}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f128</b>	1.4e5	1.3e7	1.7e7	1.7e7	1.7e7	1.7e7	9/15
IPOPsaACM	<b>1.3</b> (2)	0.59(0.8)	1.1(1)	1.1(2)	1.1(2)	<b>1.1</b> (1)	8/15
SNES	4.2(5)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ 2e5	0/15
xNES	28(32)	0.97(0.9)	1.2(1)	2.0(2)	3.4(4)	3.4(4)	3/30
xNESas	19(23)	<b>0.40</b> (0.5)	<b>0.78</b> (0.8)	<b>1.0</b> (1)	<b>1.0</b> (1)	1.3(1)	6/15

Table 30: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{129}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f129</b>	7.8e6	4.1e7	4.2e7	4.2e7	4.2e7	4.2e7	5/15
IPOPsaACM	<b>0.41</b> (0.9)	<b>0.28</b> (0.5)	<b>0.36</b> (0.5)	<b>0.36</b> (0.5)	<b>0.36</b> (0.5)	<b>0.36</b> (0.5)	9/15
SNES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>6e6</i>	0/30
xNESas	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e7</i>	0/15

Table 31: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f130</b>	4904	93149	2.5e5	2.5e5	2.6e5	2.6e5	7/15
IPOPsaACM	<b>0.55</b> (1)	27(34)	30(42)	30(43)	30(41)	30(39)	12/15
SNES	0.76(1)	<b>0.19</b> (0.3)	<b>0.09</b> (0.1)	<b>0.11</b> (0.1)	<b>0.36</b> (0.3)	<b>2.1</b> (2)	2/15
xNES	14(20)	10(9)	4.9(5)	4.9(5)	4.9(5)	4.9(5)	29/30
xNESas	15(23)	5.3(4)	5.4(9)	5.4(9)	5.4(9)	5.4(9)	15/15



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