

# Comparison tables: BBOB 2012 noisy testbed in 5-D

The BBOBies

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## Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2012, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2012>. 4 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [4, 2]. The experimental set-up is described in [3].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [1]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [3] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values. Table 1 gives an overview on all algorithms submitted to the noise-free testbed in 2012.

Table 1: Names and references of all algorithms submitted for the noise-free testbed

algorithm name	short	paper	reference
IPOPsaACM		Black-box Optimization Benchmarking of IPOP-saACM-ES on the BBOB-2012 Noisy Testbed (Page 261)	[8]
SNES		Benchmarking Separable Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 205)	[7]
xNES		Benchmarking Exponential Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 213)	[5]
xNESas		Benchmarking Natural Evolution Strategies with Adaptation Sampling on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 229)	[6]
SNES, xNES, xNESas		Comparing Natural Evolution Strategies to BIPOP-CMA-ES on Noiseless and Noisy Black-Box Optimization Testbeds (Page 237)	[9]

Table 2: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f101</b>	11	37	44	62	69	75	15/15
IPOPsaACM	<b>1.9</b> (1)	<b>2.1</b> (0.5)	<b>2.2</b> (0.5) <sup>*3</sup>	<b>2.2</b> (0.5) <sup>*4</sup>	<b>2.5</b> (0.3) <sup>*4</sup>	<b>2.8</b> (0.3) <sup>*4</sup>	15/15
SNES	3.8(2)	2.5(0.9)	4.3(0.8)	6.1(0.7)	8.8(1.0)	11(1)	15/15
xNES	3.4(1)	2.4(1)	5.4(0.9)	10(1)	14(1)	18(0.6)	15/15
xNESas	2.8(2)	2.4(1)	5.2(2)	7.9(2)	10(2)	13(3)	15/15

Table 3: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f102</b>	11	35	50	72	86	99	15/15
IPOPsaACM	<b>2.6</b> (2)	<b>2.1</b> (0.7)	<b>2.0</b> (0.5) <sup>*3</sup>	<b>1.9</b> (0.4) <sup>*4</sup>	<b>2.1</b> (0.3) <sup>*4</sup>	<b>2.2</b> (0.3) <sup>*4</sup>	15/15
SNES	3.5(2)	2.3(1)	3.7(1)	5.4(0.7)	7.3(0.7)	8.6(0.4)	15/15
xNES	3.1(4)	2.8(1)	4.9(1)	8.8(1)	12(1)	14(1)	15/15
xNESas	3.3(3)	2.7(2)	4.7(1)	7.3(1)	9.2(1)	10(2)	15/15

Table 4: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f103</b>	11	28	30	31	35	115	15/15
IPOPsaACM	3.0(1)	2.8(0.7)	<b>3.4(0.9)</b> * <sup>2</sup>	<b>4.6(1)</b> * <sup>4</sup>	<b>7.1(3)</b> * <sup>4</sup>	<b>3.2(1)</b> * <sup>4</sup>	15/15
SNES	2.7(2)	<b>2.7(1)</b>	5.5(1)	13(2)	26(15)	21(11)	15/15
xNES	3.7(2)	3.6(1)	8.2(2)	20(3)	31(3)	13(1)	15/15
xNESas	<b>2.7(2)</b>	2.9(2)	7.2(2)	16(3)	24(5)	11(2)	15/15

Table 5: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{104}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f104</b>	173	773	1287	1768	2040	2284	15/15
IPOPsaACM	<b>0.88</b> (0.3)	<b>1.5</b> (1)	<b>1.1</b> (1)	<b>0.89</b> (0.8)	<b>0.80</b> (0.7)*	<b>0.73</b> (0.7)*	15/15
SNES	1.5(0.6)	21(26)	44(42)	$\infty$	$\infty$	$\infty$	0/15
xNES	1.4(0.7)	2.4(0.9)	5.6(10)	7.3(11)	6.4(10)	5.9(9)	15/15
xNESas	1.4(0.4)	2.4(0.6)	2.7(6)	2.3(4)	2.1(4)	2.0(3)	15/15

Table 6: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{105}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f105</b>	167	1436	5174	10388	10824	11202	15/15
IPOPsaACM	1.4 <sup>(0.5)</sup>	<b>1.5</b> <sup>(2)</sup>	<b>0.63</b> <sup>(0.4)</sup>	<b>0.33</b> <sup>(0.2)</sup> <sub>↓3</sub>	<b>0.32</b> <sup>(0.2)</sup> <sub>↓3</sub>	<b>0.32</b> <sup>(0.2)</sup> <sub>↓3</sub>	15/15
SNES	1.7 <sup>(0.4)</sup>	17 <sup>(21)</sup>	12 <sup>(12)</sup>	35 <sup>(36)</sup>	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	<b>1.3</b> <sup>(0.5)</sup>	3.6 <sup>(6)</sup>	4.9 <sup>(7)</sup>	3.6 <sup>(5)</sup>	4.0 <sup>(5)</sup>	4.0 <sup>(5)</sup>	15/15
xNESas	1.4 <sup>(0.5)</sup>	4.0 <sup>(4)</sup>	14 <sup>(13)</sup>	11 <sup>(7)</sup>	11 <sup>(7)</sup>	10 <sup>(7)</sup>	15/15

Table 7: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{106}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f106</b>	92	529	1050	2666	2887	3087	15/15
IPOPsaACM	<b>1.7</b> (0.9)	<b>0.89</b> (0.2) <sup>*2</sup>	<b>0.60</b> (0.2) <sup>*3</sup>	<b>0.30</b> (0.1) <sub>↓4</sub> <sup>*3</sup>	<b>0.32</b> (0.1) <sub>↓4</sub> <sup>*3</sup>	<b>0.36</b> (0.1) <sub>↓4</sub> <sup>*3</sup>	15/15
SNES	3.9(1)	26(32)	209(239)	276(296)	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	2.9(1.0)	2.0(0.8)	2.2(0.8)	1.2(0.9)	1.2(0.9)	1.3(1)	15/15
xNESas	2.7(0.8)	3.3(0.9)	3.7(5)	2.2(3)	2.2(3)	2.7(3)	15/15

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Table 8: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{107}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f107</b>	40	228	453	940	1376	1850	15/15
IPOPsaACM	<b>1.4</b> (2)	<b>1.1</b> (0.7)	1.4(1)	<b>1.3</b> (0.8)	<b>1.4</b> (1.0)	1.9(1)	15/15
SNES	4.2(6)	2.0(1)	<b>1.4</b> (0.8)	1.3(0.9)	1.4(0.7)	<b>1.3</b> (0.5)	15/15
xNES	3.2(3)	31(66)	20(33)	10(16)	7.6(11)	45(8)	14/15
xNESas	3.2(5)	7.1(1)	4.2(0.5)	6.9(11)	7.2(8)	7.0(10)	15/15

Table 9: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f108</b>	87	5144	14469	30935	58628	80667	15/15
IPOPsaACM	<b>7.8</b> <sup>(9)</sup>	<b>1.1</b> <sup>(1)</sup>	<b>0.60</b> <sup>(0.4)*2</sup>	<b>0.80</b> <sup>(0.5)*4</sup>	<b>0.74</b> <sup>(0.4)*4</sup>	<b>1.0</b> <sup>(0.6)</sup>	15/15
SNES	15 <sup>(20)</sup>	1.5 <sup>(3)</sup>	8.4 <sup>(10)</sup>	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	84 <sup>(117)</sup>	18 <sup>(22)</sup>	36 <sup>(28)</sup>	$\infty$	$\infty$	$\infty$ <i>7e5</i>	0/15
xNESas	69 <sup>(120)</sup>	12 <sup>(17)</sup>	56 <sup>(59)</sup>	$\infty$	$\infty$	$\infty$ <i>1e6</i>	0/15

Table 10: 05-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f109</b>	11	57	216	572	873	946	15/15
IPOPsaACM	<b>2.9</b> (2)	<b>1.6</b> (0.6)	<b>0.83</b> (0.3)	<b>1.2</b> (0.3)	<b>1.2</b> (0.3) <sup>*2</sup>	<b>1.6</b> (0.4) <sup>*3</sup>	15/15
SNES	4.4(2)	1.9(0.7)	0.93(0.3)	1.8(1)	13(21)	371(385)	0/15
xNES	3.4(2)	2.0(0.8)	1.4(0.3)	2.0(0.5)	2.3(0.2)	4.1(0.7)	15/15
xNESas	3.6(2)	1.7(0.7)	1.3(0.5)	1.8(0.5)	2.3(0.6)	4.1(0.8)	15/15

Table 11: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{110}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f110</b>	949	33625	1.2e5	5.9e5	6.0e5	6.1e5	15/15
IPOPsaACM	0.71(0.3)	5.6(7)	3.5(4)	<b>0.78</b> (0.8)	<b>0.84</b> (0.8)	<b>0.84</b> (0.8)	15/15
SNES	0.76(1)	<b>0.33</b> (0.2) <sub>↓</sub>	<b>0.65</b> (0.7)	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	0.49(0.2)	1.3(2)	2.1(3)	1.7(2)	2.2(2)	2.2(2)	7/15
xNESas	<b>0.44</b> (0.2)	1.9(2)	3.6(5)	1.2(1)	1.6(2)	2.3(3)	8/15

Table 12: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{111}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f111</b>	6856	6.1e5	8.8e6	2.3e7	3.1e7	3.1e7	3/15
IPOPsaACM	<b>0.50</b> (0.3)	7.4(8)	1.8(2)	<b>1.00</b> (1.0)	<b>0.74</b> (0.8)	<b>0.74</b> (0.8)	3/15
SNES	1.9(2)	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	7.2(9)	4.1(5)	<b>0.61</b> (0.7)	$\infty$	$\infty$	$\infty$ <i>8e5</i>	0/15
xNESas	5.4(8)	<b>1.8</b> (2)	0.96(1)	$\infty$	$\infty$	$\infty$ <i>1e6</i>	0/15

Table 13: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{112}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f112</b>	107	1684	3421	4502	5132	5596	15/15
IPOPsaACM	<b>1.4</b> <sub>(0.6)</sub> *	<b>1.5</b> <sub>(2)</sub>	<b>1.2</b> <sub>(0.9)</sub>	<b>1.2</b> <sub>(0.6)</sub>	<b>1.2</b> <sub>(0.6)</sub>	<b>1.2</b> <sub>(0.6)</sub>	15/15
SNES	1.9 <sub>(0.4)</sub>	16 <sub>(19)</sub>	19 <sub>(20)</sub>	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	4.6 <sub>(1)</sub>	3.0 <sub>(5)</sub>	3.0 <sub>(3)</sub>	6.5 <sub>(8)</sub>	12 <sub>(15)</sub>	18 <sub>(28)</sub>	15/15
xNESas	2.3 <sub>(1)</sub>	2.6 <sub>(5)</sub>	7.9 <sub>(10)</sub>	17 <sub>(18)</sub>	28 <sub>(23)</sub>	37 <sub>(38)</sub>	15/15

Table 14: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{113}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f113</b>	133	1883	8081	24128	24128	24402	15/15
IPOPsaACM	3.0(2)	0.82(0.8)	<b>0.47</b> (0.6)	<b>0.35</b> (0.4)	<b>0.35</b> (0.4)	<b>0.35</b> (0.4)	15/15
SNES	1.8(2)	<b>0.78</b> (0.9)	2.1(3)	3.1(3)	3.1(3)	4.1(4)	5/15
xNES	10(6)	3.3(8)	2.1(3)	1.2(2)	1.2(2)	1.2(2)	15/15
xNESas	<b>1.2</b> (1)	2.4(4)	2.5(4)	1.4(2)	1.4(2)	1.5(2)	15/15

Table 15: 05-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f114</b>	767	14720	56311	83272	83272	84949	15/15
IPOPsaACM	2.6(3)	<b>0.73</b> (0.4)	<b>0.54</b> (0.4) <sup>*3</sup>	<b>0.44</b> (0.2) <sup>*2</sup>	<b>0.44</b> (0.2) <sup>*2</sup>	<b>0.44</b> (0.3) <sup>*2</sup>	15/15
SNES	<b>2.6</b> (3)	2.4(3)	$\infty$	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	10(17)	10(10)	33(37)	$\infty$	$\infty$	$\infty$ <i>8e5</i>	0/15
xNESas	8.0(13)	9.1(13)	157(166)	$\infty$	$\infty$	$\infty$ <i>1e6</i>	0/15



Table 16: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{115}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f115</b>	64	485	1829	2550	2550	2970	15/15
IPOPsaACM	1.6(0.6)	0.98(1)	<b>1.2(1)</b>	<b>1.2(0.8)</b>	<b>1.2(0.8)</b>	<b>1.1(0.7)</b>	15/15
SNES	1.6(0.8)	1.8(2)	4.4(4)	40(43)	40(47)	45(43)	4/15
xNES	1.7(1)	1.9(0.3)	2.3(5)	2.5(5)	2.5(5)	2.6(4)	15/15
xNESas	<b>1.3(0.9)</b>	<b>0.88(0.4)</b>	1.8(4)	1.8(4)	1.8(4)	1.6(3)	15/15

Table 17: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{116}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f116</b>	5730	14472	22311	26868	30329	31661	15/15
IPOPsaACM	1.0(1)	<b>0.74</b> (0.8)	<b>0.56</b> (0.5)	<b>0.59</b> (0.5)	<b>0.56</b> (0.4)↓	<b>0.56</b> (0.4)↓	15/15
SNES	1.6(1)	5.9(6)	∞	∞	∞	∞ <i>5e4</i>	0/15
xNES	<b>0.62</b> (1)	0.78(1)	1.3(2)	1.2(1)	1.2(1)	1.2(1)	14/15
xNESas	1.4(2)	1.2(2)	1.1(2)	1.3(1)	1.6(2)	1.8(2)	15/15

Table 18: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{117}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f117</b>	26686	76052	1.1e5	1.4e5	1.7e5	1.9e5	15/15
IPOPsaACM	<b>0.60</b> <sub>(0.5)</sub> <sup>*2</sup>	<b>0.43</b> <sub>(0.3)</sub> <sup>*2</sup>	<b>0.42</b> <sub>(0.3)</sub> <sup>*2</sup> <sub>↓2</sub>	<b>0.54</b> <sub>(0.3)</sub> ↓	<b>0.59</b> <sub>(0.3)</sub>	<b>0.60</b> <sub>(0.2)</sub>	15/15
SNES	6.3 <sub>(6)</sub>	∞	∞	∞	∞	∞ <i>5e4</i>	0/15
xNES	9.4 <sub>(13)</sub>	47 <sub>(49)</sub>	∞	∞	∞	∞ <i>8e5</i>	0/15
xNESas	8.4 <sub>(6)</sub>	39 <sub>(47)</sub>	∞	∞	∞	∞ <i>1e6</i>	0/15

Table 19: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f118</b>	429	1217	1555	1998	2430	2913	15/15
IPOPsaACM	<b>0.49</b> <sub>(0.1)</sub> <sup>*</sup> <sub>↓4</sub> <sup>3</sup>	<b>0.25</b> <sub>(0.1)</sub> <sup>*</sup> <sub>↓4</sub> <sup>3</sup>	<b>0.33</b> <sub>(0.1)</sub> <sup>*</sup> <sub>↓4</sub> <sup>2</sup>	<b>0.48</b> <sub>(0.1)</sub> <sup>*</sup> <sub>↓4</sub> <sup>2</sup>	<b>0.63</b> <sub>(0.1)</sub> <sup>*</sup> <sub>↓3</sub> <sup>2</sup>	<b>0.74</b> <sub>(0.3)</sub> <sup>*</sup> <sub>↓2</sub>	15/15
SNES	11 <sub>(9)</sub>	33 <sub>(36)</sub>	$\infty$	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	1.0 <sub>(0.4)</sub>	0.50 <sub>(0.1)</sub> <sub>↓4</sub>	0.52 <sub>(0.1)</sub> <sub>↓4</sub>	0.73 <sub>(0.1)</sub> <sub>↓2</sub>	1.0 <sub>(0.2)</sub>	1.6 <sub>(0.2)</sub>	15/15
xNESas	1.00 <sub>(0.4)</sub>	0.48 <sub>(0.1)</sub> <sub>↓4</sub>	0.48 <sub>(0.1)</sub> <sub>↓4</sub>	0.69 <sub>(0.2)</sub> <sub>↓2</sub>	0.96 <sub>(0.2)</sub>	1.1 <sub>(0.2)</sub>	15/15

Table 20: 05-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{119}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f119</b>	12	657	1136	10372	35296	49747	15/15
IPOPsaACM	4.9(10)	1.1(2)	0.99(0.9)	<b>0.50</b> (0.5)	<b>0.47</b> (0.2) $\downarrow_2$	<b>0.61</b> (0.5) $\ast^2$	15/15
SNES	3.9(6)	0.64(0.9)	<b>0.64</b> (0.5)	0.84(0.9)	$\infty$	<i>5e4</i>	0/15
xNES	<b>1.9</b> (2)	<b>0.38</b> (0.4)	0.66(0.2)	2.6(3)	1.5(1)	12(13)	9/15
xNESas	3.8(4)	2.1(1)	6.3(13)	1.6(2)	2.3(3)	5.9(6)	15/15

Table 21: 05-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f120</b>	16	2900	18698	72438	3.3e5	5.5e5	15/15
IPOPsaACM	26 <sup>(56)</sup>	1.1 <sup>(1)</sup>	<b>0.80</b> <sup>(0.5)</sup> *	<b>0.52</b> <sup>(0.3)</sup> * <sup>4</sup>	<b>0.36</b> <sup>(0.3)</sup> ↓ <sub>3</sub>	<b>0.64</b> <sup>(0.5)</sup>	15/15
SNES	12 <sup>(32)</sup>	<b>0.72</b> <sup>(0.9)</sup>	38 <sup>(42)</sup>	∞	∞	∞ <i>5e4</i>	0/15
xNES	<b>9.0</b> <sup>(12)</sup>	14 <sup>(17)</sup>	43 <sup>(42)</sup>	∞	∞	∞ <i>8e5</i>	0/15
xNESas	51 <sup>(18)</sup>	13 <sup>(21)</sup>	25 <sup>(34)</sup>	∞	∞	∞ <i>1e6</i>	0/15

Table 22: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f121</b>	8.6	111	273	1583	3870	6195	15/15
IPOPsaACM	3.3(4)	0.98(0.5)	0.97(0.5)	<b>1.0</b> (0.6)	<b>0.95</b> (0.4)	<b>0.86</b> (0.2)	15/15
SNES	<b>2.6</b> (3)	1.1(0.8)	<b>0.77</b> (0.4)	11(14)	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	2.7(3)	0.96(0.5)	1.2(0.2)	1.3(0.5)	1.2(1)	1.7(2)	15/15
xNESas	2.6(2)	<b>0.85</b> (0.6)	0.96(0.5)	1.6(0.8)	1.5(2)	2.3(3)	15/15

Table 23: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{122}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f122</b>	10	1727	9190	30087	53743	1.1e5	15/15
IPOPsaACM	2.6(3)	1.2(0.8)	<b>0.75</b> (0.5)	<b>0.58</b> (0.2) <sub>↓</sub> <sup>*4</sup>	<b>0.77</b> (0.3) <sup>*4</sup>	<b>0.66</b> (0.3) <sub>↓</sub>	15/15
SNES	7.8(10)	<b>0.65</b> (0.6)	2.3(3)	∞	∞	∞ <i>5e4</i>	0/15
xNES	<b>1.7</b> (2)	1.9(2)	6.4(4)	200(214)	∞	∞ <i>8e5</i>	0/15
xNESas	5.0(4)	5.5(11)	8.9(8)	583(644)	∞	∞ <i>1e6</i>	0/15



Table 24: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{123}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f123</b>	11	16066	81505	3.4e5	6.7e5	2.2e6	15/15
IPOPsaACM	23(52)	<b>0.74</b> (0.4)	<b>0.70</b> (0.5)	<b>0.58</b> (0.3)	<b>0.80</b> (0.7)	<b>0.71</b> (0.5)	15/15
SNES	12(16)	3.1(3)	$\infty$	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	36(70)	10(9)	$\infty$	$\infty$	$\infty$	$\infty$ <i>8e5</i>	0/15
xNESas	<b>6.6</b> (9)	7.2(7)	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e6</i>	0/15

Table 25: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{124}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f124</b>	10	202	1040	20478	45337	95200	15/15
IPOPsaACM	2.6(2)	1.3(0.6)	3.1(4)	<b>0.85</b> (0.7)	<b>0.97</b> (0.8) <sup>*3</sup>	<b>4.1</b> (8)	15/15
SNES	2.9(4)	1.2(1.0)	<b>1.2</b> (0.9)	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	<b>2.5</b> (2)	1.4(0.4)	3.8(10)	2.0(2)	19(21)	112(125)	1/15
xNESas	2.9(3)	<b>1.2</b> (0.5)	2.0(0.7)	1.1(1)	<b>36</b> (37)	60(67)	1/15

Table 26: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f125</b>	1	1	1	2.4e5	2.4e5	2.5e5	15/15
IPOPsaACM	1.5(0)	<b>18</b> (18)	4308(4084)	<b>0.56</b> (0.6)	<b>0.79</b> (0.9)	<b>4.8</b> (6)	15/15
SNES	1.2(0.5)	33(34)	<b>3958</b> (3495)	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	<b>1.1</b> (0)	29(26)	9476(1e4)	$\infty$	$\infty$	$\infty$ <i>8e5</i>	0/15
xNESas	1.3(0.5)	23(22)	7786(7916)	$\infty$	$\infty$	$\infty$ <i>1e6</i>	0/15

Table 27: 05-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	#1e0	1e-1	1e-3	1e-5	1e-7	#succ
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Table 28: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f127</b>	1	1	1	3.4e5	3.9e5	4.0e5	15/15
IPOPsaACM	<b>1</b> (0)	20(22)	<b>2432</b> (3044)	<b>0.30</b> (0.3)	<b>0.32</b> (0.3)↓	<b>0.33</b> (0.3)↓	15/15
SNES	1.1(0.5)	<b>19</b> (16)	3060(2752)	∞	∞	∞ <i>5e4</i>	0/15
xNES	1.1(0)	19(22)	3395(5420)	31(36)	∞	∞ <i>7e5</i>	0/15
xNESas	1.1(0.5)	20(16)	3858(5345)	∞	∞	∞ <i>1e6</i>	0/15

Table 29: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{128}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f128</b>	111	4248	7808	12447	17217	21162	15/15
IPOPsaACM	<b>1.3</b> (1.0)	16(21)	265(321)	203(342)	147(247)	124(148)	11/15
SNES	1.6(2)	<b>1.1</b> (1)	<b>0.78</b> (0.8)	<b>0.51</b> (0.5)	<b>0.40</b> (0.3) $\downarrow 2$	<b>0.45</b> (0.4) $\downarrow 2$	15/15
xNES	7.1(2)	7.3(11)	5.2(6)	3.3(4)	2.4(3)	2.0(2)	15/15
xNESas	22(67)	6.2(9)	5.7(7)	3.6(4)	2.6(3)	2.1(2)	15/15

Table 30: 05-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{129}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f129</b>	64	10710	59443	2.8e5	5.1e5	5.8e5	15/15
IPOPsaACM	9.1(12)	10(21)	19(42)	13(18)	<b>7.1</b> (10)	<b>6.3</b> (9)	9/15
SNES	<b>7.6</b> (14)	<b>1.2</b> (1)	<b>1.8</b> (2)	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
xNES	38(34)	15(10)	10(8)	<b>11</b> (13)	$\infty$	$\infty$ <i>7e5</i>	0/15
xNESas	17(16)	11(11)	8.6(11)	14(16)	$\infty$	$\infty$ <i>1e6</i>	0/15

Table 31: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f130</b>	55	812	3034	32823	33889	34528	10/15
IPOPsaACM	<b>1.4</b> (0.9)	27(27)	126(131)	42(76)	41(74)	40(72)	13/15
SNES	2.9(7)	<b>4.8</b> (5)	<b>1.6</b> (2)	<b>0.19</b> (0.2)	<b>0.44</b> (0.4)	2.7(2)	3/15
xNES	13(1)	67(84)	25(25)	2.4(2)	2.3(2)	<b>2.3</b> (2)	15/15
xNESas	17(0.9)	67(79)	28(48)	2.6(4)	2.5(4)	2.5(4)	15/15



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