

# Comparison tables: BBOB 2012 noisy testbed in 3-D

The BBOBies

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## Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2012, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2012>. 4 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [4, 2]. The experimental set-up is described in [3].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [1]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [3] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values. Table 1 gives an overview on all algorithms submitted to the noise-free testbed in 2012.

Table 1: Names and references of all algorithms submitted for the noise-free testbed

algorithm name	short	paper	reference
IPOPsaACM		Black-box Optimization Benchmarking of IPOP-saACM-ES on the BBOB-2012 Noisy Testbed (Page 261)	[8]
SNES		Benchmarking Separable Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 205)	[7]
xNES		Benchmarking Exponential Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 213)	[5]
xNESas		Benchmarking Natural Evolution Strategies with Adaptation Sampling on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 229)	[6]
SNES, xNES, xNESas		Comparing Natural Evolution Strategies to BIPOP-CMA-ES on Noiseless and Noisy Black-Box Optimization Testbeds (Page 237)	[9]

Table 2: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f101</b>	3.6	13	19	28	33	38	15/15
IPOPsaACM	<b>3.7</b> <sup>(4)</sup>	<b>3.0</b> <sup>(2)</sup>	<b>3.3</b> <sup>(0.6)</sup>	<b>3.1</b> <sup>(0.7)</sup> <sup>*3</sup>	<b>3.4</b> <sup>(0.5)</sup> <sup>*4</sup>	<b>3.5</b> <sup>(0.4)</sup> <sup>*4</sup>	15/15
SNES	4.3 <sup>(3)</sup>	3.2 <sup>(1)</sup>	3.9 <sup>(2)</sup>	7.7 <sup>(1)</sup>	11 <sup>(1)</sup>	13 <sup>(0.9)</sup>	15/15
xNES	5.3 <sup>(4)</sup>	3.8 <sup>(2)</sup>	5.4 <sup>(2)</sup>	8.6 <sup>(2)</sup>	12 <sup>(2)</sup>	14 <sup>(1)</sup>	15/15
xNESas	4.9 <sup>(4)</sup>	3.3 <sup>(2)</sup>	4.3 <sup>(2)</sup>	7.6 <sup>(2)</sup>	11 <sup>(2)</sup>	13 <sup>(2)</sup>	15/15

Table 3: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f102</b>	3.6	12	23	32	39	48	15/15
IPOPsaACM	4.4(6)	3.2(2)	<b>2.5</b> (1)	<b>2.7</b> <sub>(0.5)</sub> <sup>*4</sup>	<b>2.9</b> <sub>(0.6)</sub> <sup>*4</sup>	<b>3.0</b> <sub>(0.5)</sub> <sup>*4</sup>	15/15
SNES	4.9(6)	3.8(2)	3.4(2)	6.7(1)	9.1(1)	10(1)	15/15
xNES	4.6(4)	3.5(2)	4.1(3)	6.9(1)	10(2)	11(1)	15/15
xNESas	<b>3.6</b> (5)	<b>3.2</b> (2)	3.8(2)	6.8(1)	8.6(1)	10(2)	15/15

Table 4: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f103</b>	3.6	13	19	19	23	43	15/15
IPOPsaACM	<b>2.9</b> <sup>(3)</sup>	<b>2.6</b> <sup>(2)</sup>	<b>3.1</b> <sup>(0.8)</sup>	<b>4.8</b> <sup>(1.0)*4</sup>	<b>6.8</b> <sup>(3)*3</sup>	<b>4.9</b> <sup>(2)*4</sup>	15/15
SNES	4.4 <sup>(4)</sup>	3.1 <sup>(2)</sup>	4.2 <sup>(1)</sup>	12 <sup>(2)</sup>	24 <sup>(15)</sup>	32 <sup>(25)</sup>	15/15
xNES	4.5 <sup>(5)</sup>	3.0 <sup>(2)</sup>	4.3 <sup>(3)</sup>	11 <sup>(2)</sup>	18 <sup>(4)</sup>	14 <sup>(2)</sup>	15/15
xNESas	5.2 <sup>(5)</sup>	3.5 <sup>(2)</sup>	4.6 <sup>(2)</sup>	12 <sup>(3)</sup>	15 <sup>(5)</sup>	12 <sup>(2)</sup>	15/15

Table 5: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{104}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f104</b>	30	207	602	648	658	668	15/15
IPOPsaACM	3.0(2)	<b>1.4</b> (0.4)	<b>0.83</b> (1)	<b>0.91</b> (1)*	<b>0.95</b> (1)* <sup>2</sup>	<b>0.98</b> (1)* <sup>2</sup>	15/15
SNES	<b>1.8</b> (0.9)	1.9(4)	<b>28</b> (26)	125(120)	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	2.4(1)	1.7(2)	<b>2.3</b> (4)	3.3(4)	3.4(4)	3.6(4)	15/15
xNESas	2.7(1)	4.0(0.5)	4.9(8)	10(16)	10(16)	10(15)	15/15

Table 6: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{105}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f105</b>	28	507	1070	3247	3271	3297	5/15
IPOPsaACM	3.4(2)	0.97(2)	<b>1.3</b> (2)	<b>0.47</b> (0.5)	<b>0.48</b> (0.5)	<b>0.48</b> (0.5)	15/15
SNES	<b>2.4</b> (2)	<b>0.92</b> (0.9)	16(15)	45(46)	135(143)	$\infty$ <i>3e4</i>	0/15
xNES	2.4(0.9)	2.8(8)	3.9(8)	3.0(3)	3.0(3)	3.1(3)	15/15
xNESas	17(2)	6.0(15)	9.3(11)	6.0(10)	6.7(10)	6.6(10)	15/15

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Table 7: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{106}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f106</b>	29	68	156	759	1294	1447	15/15
IPOPsaACM	2.5(1)	<b>2.7</b> (2)	<b>1.8</b> (0.9)*	<b>0.48</b> (0.2)* <sup>2</sup>	<b>0.36</b> (0.1)* <sub>↓4</sub> <sup>2</sup>	<b>0.36</b> (0.1)* <sub>↓4</sub> <sup>3</sup>	15/15
SNES	2.6(2)	5.7(9)	77(86)	∞	∞	∞ <i>3e4</i>	0/15
xNES	<b>2.3</b> (1)	3.9(2)	10(20)	2.6(4)	1.8(2)	1.7(2)	15/15
xNESas	2.7(2)	16(3)	9.3(4)	3.3(6)	2.1(4)	2.0(3)	15/15



Table 8: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{107}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f107</b>	5.9	47	153	325	505	685	15/15
IPOPsaACM	<b>4.0</b> (3)	<b>1.4</b> (1)	<b>0.96</b> (0.5)	<b>1.3</b> (0.7)	<b>1.3</b> (0.6)	1.3(0.4)	15/15
SNES	15(23)	3.3(5)	1.5(2)	1.5(0.7)	1.4(0.4)	<b>1.3</b> (0.4)	15/15
xNES	64(26)	17(32)	5.6(10)	3.9(5)	3.0(3)	2.5(2)	15/15
xNESas	107(24)	14(3)	5.0(1)	3.0(1.0)	2.4(0.5)	2.9(6)	15/15

Table 9: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f108</b>	5.8	98	1966	10825	17187	32181	15/15
IPOPsaACM	<b>11</b> <sub>(15)</sub>	7.2 <sub>(11)</sub>	1.1 <sub>(1)</sub>	<b>0.83</b> <sub>(0.5)</sub> <sup>*4</sup>	<b>1.1</b> <sub>(0.8)</sub> <sup>*4</sup>	<b>0.93</b> <sub>(0.4)</sub> <sup>*4</sup>	15/15
SNES	26 <sub>(40)</sub>	<b>6.0</b> <sub>(8)</sub>	<b>0.69</b> <sub>(0.5)</sub>	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	62 <sub>(34)</sub>	36 <sub>(54)</sub>	12 <sub>(19)</sub>	150 <sub>(165)</sub>	$\infty$	$\infty$ <i>2e5</i>	0/15
xNESas	213 <sub>(641)</sub>	56 <sub>(101)</sub>	10 <sub>(11)</sub>	80 <sub>(85)</sub>	$\infty$	$\infty$ <i>4e5</i>	0/15

Table 10: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f109</b>	3.6	21	93	193	251	251	15/15
IPOPsaACM	<b>3.2</b> (3)	<b>1.7</b> (1)	0.85(0.2)	2.1(2)	3.2(2)	<b>4.5</b> (3)	15/15
SNES	3.9(5)	1.8(1)	<b>0.73</b> (0.4)	1.8(1)	9.1(11)	502(593)	0/15
xNES	3.6(5)	1.9(1)	1.00(0.6)	<b>1.7</b> (0.8)	3.0(2)	5.7(2)	15/15
xNESas	3.8(4)	1.8(2)	0.86(0.5)	1.8(0.7)	<b>2.6</b> (0.8)	6.6(5)	15/15

Table 11: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{110}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f110</b>	56	922	6277	35327	61979	63571	15/15
IPOPsaACM	1.6(1)	2.7(4)	3.0(4)	<b>0.97</b> (1.0)	<b>0.57</b> (0.6)	<b>0.57</b> (0.6)	15/15
SNES	2.7(3)	<b>0.82</b> (1)	2.8(2)	1.8(2)	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	2.9(3)	4.5(6)	<b>2.1</b> (3)	1.1(1)	0.74(0.9)	0.72(0.8)	15/15
xNESas	<b>1.5</b> (1.0)	2.5(4)	4.5(3)	1.8(2)	1.1(0.9)	1.3(1.0)	15/15

Table 12: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{111}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f111</b>	174	3475	29972	1.9e5	1.4e6	1.5e6	14/15
IPOPsaACM	3.8(6)	1.2(2)	9.1(18)	<b>4.9</b> (4)	<b>0.70</b> (0.6)	<b>0.71</b> (0.6)	15/15
SNES	<b>2.1</b> (2)	<b>0.94</b> (0.4)	7.1(8)	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	12(16)	4.7(6)	3.1(3)	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNESas	12(20)	3.5(4)	<b>1.3</b> (2)	16(17)	$\infty$	$\infty$ <i>4e5</i>	0/15

Table 13: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{112}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f112</b>	29	338	1568	2849	3105	3534	15/15
IPOPsaACM	3.3(2)	1.7(2)	<b>0.87</b> (0.9)	<b>0.78</b> (0.4)	<b>0.83</b> (0.4)	<b>0.82</b> (0.4)	15/15
SNES	2.8(2)	1.8(2)	9.0(10)	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	<b>2.5</b> (2)	<b>1.0</b> (0.7)	1.4(2)	2.7(3)	4.0(5)	4.1(4)	15/15
xNESas	2.8(3)	8.0(13)	5.6(7)	5.3(6)	5.2(6)	7.2(8)	15/15

Table 14: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{113}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f113</b>	26	126	1948	3236	3236	3428	12/15
IPOPsaACM	4.2(6)	4.4(7)	0.75(1)	<b>0.70</b> (0.9)	<b>0.70</b> (0.9)	<b>0.74</b> (0.8)	15/15
SNES	2.6(3)	<b>2.7</b> (3)	<b>0.69</b> (1)	0.92(0.9)	0.92(0.9)	1.1(1)	15/15
xNES	<b>1.5</b> (0.9)	5.4(13)	1.5(3)	1.5(2)	1.5(2)	1.5(2)	15/15
xNESas	8.8(8)	25(28)	4.8(6)	3.4(4)	3.4(4)	3.6(3)	15/15

Table 15: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f114</b>	26	1015	6279	28324	28324	32580	15/15
IPOPsaACM	<b>10</b> (15)	<b>1.3</b> (2)	<b>0.96</b> (0.9)	<b>0.40</b> (0.3) <sup>*2</sup>	<b>0.40</b> (0.3) <sup>*2</sup>	<b>0.41</b> (0.3) <sup>*2</sup>	15/15
SNES	12(15)	1.4(2)	2.8(3)	16(16)	16(15)	$\infty$ 3e4	0/15
xNES	30(89)	4.7(6)	6.3(8)	13(14)	13(14)	21(24)	3/15
xNESas	146(189)	11(17)	9.5(11)	24(20)	24(20)	45(49)	2/15



Table 16: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{115}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f115</b>	12	118	593	890	890	1246	15/15
IPOPsaACM	<b>2.8</b> (2)	<b>1.1</b> (0.5)	<b>1.2</b> (1.0)	<b>1.5</b> (2)	<b>1.5</b> (2)	<b>1.5</b> (2)	15/15
SNES	3.8(3)	1.9(2)	1.6(1)	10(17)	10(17)	11(14)	9/15
xNES	6.5(4)	6.9(13)	4.8(10)	4.6(9)	4.6(9)	3.4(7)	15/15
xNESas	4.9(5)	4.3(0.6)	3.8(5)	2.7(4)	2.7(4)	4.1(8)	15/15

Table 17: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{116}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f116</b>	169	2642	4419	7143	9614	11370	15/15
IPOPsaACM	3.9(7)	<b>0.77</b> (0.9)	<b>0.60</b> (0.6)	<b>0.50</b> (0.3)	<b>0.41</b> (0.3)	<b>0.37</b> (0.2)	15/15
SNES	<b>3.8</b> (4)	1.2(1)	3.8(4)	30(32)	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	9.5(15)	1.3(3)	1.1(2)	0.74(1)	0.60(0.9)	0.80(0.9)	15/15
xNESas	24(63)	4.7(7)	3.1(4)	1.9(2)	1.7(2)	1.5(2)	15/15

Table 18: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{117}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f117</b>	2392	14361	39508	61720	73678	80041	15/15
IPOPsaACM	2.5(3)	<b>1.3</b> (1)	<b>0.71</b> (0.4)	<b>0.54</b> (0.2)	<b>0.57</b> (0.2)	<b>0.60</b> (0.2)	15/15
SNES	<b>1.5</b> (2)	1.8(2)	11(13)	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	3.9(7)	2.3(3)	3.1(4)	57(59)	$\infty$	$\infty$ <i>2e5</i>	0/15
xNESas	3.6(5)	5.1(7)	6.9(7)	$\infty$	$\infty$	$\infty$ <i>4e5</i>	0/15

Table 19: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f118</b>	109	205	712	1008	1283	1593	15/15
IPOPsaACM	<b>1.1</b> (0.4)	<b>0.75</b> (0.3)*	<b>0.35</b> (0.1) $\downarrow_3$	<b>0.52</b> (0.2) $\downarrow_3$	<b>0.70</b> (0.4) $\downarrow$	<b>0.76</b> (0.3)	15/15
SNES	3.9(4)	15(16)	20(16)	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	1.5(1)	2.0(1)	0.79(0.6)	1.3(2)	1.6(2)	1.5(2)	15/15
xNESas	1.6(0.6)	1.3(0.8)	0.53(0.2) $\downarrow_2$	0.60(0.2) $\downarrow_2$	1.1(0.2)	1.1(0.2)	15/15

Table 20: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{119}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f119</b>	2.2	66	421	2005	12038	15719	15/15
IPOPsaACM	<b>2.8</b> (3)	<b>1.3</b> (2)	<b>0.45</b> (0.3)	<b>0.65</b> (0.5)	<b>0.55</b> (0.4)	<b>0.84</b> (0.7)	15/15
SNES	12(20)	2.6(3)	0.68(0.5)	0.67(0.6)	11(12)	<i><math>\infty</math></i> <i>3e4</i>	0/15
xNES	9.0(14)	18(58)	3.5(9)	2.0(2)	0.65(1)	1.1(1.0)	15/15
xNESas	8.2(9)	7.4(4)	2.6(7)	2.6(3)	1.1(1)	1.3(2)	15/15

Table 21: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f120</b>	2.2	81	1802	31935	1.2e5	2.7e5	15/15
IPOPsaACM	<b>20</b> (50)	9.0(18)	1.6(2)	<b>0.57</b> (0.2)*4	<b>0.40</b> (0.2)↓2	<b>0.51</b> (0.3)	15/15
SNES	23(67)	<b>6.9</b> (10)	<b>1.2</b> (2)	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	414(1025)	55(83)	12(14)	50(51)	$\infty$	$\infty$ <i>2e5</i>	0/15
xNESas	29(40)	57(53)	13(18)	105(106)	$\infty$	$\infty$ <i>5e5</i>	0/15

Table 22: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f121</b>	2.2	41	116	699	2297	3321	15/15
IPOPsaACM	3.6(5)	<b>1.0</b> (1.0)	1.5(0.6)	1.1(1)	0.96(0.3)	1.1(0.8)	15/15
SNES	<b>2.9</b> (4)	1.4(1)	1.1(0.4)	<b>2.7</b> (3)	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	7.7(11)	1.4(1.0)	<b>1.0</b> (0.5)	0.89(0.6)	<b>0.65</b> (0.4)	<b>0.86</b> (0.6)	15/15
xNESas	4.8(7)	1.7(3)	1.3(1)	<b>0.83</b> (0.3)	0.82(0.5)	1.0(1.0)	15/15

Table 23: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{122}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f122</b>	5.8	357	1802	7595	12242	19009	15/15
IPOPsaACM	3.1(2)	1.4(2)	1.3(2)	<b>0.90</b> (0.5)	<b>1.1</b> (1) <sup>*2</sup>	<b>1.1</b> (0.7) <sup>*3</sup>	15/15
SNES	6.3(7)	<b>0.86</b> (1)	<b>0.63</b> (0.6)	9.3(11)	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	<b>2.3</b> (2)	1.8(4)	3.9(5)	3.9(5)	17(19)	$\infty$ <i>3e5</i>	0/15
xNESas	4.9(6)	13(24)	11(20)	8.0(8)	52(55)	$\infty$ <i>5e5</i>	0/15



Table 24: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{123}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f123</b>	4.9	1546	21830	93159	1.9e5	4.4e5	15/15
IPOPsaACM	23(21)	1.9(2)	<b>0.80</b> (0.6) <sup>*3</sup>	<b>0.69</b> (0.2)	<b>0.78</b> (0.4)	<b>0.99</b> (0.7)	15/15
SNES	5.4(8)	<b>0.96</b> (0.8)	$\infty$	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	<b>5.1</b> (6)	4.9(6)	70(82)	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
xNESas	24(66)	11(11)	38(44)	$\infty$	$\infty$	$\infty$ <i>5e5</i>	0/15

Table 25: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{124}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f124</b>	3.6	196	926	7091	12902	14882	14/15
IPOP <sub>sa</sub> ACM	<b>2.2</b> (3)	0.71(0.6)	0.90(1)	<b>0.69</b> (0.5)	<b>1.1</b> (0.5) <sup>*3</sup>	<b>1.3</b> (0.6) <sup>*3</sup>	15/15
SNES	5.6(7)	<b>0.65</b> (0.7)	<b>0.59</b> (0.7)	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	5.6(5)	2.1(0.5)	<b>0.70</b> (0.3)	1.7(2)	6.5(6)	105(115)	0/15

Table 26: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f125</b>	1	1	1	24677	36351	38000	15/15
IPOPsaACM	<b>1</b> (0)	10(16)	343(650)	<b>0.91</b> (0.8)	<b>0.94</b> (0.8)	<b>1.0</b> (0.7)	15/15
SNES	1.1(0.5)	14(27)	260(286)	8.2(10)	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	1.1(0.5)	<b>9.3</b> (14)	189(266)	3.2(3)	8.4(10)	20(22)	3/15
xNESas	1.1(0.5)	15(10)	<b>131</b> (95)	5.5(6)	15(13)	29(30)	3/15

Table 27: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f126</b>	1	1	1	1.1e5	6.3e5	9.6e5	15/15
IPOPsaACM	<b>1</b> (0)	12(24)	737(972)	<b>0.85</b> (1)	<b>0.84</b> (1)	<b>0.90</b> (1)	15/15
SNES	1.2(0.5)	39(48)	<b>399</b> (496)	$\infty$	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	1.3(0.5)	<b>7.3</b> (10)	1716(3734)	14(16)	$\infty$	$\infty$ <i>2e5</i>	0/15
xNESas	1.3(0.5)	62(138)	2313(3108)	6.5(7)	$\infty$	$\infty$ <i>4e5</i>	0/15

Table 28: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f127</b>	1	1	1	39085	45347	45996	8/15
IPOPsaACM	<b>1</b> (0)	10(9)	144(99)	<b>0.48</b> (0.6)	<b>0.77</b> (0.9)	<b>0.95</b> (1)	15/15
SNES	1.6(0)	11(12)	<b>112</b> (106)	1.9(2)	$\infty$	$\infty$ <i>3e4</i>	0/15
xNES	1.2(0.5)	<b>6.2</b> (6)	139(74)	1.6(2)	12(14)	22(24)	2/15
xNESas	1.3(0.5)	12(12)	244(376)	1.9(2)	5.6(7)	13(13)	8/15

Table 29: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{128}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f128</b>	5.5	426	1125	1917	2715	4340	15/15
IPOPsaACM	2.6(3)	4.6(6)	18(32)	19(31)	198(553)	124(346)	13/15
SNES	2.6(3)	<b>2.7</b> (3)	<b>2.2</b> (3)	<b>1.3</b> (1)	<b>1.00</b> (1)	<b>0.68</b> (0.7)	15/15
xNES	42(16)	11(21)	9.1(10)	5.4(6)	3.8(4)	2.4(3)	15/15
xNESas	<b>1.5</b> (2)	30(21)	20(47)	12(27)	8.6(19)	5.4(12)	15/15

Table 30: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{129}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f129</b>	4.8	362	3392	11584	28362	38534	15/15
IPOPsaACM	3.2(2)	10(6)	2.7(5)	4.6(3)	10(6)	<b>7.4(5)</b>	14/15
SNES	<b>1.8(2)</b>	<b>3.7(4)</b>	<b>0.69(0.7)</b>	<b>3.0(3)</b>	<b>4.7(5)</b>	11(12)	1/15
xNES	3.0(3)	6.5(9)	5.6(8)	6.3(7)	16(19)	21(20)	2/15
xNESas	3.5(7)	23(42)	6.5(9)	13(18)	27(32)	167(187)	0/15

Table 31: 03-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f130</b>	5.5	245	515	1502	11944	14346	12/15
IPOPsaACM	2.2(2)	12(20)	15(18)	27(8)	13(3)	16(5)	14/15
SNES	3.1(4)	<b>3.7(5)</b>	<b>2.6(2)</b>	<b>0.98(0.7)</b>	<b>0.17(0.1)</b> ↓	<b>0.34(0.4)</b>	12/15
xNES	2.2(2)	46(70)	42(58)	15(20)	2.0(3)	1.9(2)	15/15
xNESas	<b>1.5(0.8)</b>	11(22)	48(98)	17(33)	2.2(4)	2.0(4)	15/15



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