

# Comparison tables: BBOB 2012 noisy testbed in 2-D

The BBOBies

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## Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2012, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2012>. 4 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [4, 2]. The experimental set-up is described in [3].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [1]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [3] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values. Table 1 gives an overview on all algorithms submitted to the noise-free testbed in 2012.

Table 1: Names and references of all algorithms submitted for the noise-free testbed

algorithm name	short	paper	reference
IPOPsaACM		Black-box Optimization Benchmarking of IPOP-saACM-ES on the BBOB-2012 Noisy Testbed (Page 261)	[8]
SNES		Benchmarking Separable Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 205)	[7]
xNES		Benchmarking Exponential Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 213)	[5]
xNESas		Benchmarking Natural Evolution Strategies with Adaptation Sampling on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 229)	[6]
SNES, xNES, xNESas		Comparing Natural Evolution Strategies to BIPOP-CMA-ES on Noiseless and Noisy Black-Box Optimization Testbeds (Page 237)	[9]

Table 2: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f101</b>	1.8	8.0	10	14	20	23	15/15
IPOPsaACM	<b>3.4</b> (4)	<b>1.8</b> (2)	4.1(1)	<b>4.0</b> (1)*	<b>3.9</b> (0.6)* <sup>4</sup>	<b>4.1</b> (0.6)* <sup>4</sup>	15/15
SNES	4.4(4)	2.0(2)	<b>3.2</b> (2)	7.2(3)	11(2)	14(2)	15/15
xNES	8.4(7)	5.1(3)	6.8(3)	9.3(4)	12(3)	13(3)	15/15
xNESas	6.7(7)	3.4(2)	5.4(3)	8.0(4)	10(2)	12(2)	15/15

Table 3: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f102</b>	1.8	7.1	11	19	25	31	15/15
IPOPsaACM	<b>3.1</b> (3)	<b>2.8</b> (2)	<b>3.1</b> (2)	<b>3.2</b> (0.8) <sup>*2</sup>	<b>3.3</b> (0.6) <sup>*3</sup>	<b>3.1</b> (0.6) <sup>*4</sup>	15/15
SNES	6.6(8)	3.8(2)	4.3(2)	7.0(1)	8.6(1)	10(1)	15/15
xNES	5.1(6)	3.4(4)	4.4(5)	6.4(2)	8.0(3)	8.8(2)	15/15
xNESas	7.0(7)	42(4)	29(3)	20(7)	29(80)	26(65)	15/15

Table 4: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f103</b>	1.8	7.9	9.4	9.4	10	14	15/15
IPOPsaACM	4.4 <sup>(4)</sup>	2.9 <sup>(3)</sup>	<b>3.8</b> <sup>(2)</sup>	<b>6.6</b> <sup>(1)*2</sup>	<b>8.9</b> <sup>(3)*3</sup>	<b>8.7</b> <sup>(2)*4</sup>	15/15
SNES	4.3 <sup>(5)</sup>	<b>2.6</b> <sup>(1)</sup>	4.2 <sup>(2)</sup>	14 <sup>(5)</sup>	35 <sup>(23)</sup>	71 <sup>(58)</sup>	15/15
xNES	<b>4.2</b> <sup>(4)</sup>	3.1 <sup>(2)</sup>	5.2 <sup>(3)</sup>	14 <sup>(4)</sup>	25 <sup>(10)</sup>	25 <sup>(5)</sup>	15/15
xNESas	4.3 <sup>(5)</sup>	4.4 <sup>(5)</sup>	7.2 <sup>(4)</sup>	14 <sup>(5)</sup>	27 <sup>(19)</sup>	28 <sup>(15)</sup>	15/15

Table 5: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{104}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f104</b>	5.4	15	194	248	256	263	15/15
IPOPsaACM	4.4(3)	<b>4.9</b> (4)	<b>1.5</b> (0.8)	<b>1.5</b> (0.6)	<b>1.5</b> (0.6)	<b>1.5</b> (0.6)*	15/15
SNES	12(7)	9.2(12)	3.7(4)	125(158)	$\infty$	$\infty$ 2e4	0/15
xNES	4.7(6)	18(6)	5.7(7)	5.5(6)	7.5(16)	7.6(15)	15/15
xNESas	<b>3.4</b> (3)	32(5)	4.9(12)	4.9(10)	6.2(10)	6.3(10)	15/15

Table 6: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{105}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f105</b>	5.4	15	357	381	397	410	15/15
IPOPsaACM	4.5(4)	11(4)	<b>0.90</b> (1)	<b>1.4</b> (2)	<b>1.4</b> (2)	<b>1.5</b> (2)	15/15
SNES	<b>4.3</b> (5)	<b>6.4</b> (8)	3.0(5)	52(53)	348(405)	<i><math>\infty</math> 2e4</i>	0/15
xNES	5.8(5)	37(8)	4.3(7)	5.7(10)	5.7(9)	5.7(9)	15/15
xNESas	54(6)	69(137)	7.2(12)	9.2(16)	11(16)	11(15)	15/15

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Table 7: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{106}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f106</b>	5.4	15	139	352	490	650	15/15
IPOPsaACM	<b>2.7</b> (2)	<b>4.2</b> (4)	<b>1.1</b> (0.7)	<b>0.72</b> (0.5)	<b>0.63</b> (0.4)	<b>0.58</b> (0.4)*	15/15
SNES	5.3(5)	4.5(4)	8.0(11)	48(46)	296(328)	$\infty$ 2e4	0/15
xNES	5.6(6)	5.8(5)	2.3(3)	3.0(3)	3.2(5)	2.8(4)	15/15
xNESas	5.1(5)	11(11)	6.1(5)	4.5(4)	3.6(3)	2.9(2)	15/15



Table 8: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{107}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f107</b>	1.8	13	28	158	255	421	15/15
IPOPsaACM	<b>5.2</b> (6)	<b>1.8</b> (2)	<b>2.1</b> (2)	1.2(0.7)	1.4(0.6)	1.1(0.4)	15/15
SNES	15(21)	3.9(4)	2.7(3)	<b>1.1</b> (0.6)	<b>1.3</b> (0.4)	<b>1.0</b> (0.2)	15/15
xNES	27(19)	33(114)	18(55)	5.2(10)	3.6(6)	2.9(4)	13/15
xNESas	154(9)	90(171)	44(81)	10(15)	7.7(9)	5.6(6)	15/15

Table 9: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f108</b>	1.8	30	202	3422	7369	15979	15/15
IPOPsaACM	<b>15</b> <sup>(14)</sup>	<b>10</b> <sup>(13)</sup>	4.8 <sup>(7)</sup>	<b>1.0</b> <sup>(0.6)</sup>	<b>1.2</b> <sup>(1)</sup> * <sup>3</sup>	<b>0.88</b> <sup>(0.5)</sup> * <sup>3</sup>	15/15
SNES	53 <sup>(74)</sup>	10 <sup>(15)</sup>	<b>2.8</b> <sup>(3)</sup>	2.5 <sup>(2)</sup>	$\infty$	$\infty$ 2e4	0/15
xNES	170 <sup>(558)</sup>	49 <sup>(66)</sup>	11 <sup>(13)</sup>	10 <sup>(13)</sup>	287 <sup>(327)</sup>	$\infty$ 1e5	0/15
xNESas	502 <sup>(1112)</sup>	100 <sup>(123)</sup>	31 <sup>(31)</sup>	34 <sup>(30)</sup>	406 <sup>(434)</sup>	$\infty$ 2e5	0/15

Table 10: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{109}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f109</b>	1.8	10	13	68	96	96	15/15
IPOPsaACM	4.3(6)	<b>2.2</b> (2)	4.3(4)	<b>2.3</b> (2)	<b>3.3</b> (2)	<b>5.5</b> (3)	15/15
SNES	<b>3.9</b> (2)	2.4(1)	<b>3.6</b> (2)	2.6(1)	11(10)	336(417)	1/15
xNES	5.8(5)	3.6(4)	5.5(4)	5.8(3)	5.3(3)	8.7(12)	15/15
xNESas	5.4(6)	5.7(12)	11(10)	5.7(4)	9.1(17)	11(22)	15/15

Table 11: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{110}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f110</b>	7.1	34	623	2319	8407	9154	14/15
IPOPsaACM	<b>4.1</b> (3)	5.8(2)	2.6(2)	<b>2.9</b> (3)	<b>1.1</b> (0.9)	<b>1.0</b> (0.8)	15/15
SNES	5.9(7)	<b>2.9</b> (4)	<b>1.2</b> (1)	8.4(9)	34(38)	$\infty$ <i>2e4</i>	0/15
xNES	11(7)	26(30)	4.2(7)	4.2(4)	1.4(1)	1.3(1)	14/15
xNESas	7.1(8)	53(118)	8.8(10)	5.4(6)	2.2(2)	2.3(3)	15/15

Table 12: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{111}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f111</b>	24	119	718	12718	61860	1.7e5	15/15
IPOPsaACM	5.9(3)	3.6(7)	4.1(3)	7.9(11)	<b>2.7</b> (3)	<b>1.0</b> (1)	15/15
SNES	<b>4.7</b> (5)	<b>2.9</b> (3)	<b>1.9</b> (2)	<b>4.9</b> (6)	$\infty$	$\infty$ <i>2e4</i>	0/15
xNES	29(83)	13(21)	12(12)	7.0(7)	$\infty$	$\infty$ <i>2e5</i>	0/15
xNESas	50(90)	23(41)	17(21)	10(12)	$\infty$	$\infty$ <i>2e5</i>	0/15

Table 13: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{112}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f112</b>	5.4	15	625	1154	1373	1531	15/15
IPOPsaACM	4.8(6)	4.9(3)	<b>0.51</b> (0.6)	<b>0.73</b> (0.5)	<b>0.97</b> (0.7)	<b>1.1</b> (0.6)	15/15
SNES	4.7(4)	<b>4.1</b> (2)	2.1(2)	42(45)	$\infty$	$\infty$ <i>2e4</i>	0/15
xNES	<b>3.1</b> (3)	12(10)	2.5(4)	3.6(4)	4.3(4)	4.2(4)	15/15
xNESas	4.1(4)	23(14)	2.7(5)	4.1(4)	6.0(6)	5.5(5)	15/15

Table 14: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{113}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f113</b>	4.7	31	87	174	174	876	15/15
IPOPsaACM	<b>4.3</b> (5)	<b>3.0</b> (5)	11(20)	9.4(11)	9.4(11)	<b>2.0</b> (2)	15/15
SNES	8.8(11)	3.5(5)	<b>5.9</b> (8)	<b>6.5</b> (8)	<b>6.5</b> (8)	3.3(4)	14/15
xNES	7.6(9)	20(32)	14(29)	18(26)	18(26)	3.6(5)	15/15
xNESas	6.1(5)	25(75)	26(31)	30(57)	30(57)	6.0(11)	15/15

Table 15: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f114</b>	8.9	43	698	5343	5343	8680	15/15
IPOPsaACM	18 <sub>(20)</sub>	9.5 <sub>(13)</sub>	3.2 <sub>(3)</sub>	<b>1.3</b> <sub>(1)</sub>	<b>1.3</b> <sub>(1)</sub>	<b>1.1</b> <sub>(0.6)</sub>	15/15
SNES	<b>5.7</b> <sub>(5)</sub>	<b>5.0</b> <sub>(5)</sub>	<b>1.3</b> <sub>(1.0)</sub>	2.4 <sub>(3)</sub>	2.4 <sub>(3)</sub>	4.6 <sub>(5)</sub>	0/15
xNES	37 <sub>(114)</sub>	33 <sub>(50)</sub>	11 <sub>(12)</sub>	5.7 <sub>(6)</sub>	5.7 <sub>(6)</sub>	8.9 <sub>(7)</sub>	5/15
xNESas	141 <sub>(229)</sub>	162 <sub>(261)</sub>	21 <sub>(34)</sub>	17 <sub>(20)</sub>	17 <sub>(20)</sub>	20 <sub>(23)</sub>	5/15



Table 16: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{115}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f115</b>	3.2	13	225	394	394	543	15/15
IPOPsaACM	<b>5.2</b> (4)	<b>4.4</b> (4)	2.0(3)	<b>2.0</b> (2)	<b>2.0</b> (2)	<b>1.8</b> (2)	15/15
SNES	5.2(5)	6.4(2)	<b>1.3</b> (2)	2.4(4)	2.4(4)	7.6(14)	11/15
xNES	6.4(7)	24(74)	6.3(9)	5.3(6)	5.3(6)	4.7(5)	15/15
xNESas	5.2(4)	24(5)	3.8(9)	6.2(13)	6.2(13)	4.9(11)	15/15

Table 17: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{116}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f116</b>	49	101	155	275	1041	1788	15/15
IPOPsaACM	14 <sup>(19)</sup>	18 <sup>(20)</sup>	13 <sup>(13)</sup>	7.8 <sup>(8)</sup>	2.3 <sup>(2)</sup>	1.5 <sup>(1)</sup>	15/15
SNES	2.7 <sup>(4)</sup>	12 <sup>(10)</sup>	20 <sup>(16)</sup>	229 <sup>(264)</sup>	$\infty$	$\infty$ <i>2e4</i>	0/15
xNES	15 <sup>(51)</sup>	<b>8.4</b> <sup>(25)</sup>	<b>9.1</b> <sup>(17)</sup>	<b>5.6</b> <sup>(9)</sup>	<b>1.6</b> <sup>(2)</sup>	<b>0.98</b> <sup>(1)</sup>	15/15
xNESas	<b>2.0</b> <sup>(2)</sup>	26 <sup>(43)</sup>	21 <sup>(29)</sup>	14 <sup>(16)</sup>	3.8 <sup>(4)</sup>	3.0 <sup>(6)</sup>	15/15

Table 18: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{117}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f117</b>	167	1346	6454	28223	36420	43231	15/15
IPOPsaACM	3.7(7)	3.4(6)	2.0(2)	<b>0.73</b> (0.6)	<b>0.70</b> (0.4)	<b>0.73</b> (0.3)	15/15
SNES	<b>2.2</b> (5)	<b>1.1</b> (2)	<b>1.0</b> (1)	$\infty$	$\infty$	$\infty$ <i>2e4</i>	0/15
xNES	5.0(6)	3.0(5)	2.8(4)	6.6(7)	62(62)	$\infty$ <i>2e5</i>	0/15
xNESas	23(26)	9.4(9)	3.4(4)	5.4(6)	80(88)	$\infty$ <i>2e5</i>	0/15

Table 19: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f118</b>	21	103	132	584	776	972	15/15
IPOPsaACM	3.7(2)	<b>1.4</b> (1)	<b>1.4</b> (1)	<b>0.58</b> (0.4)	<b>0.64</b> (0.4)	<b>0.77</b> (0.5)	15/15
SNES	7.3(10)	12(12)	27(33)	51(59)	$\infty$	$\infty$ <i>2e4</i>	0/15
xNES	<b>3.6</b> (3)	1.8(1)	2.6(3)	1.5(2)	1.9(2)	2.1(2)	15/15
xNESas	15(3)	4.4(5)	5.4(15)	1.5(4)	1.6(3)	2.3(4)	15/15

Table 20: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{119}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f119</b>	1.4	11	71	1040	4767	10082	15/15
IPOPsaACM	<b>2.4</b> (2)	8.6(16)	1.9(2)	0.47(0.6)	<b>0.99</b> (0.7)	<b>0.82</b> (0.2)	15/15
SNES	5.2(4)	<b>5.2</b> (6)	<b>1.5</b> (1)	<b>0.44</b> (0.2) <sub>↓3</sub>	4.4(5)	30(33)	1/15
xNES	5.3(8)	65(7)	10(1)	2.4(5)	1.6(1)	1.1(1)	14/15
xNESas	10(11)	61(218)	13(33)	2.9(4)	2.2(3)	1.8(2)	15/15

Table 21: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f120</b>	1.4	11	374	5724	75406	1.9e5	15/15
IPOPsaACM	5.1(7)	<b>10</b> (12)	2.0(2)	<b>2.0</b> (2) <sup>*</sup>	<b>0.46</b> (0.4) <sub>↓</sub>	<b>0.51</b> (0.4) <sub>↓</sub>	15/15
SNES	<b>4.8</b> (9)	11(15)	<b>0.98</b> (1.0)	50(56)	$\infty$	$\infty$ <i>2e4</i>	0/15
xNES	107(33)	193(307)	12(20)	11(7)	$\infty$	$\infty$ <i>1e5</i>	0/15
xNESas	8.8(6)	160(375)	13(18)	23(24)	$\infty$	$\infty$ <i>2e5</i>	0/15

Table 22: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f121</b>	1.4	7.1	42	327	1120	1702	15/15
IPOPsaACM	<b>2.5</b> (4)	<b>2.1</b> (2)	1.2(0.7)	<b>1.2</b> (0.7)	<b>1.0</b> (0.4)	<b>1.2</b> (0.4)	15/15
SNES	3.5(6)	4.7(5)	1.4(0.8)	1.9(2)	255(286)	$\infty$ <i>2e4</i>	0/15
xNES	4.4(5)	4.4(4)	1.7(1)	1.3(0.9)	1.2(1.0)	1.7(2)	15/15
xNESas	3.0(5)	2.6(2)	<b>1.1</b> (0.7)	1.7(0.8)	1.6(3)	2.3(4)	15/15

Table 23: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{122}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f122</b>	2.9	95	523	2244	4351	9561	15/15
IPOPsaACM	<b>3.9</b> (5)	<b>1.1</b> (0.7)	1.3(1)	<b>1.2</b> (1)	<b>1.2</b> (0.7)	<b>0.79</b> (0.4) <sup>*3</sup>	15/15
SNES	18(13)	2.2(3)	<b>0.94</b> (1)	3.2(4)	65(75)	$\infty$ 2e4	0/15
xNES	116(343)	17(32)	4.9(7)	7.0(9)	13(13)	35(38)	4/15
xNESas	106(28)	28(32)	14(19)	12(14)	19(15)	53(52)	3/15



Table 24: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{123}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f123</b>	3.1	211	6371	38734	1.0e5	2.2e5	15/15
IPOPsaACM	40 <sub>(34)</sub>	3.7 <sub>(5)</sub>	<b>0.90</b> <sub>(0.7)</sub>	<b>0.95</b> <sub>(0.4)</sub>	<b>0.68</b> <sub>(0.5)</sub>	<b>0.82</b> <sub>(0.5)</sub>	15/15
SNES	<b>8.0</b> <sub>(18)</sub>	<b>2.8</b> <sub>(4)</sub>	2.2 <sub>(2)</sub>	$\infty$	$\infty$	$\infty$ <i>2e4</i>	0/15
xNES	68 <sub>(10)</sub>	20 <sub>(19)</sub>	8.3 <sub>(9)</sub>	$\infty$	$\infty$	$\infty$ <i>1e5</i>	0/15
xNESas	172 <sub>(527)</sub>	47 <sub>(55)</sub>	12 <sub>(16)</sub>	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15

Table 25: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{124}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f124</b>	3.5	64	316	1991	5595	9019	15/15
IPOPsaACM	<b>2.3</b> (2)	3.4(1)	1.4(2)	<b>0.84</b> (0.7)	<b>1.1</b> (0.8)*4	<b>2.4</b> (1)	15/15
SNES	4.0(3)	<b>1.9</b> (3)	<b>0.91</b> (0.9)	71(72)	$\infty$	$\infty$ 2e4	0/15
xNES	4.0(5)	6.3(17)	2.7(5)	4.6(5)	23(22)	41(46)	5/15

Table 26: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{125}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f125</b>	1	1	1	1150	3854	7556	15/15
IPOPsaACM	1.1(0)	<b>4.1</b> (4)	37(34)	1.9(3)	<b>1.4</b> (1)	<b>1.6</b> (2)	15/15
SNES	<b>1</b> (0)	6.3(9)	40(49)	<b>0.82</b> (1)	2.7(2)	12(13)	1/15
xNES	1.1(0)	6.8(9)	60(48)	4.6(5)	5.1(6)	3.1(3)	14/15
xNESas	1.3(1)	6.1(4)	<b>30</b> (32)	7.2(7)	7.1(8)	8.4(10)	14/15

Table 27: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best}}$  2009 on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f126</b>	1	1	1	3417	11056	36387	15/15
IPOPsaACM	<b>1</b> (0)	9.2(10)	70(89)	<b>1.3</b> (1)	<b>1.3</b> (1)	<b>1.4</b> (1)	15/15
SNES	<b>1</b> (0)	5.5(8)	<b>66</b> (79)	1.5(2)	8.2(9)	$\infty$ 2e4	0/15
xNES	1.1(0)	6.1(6)	667(1505)	4.4(4)	7.3(8)	60(67)	0/15
xNESas	1.1(0)	<b>3.3</b> (2)	980(2133)	10(13)	12(5)	25(25)	1/15

Table 28: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f127</b>	1	1	1	1185	6771	7277	13/15
IPOPsaACM	1.3(0)	5.5(6)	75(59)	2.5(2)	<b>0.94</b> (1)	<b>1.1</b> (1)	15/15
SNES	<b>1.1</b> (0.5)	4.9(5)	<b>37</b> (31)	<b>1.6</b> (1)	1.7(2)	19(21)	0/15
xNES	1.8(0.5)	5.7(6)	167(87)	7.4(10)	2.6(3)	5.0(6)	15/15
xNESas	1.3(0)	<b>4.3</b> (6)	67(77)	8.9(14)	3.5(4)	5.5(6)	15/15

Table 29: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best}} 2009$  on  $f_{128}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f128</b>	1.8	41	134	387	593	620	15/15
IPOPsaACM	1.5(1)	8.1(8)	22(23)	19(28)	83(23)	91(23)	15/15
SNES	1.6(1)	<b>5.1</b> (6)	<b>2.0</b> (3)	<b>1.2</b> (1)	<b>0.93</b> (0.8)	<b>1.3</b> (2)	15/15
xNES	1.4(0.8)	46(72)	22(23)	10(13)	6.9(8)	6.6(8)	15/15
xNESas	<b>1.2</b> (1)	32(61)	65(99)	32(39)	23(26)	22(25)	15/15

Table 30: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{129}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f129</b>	1.8	65	220	1902	5944	10661	15/15
IPOPsaACM	1.4(2)	<b>3.3</b> (4)	11(9)	2.7(3)	<b>1.6</b> (1)	<b>1.2</b> (1)*	15/15
SNES	1.4(1)	3.5(4)	<b>3.0</b> (4)	<b>1.6</b> (2)	1.9(2)	13(14)	0/15
xNES	<b>0.85</b> (0.6)	25(32)	19(23)	5.0(6)	5.5(6)	11(10)	9/15
xNESas	1.1(0.8)	25(67)	35(36)	14(13)	18(13)	25(22)	6/15

Table 31: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

$\Delta f_{\text{opt}}$	1e1	1e0	1e-1	1e-3	1e-5	1e-7	#succ
<b>f130</b>	1.5	45	198	797	1772	4442	15/15
IPOPsaACM	1.7(1)	4.8(5)	8.2(15)	6.8(4)	12(13)	26(49)	15/15
SNES	1.4(1.0)	<b>3.6</b> (4)	<b>2.6</b> (4)	<b>1.0</b> (1)	<b>0.62</b> (0.7)	<b>0.50</b> (0.4)	15/15
xNES	<b>1.3</b> (1)	20(24)	16(32)	4.2(8)	1.9(4)	0.81(1)	15/15
xNESas	1.7(2)	57(89)	35(54)	8.9(13)	4.9(7)	2.0(3)	15/15



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