

# Comparison tables: BBOB 2012 noisy testbed in 2-D

The BBOBies

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## Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2012, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2012>. 4 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [4, 2]. The experimental set-up is described in [3].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [1]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [3] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values. Table 1 gives an overview on all algorithms submitted to the noise-free testbed in 2012.

Table 1: Names and references of all algorithms submitted for the noise-free testbed

| algorithm name     | short | paper  | reference |
|--------------------|-------|--|-----------|
| IPOPsaACM          |       | Black-box Optimization Benchmarking of IPOP-saACM-ES on the BBOB-2012 Noisy Testbed (Page 261)   | [8]       |
| SNES               |       | Benchmarking Separable Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 205)                | [7]       |
| xNES               |       | Benchmarking Exponential Natural Evolution Strategies on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 213)              | [5]       |
| xNESas             |       | Benchmarking Natural Evolution Strategies with Adaptation Sampling on the Noiseless and Noisy Black-Box Optimization Testbeds (Page 229) | [6]       |
| SNES, xNES, xNESas |       | Comparing Natural Evolution Strategies to BIPOP-CMA-ES on Noiseless and Noisy Black-Box Optimization Testbeds (Page 237)                 | [9]       |

Table 2: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3            | 1e-5                           | 1e-7                           | #succ |
|-------------------------|----------------|----------------|----------------|-----------------|--------------------------------|--------------------------------|-------|
| <b>f101</b>             | 1.8            | 8.0            | 10             | 14              | 20                             | 23                             | 15/15 |
| IPOPsaACM               | <b>3.4</b> (4) | <b>1.8</b> (2) | 4.1(1)         | <b>4.0</b> (1)* | <b>3.9</b> (0.6)* <sup>4</sup> | <b>4.1</b> (0.6)* <sup>4</sup> | 15/15 |
| SNES                    | 4.4(4)         | 2.0(2)         | <b>3.2</b> (2) | 7.2(3)          | 11(2)                          | 14(2)                          | 15/15 |
| xNES                    | 8.4(7)         | 5.1(3)         | 6.8(3)         | 9.3(4)          | 12(3)                          | 13(3)                          | 15/15 |
| xNESas                  | 6.7(7)         | 3.4(2)         | 5.4(3)         | 8.0(4)          | 10(2)                          | 12(2)                          | 15/15 |

Table 3: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3                           | 1e-5                           | 1e-7                           | #succ |
|-------------------------|----------------|----------------|----------------|--------------------------------|--------------------------------|--------------------------------|-------|
| <b>f102</b>             | 1.8            | 7.1            | 11             | 19                             | 25                             | 31                             | 15/15 |
| IPOPsSaACM              | <b>3.1</b> (3) | <b>2.8</b> (2) | <b>3.1</b> (2) | <b>3.2</b> (0.8) <sup>*2</sup> | <b>3.3</b> (0.6) <sup>*3</sup> | <b>3.1</b> (0.6) <sup>*4</sup> | 15/15 |
| SNES                    | 6.6(8)         | 3.8(2)         | 4.3(2)         | 7.0(1)                         | 8.6(1)                         | 10(1)                          | 15/15 |
| xNES                    | 5.1(6)         | 3.4(4)         | 4.4(5)         | 6.4(2)                         | 8.0(3)                         | 8.8(2)                         | 15/15 |
| xNESas                  | 7.0(7)         | 42(4)          | 29(3)          | 20(7)                          | 29(80)                         | 26(65)                         | 15/15 |

Table 4: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3                         | 1e-5                         | 1e-7                         | #succ |
|-------------------------|----------------|----------------|----------------|------------------------------|------------------------------|------------------------------|-------|
| <b>f103</b>             | 1.8            | 7.9            | 9.4            | 9.4                          | 10                           | 14                           | 15/15 |
| IPOPsaACM               | 4.4(4)         | 2.9(3)         | <b>3.8</b> (2) | <b>6.6</b> (1) <sup>*2</sup> | <b>8.9</b> (3) <sup>*3</sup> | <b>8.7</b> (2) <sup>*4</sup> | 15/15 |
| SNES                    | 4.3(5)         | <b>2.6</b> (1) | 4.2(2)         | 14(5)                        | 35(23)                       | 71(58)                       | 15/15 |
| xNES                    | <b>4.2</b> (4) | 3.1(2)         | 5.2(3)         | 14(4)                        | 25(10)                       | 25(5)                        | 15/15 |
| xNESas                  | 4.3(5)         | 4.4(5)         | 7.2(4)         | 14(5)                        | 27(19)                       | 28(15)                       | 15/15 |

Table 5: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{104}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1             | 1e-3             | 1e-5             | 1e-7              | #succ |
|-------------------------|----------------|----------------|------------------|------------------|------------------|-------------------|-------|
| <b>f104</b>             | 5.4            | 15             | 194              | 248              | 256              | 263               | 15/15 |
| IPOPsaACM               | 4.4(3)         | <b>4.9</b> (4) | <b>1.5</b> (0.8) | <b>1.5</b> (0.6) | <b>1.5</b> (0.6) | <b>1.5</b> (0.6)* | 15/15 |
| SNES                    | 12(7)          | 9.2(12)        | 3.7(4)           | 125(158)         | $\infty$         | $\infty$ 2e4      | 0/15  |
| xNES                    | 4.7(6)         | 18(6)          | 5.7(7)           | 5.5(6)           | 7.5(16)          | 7.6(15)           | 15/15 |
| xNESas                  | <b>3.4</b> (3) | 32(5)          | 4.9(12)          | 4.9(10)          | 6.2(10)          | 6.3(10)           | 15/15 |

Table 6: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{105}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1            | 1e-3           | 1e-5           | 1e-7                           | #succ |
|-------------------------|----------------|----------------|-----------------|----------------|----------------|--------------------------------|-------|
| <b>f105</b>             | 5.4            | 15             | 357             | 381            | 397            | 410                            | 15/15 |
| IPOPsaACM               | 4.5(4)         | 11(4)          | <b>0.90</b> (1) | <b>1.4</b> (2) | <b>1.4</b> (2) | <b>1.5</b> (2)                 | 15/15 |
| SNES                    | <b>4.3</b> (5) | <b>6.4</b> (8) | 3.0(5)          | 52(53)         | 348(405)       | <i><math>\infty</math> 2e4</i> | 0/15  |
| xNES                    | 5.8(5)         | 37(8)          | 4.3(7)          | 5.7(10)        | 5.7(9)         | 5.7(9)                         | 15/15 |
| xNESas                  | 54(6)          | 69(137)        | 7.2(12)         | 9.2(16)        | 11(16)         | 11(15)                         | 15/15 |

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Table 7: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{106}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1             | 1e-3              | 1e-5              | 1e-7               | #succ |
|-------------------------|----------------|----------------|------------------|-------------------|-------------------|--------------------|-------|
| <b>f106</b>             | 5.4            | 15             | 139              | 352               | 490               | 650                | 15/15 |
| IPOPsaACM               | <b>2.7</b> (2) | <b>4.2</b> (4) | <b>1.1</b> (0.7) | <b>0.72</b> (0.5) | <b>0.63</b> (0.4) | <b>0.58</b> (0.4)* | 15/15 |
| SNES                    | 5.3(5)         | 4.5(4)         | 8.0(11)          | 48(46)            | 296(328)          | ∞ 2e4              | 0/15  |
| xNES                    | 5.6(6)         | 5.8(5)         | 2.3(3)           | 3.0(3)            | 3.2(5)            | 2.8(4)             | 15/15 |
| xNESas                  | 5.1(5)         | 11(11)         | 6.1(5)           | 4.5(4)            | 3.6(3)            | 2.9(2)             | 15/15 |



Table 8: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{107}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3             | 1e-5             | 1e-7             | #succ |
|-------------------------|----------------|----------------|----------------|------------------|------------------|------------------|-------|
| <b>f107</b>             | 1.8            | 13             | 28             | 158              | 255              | 421              | 15/15 |
| IPOPsaACM               | <b>5.2</b> (6) | <b>1.8</b> (2) | <b>2.1</b> (2) | 1.2(0.7)         | 1.4(0.6)         | 1.1(0.4)         | 15/15 |
| SNES                    | 15(21)         | 3.9(4)         | 2.7(3)         | <b>1.1</b> (0.6) | <b>1.3</b> (0.4) | <b>1.0</b> (0.2) | 15/15 |
| xNES                    | 27(19)         | 33(114)        | 18(55)         | 5.2(10)          | 3.6(6)           | 2.9(4)           | 13/15 |
| xNESas                  | 154(9)         | 90(171)        | 44(81)         | 10(15)           | 7.7(9)           | 5.6(6)           | 15/15 |

Table 9: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1                       | 1e0                       | 1e-1                      | 1e-3                        | 1e-5                                     | 1e-7  | #succ |
|-------------------------|---------------------------|---------------------------|---------------------------|-----------------------------|--|---|-------|
| <b>f108</b>             | 1.8                       | 30                        | 202                       | 3422                        | 7369                                     | 15979                                       | 15/15 |
| IPOPsaACM               | <b>15</b> <sup>(14)</sup> | <b>10</b> <sup>(13)</sup> | 4.8 <sup>(7)</sup>        | <b>1.0</b> <sup>(0.6)</sup> | <b>1.2</b> <sup>(1)</sup> * <sup>3</sup> | <b>0.88</b> <sup>(0.5)</sup> * <sup>3</sup> | 15/15 |
| SNES                    | 53 <sup>(74)</sup>        | 10 <sup>(15)</sup>        | <b>2.8</b> <sup>(3)</sup> | 2.5 <sup>(2)</sup>          | $\infty$                                 | $\infty$ 2e4                                | 0/15  |
| xNES                    | 170 <sup>(558)</sup>      | 49 <sup>(66)</sup>        | 11 <sup>(13)</sup>        | 10 <sup>(13)</sup>          | 287 <sup>(327)</sup>                     | $\infty$ 1e5                                | 0/15  |
| xNESas                  | 502 <sup>(1112)</sup>     | 100 <sup>(123)</sup>      | 31 <sup>(31)</sup>        | 34 <sup>(30)</sup>          | 406 <sup>(434)</sup>                     | $\infty$ 2e5                                | 0/15  |

Table 10: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{109}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3           | 1e-5           | 1e-7           | #succ |
|-------------------------|----------------|----------------|----------------|----------------|----------------|----------------|-------|
| <b>f109</b>             | 1.8            | 10             | 13             | 68             | 96             | 96             | 15/15 |
| IPOPsaACM               | 4.3(6)         | <b>2.2</b> (2) | 4.3(4)         | <b>2.3</b> (2) | <b>3.3</b> (2) | <b>5.5</b> (3) | 15/15 |
| SNES                    | <b>3.9</b> (2) | 2.4(1)         | <b>3.6</b> (2) | 2.6(1)         | 11(10)         | 336(417)       | 1/15  |
| xNES                    | 5.8(5)         | 3.6(4)         | 5.5(4)         | 5.8(3)         | 5.3(3)         | 8.7(12)        | 15/15 |
| xNESas                  | 5.4(6)         | 5.7(12)        | 11(10)         | 5.7(4)         | 9.1(17)        | 11(22)         | 15/15 |

Table 11: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{110}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3           | 1e-5             | 1e-7                | #succ |
|-------------------------|----------------|----------------|----------------|----------------|------------------|---------------------|-------|
| <b>f110</b>             | 7.1            | 34             | 623            | 2319           | 8407             | 9154                | 14/15 |
| IPOPsaACM               | <b>4.1</b> (3) | 5.8(2)         | 2.6(2)         | <b>2.9</b> (3) | <b>1.1</b> (0.9) | <b>1.0</b> (0.8)    | 15/15 |
| SNES                    | 5.9(7)         | <b>2.9</b> (4) | <b>1.2</b> (1) | 8.4(9)         | 34(38)           | $\infty$ <i>2e4</i> | 0/15  |
| xNES                    | 11(7)          | 26(30)         | 4.2(7)         | 4.2(4)         | 1.4(1)           | 1.3(1)              | 14/15 |
| xNESas                  | 7.1(8)         | 53(118)        | 8.8(10)        | 5.4(6)         | 2.2(2)           | 2.3(3)              | 15/15 |

Table 12: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{111}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3           | 1e-5           | 1e-7                | #succ |
|-------------------------|----------------|----------------|----------------|----------------|----------------|---------------------|-------|
| <b>f111</b>             | 24             | 119            | 718            | 12718          | 61860          | 1.7e5               | 15/15 |
| IPOPsaACM               | 5.9(3)         | 3.6(7)         | 4.1(3)         | 7.9(11)        | <b>2.7</b> (3) | <b>1.0</b> (1)      | 15/15 |
| SNES                    | <b>4.7</b> (5) | <b>2.9</b> (3) | <b>1.9</b> (2) | <b>4.9</b> (6) | $\infty$       | $\infty$ <i>2e4</i> | 0/15  |
| xNES                    | 29(83)         | 13(21)         | 12(12)         | 7.0(7)         | $\infty$       | $\infty$ <i>2e5</i> | 0/15  |
| xNESas                  | 50(90)         | 23(41)         | 17(21)         | 10(12)         | $\infty$       | $\infty$ <i>2e5</i> | 0/15  |

Table 13: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{112}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1              | 1e-3              | 1e-5              | 1e-7                | #succ |
|-------------------------|----------------|----------------|-------------------|-------------------|-------------------|---------------------|-------|
| <b>f112</b>             | 5.4            | 15             | 625               | 1154              | 1373              | 1531                | 15/15 |
| IPOPsaACM               | 4.8(6)         | 4.9(3)         | <b>0.51</b> (0.6) | <b>0.73</b> (0.5) | <b>0.97</b> (0.7) | <b>1.1</b> (0.6)    | 15/15 |
| SNES                    | 4.7(4)         | <b>4.1</b> (2) | 2.1(2)            | 42(45)            | $\infty$          | $\infty$ <i>2e4</i> | 0/15  |
| xNES                    | <b>3.1</b> (3) | 12(10)         | 2.5(4)            | 3.6(4)            | 4.3(4)            | 4.2(4)              | 15/15 |
| xNESas                  | 4.1(4)         | 23(14)         | 2.7(5)            | 4.1(4)            | 6.0(6)            | 5.5(5)              | 15/15 |

Table 14: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{113}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3           | 1e-5           | 1e-7           | #succ |
|-------------------------|----------------|----------------|----------------|----------------|----------------|----------------|-------|
| <b>f113</b>             | 4.7            | 31             | 87             | 174            | 174            | 876            | 15/15 |
| IPOPsaACM               | <b>4.3</b> (5) | <b>3.0</b> (5) | 11(20)         | 9.4(11)        | 9.4(11)        | <b>2.0</b> (2) | 15/15 |
| SNES                    | 8.8(11)        | 3.5(5)         | <b>5.9</b> (8) | <b>6.5</b> (8) | <b>6.5</b> (8) | 3.3(4)         | 14/15 |
| xNES                    | 7.6(9)         | 20(32)         | 14(29)         | 18(26)         | 18(26)         | 3.6(5)         | 15/15 |
| xNESas                  | 6.1(5)         | 25(75)         | 26(31)         | 30(57)         | 30(57)         | 6.0(11)        | 15/15 |

Table 15: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1                       | 1e0                       | 1e-1                        | 1e-3                      | 1e-5                      | 1e-7                        | #succ |
|-------------------------|---------------------------|---------------------------|-----------------------------|---------------------------|---------------------------|-----------------------------|-------|
| <b>f114</b>             | 8.9                       | 43                        | 698                         | 5343                      | 5343                      | 8680                        | 15/15 |
| IPOPsaACM               | 18 <sub>(20)</sub>        | 9.5 <sub>(13)</sub>       | 3.2 <sub>(3)</sub>          | <b>1.3</b> <sub>(1)</sub> | <b>1.3</b> <sub>(1)</sub> | <b>1.1</b> <sub>(0.6)</sub> | 15/15 |
| SNES                    | <b>5.7</b> <sub>(5)</sub> | <b>5.0</b> <sub>(5)</sub> | <b>1.3</b> <sub>(1.0)</sub> | 2.4 <sub>(3)</sub>        | 2.4 <sub>(3)</sub>        | 4.6 <sub>(5)</sub>          | 0/15  |
| xNES                    | 37 <sub>(114)</sub>       | 33 <sub>(50)</sub>        | 11 <sub>(12)</sub>          | 5.7 <sub>(6)</sub>        | 5.7 <sub>(6)</sub>        | 8.9 <sub>(7)</sub>          | 5/15  |
| xNESas                  | 141 <sub>(229)</sub>      | 162 <sub>(261)</sub>      | 21 <sub>(34)</sub>          | 17 <sub>(20)</sub>        | 17 <sub>(20)</sub>        | 20 <sub>(23)</sub>          | 5/15  |



Table 16: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{115}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3           | 1e-5           | 1e-7           | #succ |
|-------------------------|----------------|----------------|----------------|----------------|----------------|----------------|-------|
| <b>f115</b>             | 3.2            | 13             | 225            | 394            | 394            | 543            | 15/15 |
| IPOPsaACM               | <b>5.2</b> (4) | <b>4.4</b> (4) | 2.0(3)         | <b>2.0</b> (2) | <b>2.0</b> (2) | <b>1.8</b> (2) | 15/15 |
| SNES                    | 5.2(5)         | 6.4(2)         | <b>1.3</b> (2) | 2.4(4)         | 2.4(4)         | 7.6(14)        | 11/15 |
| xNES                    | 6.4(7)         | 24(74)         | 6.3(9)         | 5.3(6)         | 5.3(6)         | 4.7(5)         | 15/15 |
| xNESas                  | 5.2(4)         | 24(5)          | 3.8(9)         | 6.2(13)        | 6.2(13)        | 4.9(11)        | 15/15 |

Table 17: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{116}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1                       | 1e0                        | 1e-1                       | 1e-3                      | 1e-5                      | 1e-7                       | #succ |
|-------------------------|---------------------------|----------------------------|----------------------------|---------------------------|---------------------------|----------------------------|-------|
| <b>f116</b>             | 49                        | 101                        | 155                        | 275                       | 1041                      | 1788                       | 15/15 |
| IPOPsaACM               | 14 <sup>(19)</sup>        | 18 <sup>(20)</sup>         | 13 <sup>(13)</sup>         | 7.8 <sup>(8)</sup>        | 2.3 <sup>(2)</sup>        | 1.5 <sup>(1)</sup>         | 15/15 |
| SNES                    | 2.7 <sup>(4)</sup>        | 12 <sup>(10)</sup>         | 20 <sup>(16)</sup>         | 229 <sup>(264)</sup>      | $\infty$                  | $\infty$ <i>2e4</i>        | 0/15  |
| xNES                    | 15 <sup>(51)</sup>        | <b>8.4</b> <sup>(25)</sup> | <b>9.1</b> <sup>(17)</sup> | <b>5.6</b> <sup>(9)</sup> | <b>1.6</b> <sup>(2)</sup> | <b>0.98</b> <sup>(1)</sup> | 15/15 |
| xNESas                  | <b>2.0</b> <sup>(2)</sup> | 26 <sup>(43)</sup>         | 21 <sup>(29)</sup>         | 14 <sup>(16)</sup>        | 3.8 <sup>(4)</sup>        | 3.0 <sup>(6)</sup>         | 15/15 |

Table 18: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{117}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3              | 1e-5              | 1e-7                | #succ |
|-------------------------|----------------|----------------|----------------|-------------------|-------------------|---------------------|-------|
| <b>f117</b>             | 167            | 1346           | 6454           | 28223             | 36420             | 43231               | 15/15 |
| IPOPsaACM               | 3.7(7)         | 3.4(6)         | 2.0(2)         | <b>0.73</b> (0.6) | <b>0.70</b> (0.4) | <b>0.73</b> (0.3)   | 15/15 |
| SNES                    | <b>2.2</b> (5) | <b>1.1</b> (2) | <b>1.0</b> (1) | $\infty$          | $\infty$          | $\infty$ <i>2e4</i> | 0/15  |
| xNES                    | 5.0(6)         | 3.0(5)         | 2.8(4)         | 6.6(7)            | 62(62)            | $\infty$ <i>2e5</i> | 0/15  |
| xNESas                  | 23(26)         | 9.4(9)         | 3.4(4)         | 5.4(6)            | 80(88)            | $\infty$ <i>2e5</i> | 0/15  |

Table 19: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3              | 1e-5              | 1e-7                | #succ |
|-------------------------|----------------|----------------|----------------|-------------------|-------------------|---------------------|-------|
| <b>f118</b>             | 21             | 103            | 132            | 584               | 776               | 972                 | 15/15 |
| IPOPsaACM               | 3.7(2)         | <b>1.4</b> (1) | <b>1.4</b> (1) | <b>0.58</b> (0.4) | <b>0.64</b> (0.4) | <b>0.77</b> (0.5)   | 15/15 |
| SNES                    | 7.3(10)        | 12(12)         | 27(33)         | 51(59)            | $\infty$          | $\infty$ <i>2e4</i> | 0/15  |
| xNES                    | <b>3.6</b> (3) | 1.8(1)         | 2.6(3)         | 1.5(2)            | 1.9(2)            | 2.1(2)              | 15/15 |
| xNESas                  | 15(3)          | 4.4(5)         | 5.4(15)        | 1.5(4)            | 1.6(3)            | 2.3(4)              | 15/15 |

Table 20: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{119}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3                            | 1e-5              | 1e-7              | #succ |
|-------------------------|----------------|----------------|----------------|---------------------------------|-------------------|-------------------|-------|
| <b>f119</b>             | 1.4            | 11             | 71             | 1040                            | 4767              | 10082             | 15/15 |
| IPOPsaACM               | <b>2.4</b> (2) | 8.6(16)        | 1.9(2)         | 0.47(0.6)                       | <b>0.99</b> (0.7) | <b>0.82</b> (0.2) | 15/15 |
| SNES                    | 5.2(4)         | <b>5.2</b> (6) | <b>1.5</b> (1) | <b>0.44</b> (0.2) <sub>↓3</sub> | 4.4(5)            | 30(33)            | 1/15  |
| xNES                    | 5.3(8)         | 65(7)          | 10(1)          | 2.4(5)                          | 1.6(1)            | 1.1(1)            | 14/15 |
| xNESas                  | 10(11)         | 61(218)        | 13(33)         | 2.9(4)                          | 2.2(3)            | 1.8(2)            | 15/15 |

Table 21: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1              | 1e-3                        | 1e-5                           | 1e-7                           | #succ |
|-------------------------|----------------|----------------|-------------------|-----------------------------|--------------------------------|--------------------------------|-------|
| <b>f120</b>             | 1.4            | 11             | 374               | 5724                        | 75406                          | 1.9e5                          | 15/15 |
| IPOPsaACM               | 5.1(7)         | <b>10</b> (12) | 2.0(2)            | <b>2.0</b> (2) <sup>*</sup> | <b>0.46</b> (0.4) <sub>↓</sub> | <b>0.51</b> (0.4) <sub>↓</sub> | 15/15 |
| SNES                    | <b>4.8</b> (9) | 11(15)         | <b>0.98</b> (1.0) | 50(56)                      | $\infty$                       | $\infty$ <i>2e4</i>            | 0/15  |
| xNES                    | 107(33)        | 193(307)       | 12(20)            | 11(7)                       | $\infty$                       | $\infty$ <i>1e5</i>            | 0/15  |
| xNESas                  | 8.8(6)         | 160(375)       | 13(18)            | 23(24)                      | $\infty$                       | $\infty$ <i>2e5</i>            | 0/15  |

Table 22: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1             | 1e-3             | 1e-5             | 1e-7                | #succ |
|-------------------------|----------------|----------------|------------------|------------------|------------------|---------------------|-------|
| <b>f121</b>             | 1.4            | 7.1            | 42               | 327              | 1120             | 1702                | 15/15 |
| IPOPsaACM               | <b>2.5</b> (4) | <b>2.1</b> (2) | 1.2(0.7)         | <b>1.2</b> (0.7) | <b>1.0</b> (0.4) | <b>1.2</b> (0.4)    | 15/15 |
| SNES                    | 3.5(6)         | 4.7(5)         | 1.4(0.8)         | 1.9(2)           | 255(286)         | $\infty$ <i>2e4</i> | 0/15  |
| xNES                    | 4.4(5)         | 4.4(4)         | 1.7(1)           | 1.3(0.9)         | 1.2(1.0)         | 1.7(2)              | 15/15 |
| xNESas                  | 3.0(5)         | 2.6(2)         | <b>1.1</b> (0.7) | 1.7(0.8)         | 1.6(3)           | 2.3(4)              | 15/15 |

Table 23: 02-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{122}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0              | 1e-1            | 1e-3           | 1e-5             | 1e-7                            | #succ |
|-------------------------|----------------|------------------|-----------------|----------------|------------------|---------------------------------|-------|
| <b>f122</b>             | 2.9            | 95               | 523             | 2244           | 4351             | 9561                            | 15/15 |
| IPOPsaACM               | <b>3.9</b> (5) | <b>1.1</b> (0.7) | 1.3(1)          | <b>1.2</b> (1) | <b>1.2</b> (0.7) | <b>0.79</b> (0.4) <sup>*3</sup> | 15/15 |
| SNES                    | 18(13)         | 2.2(3)           | <b>0.94</b> (1) | 3.2(4)         | 65(75)           | $\infty$ 2e4                    | 0/15  |
| xNES                    | 116(343)       | 17(32)           | 4.9(7)          | 7.0(9)         | 13(13)           | 35(38)                          | 4/15  |
| xNESas                  | 106(28)        | 28(32)           | 14(19)          | 12(14)         | 19(15)           | 53(52)                          | 3/15  |



Table 24: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{123}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1                        | 1e0                       | 1e-1                         | 1e-3                         | 1e-5                         | 1e-7                         | #succ |
|-------------------------|----------------------------|---------------------------|------------------------------|------------------------------|------------------------------|------------------------------|-------|
| <b>f123</b>             | 3.1                        | 211                       | 6371                         | 38734                        | 1.0e5                        | 2.2e5                        | 15/15 |
| IPOPsaACM               | 40 <sup>(34)</sup>         | 3.7 <sup>(5)</sup>        | <b>0.90</b> <sup>(0.7)</sup> | <b>0.95</b> <sup>(0.4)</sup> | <b>0.68</b> <sup>(0.5)</sup> | <b>0.82</b> <sup>(0.5)</sup> | 15/15 |
| SNES                    | <b>8.0</b> <sup>(18)</sup> | <b>2.8</b> <sup>(4)</sup> | 2.2 <sup>(2)</sup>           | $\infty$                     | $\infty$                     | $\infty$ <i>2e4</i>          | 0/15  |
| xNES                    | 68 <sup>(10)</sup>         | 20 <sup>(19)</sup>        | 8.3 <sup>(9)</sup>           | $\infty$                     | $\infty$                     | $\infty$ <i>1e5</i>          | 0/15  |
| xNESas                  | 172 <sup>(527)</sup>       | 47 <sup>(55)</sup>        | 12 <sup>(16)</sup>           | $\infty$                     | $\infty$                     | $\infty$ <i>2e5</i>          | 0/15  |

Table 25: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{124}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1              | 1e-3              | 1e-5               | 1e-7           | #succ |
|-------------------------|----------------|----------------|-------------------|-------------------|--------------------|----------------|-------|
| <b>f124</b>             | 3.5            | 64             | 316               | 1991              | 5595               | 9019           | 15/15 |
| IPOPsaACM               | <b>2.3</b> (2) | 3.4(1)         | 1.4(2)            | <b>0.84</b> (0.7) | <b>1.1</b> (0.8)*4 | <b>2.4</b> (1) | 15/15 |
| SNES                    | 4.0(3)         | <b>1.9</b> (3) | <b>0.91</b> (0.9) | 71(72)            | $\infty$           | $\infty$ 2e4   | 0/15  |
| xNES                    | 4.0(5)         | 6.3(17)        | 2.7(5)            | 4.6(5)            | 23(22)             | 41(46)         | 5/15  |

Table 26: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{125}$ , in *italics* is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1          | 1e0            | 1e-1           | 1e-3            | 1e-5           | 1e-7           | #succ |
|-------------------------|--------------|----------------|----------------|-----------------|----------------|----------------|-------|
| <b>f125</b>             | 1            | 1              | 1              | 1150            | 3854           | 7556           | 15/15 |
| IPOPsaACM               | 1.1(0)       | <b>4.1</b> (4) | 37(34)         | 1.9(3)          | <b>1.4</b> (1) | <b>1.6</b> (2) | 15/15 |
| SNES                    | <b>1</b> (0) | 6.3(9)         | 40(49)         | <b>0.82</b> (1) | 2.7(2)         | 12(13)         | 1/15  |
| xNES                    | 1.1(0)       | 6.8(9)         | 60(48)         | 4.6(5)          | 5.1(6)         | 3.1(3)         | 14/15 |
| xNESas                  | 1.3(1)       | 6.1(4)         | <b>30</b> (32) | 7.2(7)          | 7.1(8)         | 8.4(10)        | 14/15 |

Table 27: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best}}$  2009 on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1          | 1e0            | 1e-1           | 1e-3           | 1e-5           | 1e-7           | #succ |
|-------------------------|--------------|----------------|----------------|----------------|----------------|----------------|-------|
| <b>f126</b>             | 1            | 1              | 1              | 3417           | 11056          | 36387          | 15/15 |
| IPOPsaACM               | <b>1</b> (0) | 9.2(10)        | 70(89)         | <b>1.3</b> (1) | <b>1.3</b> (1) | <b>1.4</b> (1) | 15/15 |
| SNES                    | <b>1</b> (0) | 5.5(8)         | <b>66</b> (79) | 1.5(2)         | 8.2(9)         | $\infty$ 2e4   | 0/15  |
| xNES                    | 1.1(0)       | 6.1(6)         | 667(1505)      | 4.4(4)         | 7.3(8)         | 60(67)         | 0/15  |
| xNESas                  | 1.1(0)       | <b>3.3</b> (2) | 980(2133)      | 10(13)         | 12(5)          | 25(25)         | 1/15  |

Table 28: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1              | 1e0            | 1e-1           | 1e-3           | 1e-5            | 1e-7           | #succ |
|-------------------------|------------------|----------------|----------------|----------------|-----------------|----------------|-------|
| <b>f127</b>             | 1                | 1              | 1              | 1185           | 6771            | 7277           | 13/15 |
| IPOPsaACM               | 1.3(0)           | 5.5(6)         | 75(59)         | 2.5(2)         | <b>0.94</b> (1) | <b>1.1</b> (1) | 15/15 |
| SNES                    | <b>1.1</b> (0.5) | 4.9(5)         | <b>37</b> (31) | <b>1.6</b> (1) | 1.7(2)          | 19(21)         | 0/15  |
| xNES                    | 1.8(0.5)         | 5.7(6)         | 167(87)        | 7.4(10)        | 2.6(3)          | 5.0(6)         | 15/15 |
| xNESas                  | 1.3(0)           | <b>4.3</b> (6) | 67(77)         | 8.9(14)        | 3.5(4)          | 5.5(6)         | 15/15 |

Table 29: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best}} 2009$  on  $f_{128}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3           | 1e-5              | 1e-7           | #succ |
|-------------------------|----------------|----------------|----------------|----------------|-------------------|----------------|-------|
| <b>f128</b>             | 1.8            | 41             | 134            | 387            | 593               | 620            | 15/15 |
| IPOPsaACM               | 1.5(1)         | 8.1(8)         | 22(23)         | 19(28)         | 83(23)            | 91(23)         | 15/15 |
| SNES                    | 1.6(1)         | <b>5.1</b> (6) | <b>2.0</b> (3) | <b>1.2</b> (1) | <b>0.93</b> (0.8) | <b>1.3</b> (2) | 15/15 |
| xNES                    | 1.4(0.8)       | 46(72)         | 22(23)         | 10(13)         | 6.9(8)            | 6.6(8)         | 15/15 |
| xNESas                  | <b>1.2</b> (1) | 32(61)         | 65(99)         | 32(39)         | 23(26)            | 22(25)         | 15/15 |

Table 30: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{129}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1               | 1e0            | 1e-1           | 1e-3           | 1e-5           | 1e-7            | #succ |
|-------------------------|-------------------|----------------|----------------|----------------|----------------|-----------------|-------|
| <b>f129</b>             | 1.8               | 65             | 220            | 1902           | 5944           | 10661           | 15/15 |
| IPOPsaACM               | 1.4(2)            | <b>3.3</b> (4) | 11(9)          | 2.7(3)         | <b>1.6</b> (1) | <b>1.2</b> (1)* | 15/15 |
| SNES                    | 1.4(1)            | 3.5(4)         | <b>3.0</b> (4) | <b>1.6</b> (2) | 1.9(2)         | 13(14)          | 0/15  |
| xNES                    | <b>0.85</b> (0.6) | 25(32)         | 19(23)         | 5.0(6)         | 5.5(6)         | 11(10)          | 9/15  |
| xNESas                  | 1.1(0.8)          | 25(67)         | 35(36)         | 14(13)         | 18(13)         | 25(22)          | 6/15  |

Table 31: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

| $\Delta f_{\text{opt}}$ | 1e1            | 1e0            | 1e-1           | 1e-3           | 1e-5              | 1e-7              | #succ |
|-------------------------|----------------|----------------|----------------|----------------|-------------------|-------------------|-------|
| <b>f130</b>             | 1.5            | 45             | 198            | 797            | 1772              | 4442              | 15/15 |
| IPOPsaACM               | 1.7(1)         | 4.8(5)         | 8.2(15)        | 6.8(4)         | 12(13)            | 26(49)            | 15/15 |
| SNES                    | 1.4(1.0)       | <b>3.6</b> (4) | <b>2.6</b> (4) | <b>1.0</b> (1) | <b>0.62</b> (0.7) | <b>0.50</b> (0.4) | 15/15 |
| xNES                    | <b>1.3</b> (1) | 20(24)         | 16(32)         | 4.2(8)         | 1.9(4)            | 0.81(1)           | 15/15 |
| xNESas                  | 1.7(2)         | 57(89)         | 35(54)         | 8.9(13)        | 4.9(7)            | 2.0(3)            | 15/15 |



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