

# Comparison tables: BBOB 2010 noisy testbed with BBOB 2009 as reference in 3-D

The BBOBies

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## Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2010, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2010>. More than 30 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [11, 7]. The experimental set-up is described in [10].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [6]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [10] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values.

Table 1: 03-D, running time excess  $ERT/ERT_{\text{best}}$  2009 on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>101 Sphere moderate Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.33	1.2	4.4	6.3	6.7	9.3	11	11	13	
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	5.6	4.9	7.3	12	10	10	12	13	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.6</b>	<b>2.8</b>	6.0	7.7	7.6	8.3	9.3	11	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.2</b>	4.7	3.1	5.7	7.0	6.4	7.3	8.5	10	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	6.9	5.3	7.4	10	10	11	12	14	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	3.6	<b>3.0</b>	4.2	5.9	5.5	6.2	7.4	8.2	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.9</b>	3.6	5.2	5.1	5.7	6.4	7.4	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	3.3	<b>2.6</b>	<b>3.1</b>	<b>4.1</b>	<b>3.9</b>	<b>4.2</b>	<b>4.9</b>	<b>5.5</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	3.6	3.2	3.6	5.0	4.5	4.8	5.5	6.5	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>2.1</b>	3.4	<b>1.6</b>	<b>1.7</b>	<b>1.9</b>	<b>1.5</b>	<b>1.4</b>	<b>1.4</b>	<b>1.4</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	14	21	16	12	112	384	484	694	1414	1256	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	4.0	3.8	5.0	7.6	7.2	7.9	9.2	11	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	3.8	3.0	5.1	7.5	7.2	8.1	9.3	11	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	10	21	28	28	30	36	42	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.5</b>	<b>2.8</b>	<b>2.0</b>	<b>2.5</b>	<b>2.9</b>	<b>2.4</b>	<b>2.2</b>	<b>2.3</b>	<b>2.2</b>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	<b>2.4</b>	10	36	73	88	132	182	315	Basic RCGA [17]
SPSA	30	46	198	295	846	1989	1524	1398	1375	3664	SPSA [9]

Table 2: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>102 Sphere moderate unif</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.2	1e+00 4.0	1e-01 7.6	1e-02 9.3	1e-03 11	1e-04 12	1e-05 13	1e-07 16	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	5.6	5.6	5.9	7.2	8.1	9.5	11	11	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.3	3.9	4.6	5.4	6.2	7.1	7.6	8.6	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	3.1	3.1	4.1	4.9	5.4	6.5	7.1	7.6	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	4.3	5.8	5.3	7.4	8.1	8.9	8.6	14	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	3.2	<b>2.7</b>	<b>2.9</b>	3.6	4.3	5.1	5.6	6.0	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	4.2	3.3	3.3	4.0	4.7	5.2	5.7	6.0	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.2</b>	<b>2.2</b>	<b>3.1</b>	<b>3.4</b>	<b>3.9</b>	<b>4.1</b>	<b>4.5</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	3.0	<b>2.6</b>	<b>2.5</b>	<b>3.4</b>	<b>3.9</b>	<b>4.3</b>	<b>4.6</b>	<b>5.1</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.9</b>	3.6	<b>2.8</b>	<b>2.9</b>	<b>2.6</b>	<b>2.8</b>	<b>2.7</b>	<b>2.5</b>	<b>2.2</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	28	45	21	14	15	19	21	149	1947	4298	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	4.2	3.9	4.1	5.3	6.4	7.2	7.7	8.5	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	4.4	4.2	4.4	5.6	6.7	7.8	8.4	8.8	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	11	17	21	25	29	30	34	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.5</b>	5.9	5.7	5.4	7.2	6.8	8.1	9.1	10	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	<b>1.7</b>	17	29	43	77	115	167	242	Basic RCGA [17]
SPSA	24	38	470	396	697	2079	2142	2293	5383	87971	SPSA [9]

Table 3: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>103 Sphere moderate Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.2	1e+00 4.3	1e-01 6.4	1e-02 6.4	1e-03 6.4	1e-04 6.6	1e-05 7.7	1e-07 14	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	6.2	5.1	6.7	10	14	18	19	14	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.5</b>	<b>2.8</b>	4.5	7.5	10	12	13	10	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.7</b>	3.0	4.4	7.2	8.7	11	12	9.1	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	3.9	4.3	5.2	7.7	12	15	17	13	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	4.0	3.5	4.0	6.1	7.8	10	11	8.5	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.5</b>	<b>2.1</b>	3.9	5.8	7.8	9.4	10	<b>7.3</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.9</b>	<b>2.0</b>	<b>2.6</b>	<b>4.1</b>	<b>5.1</b>	<b>6.8</b>	<b>6.9</b>	<b>5.3</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	3.8	<b>2.3</b>	3.3	5.0	6.7	<b>8.5</b>	<b>8.0</b>	<b>6.1</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.9</b>	3.3	<b>1.7</b>	<b>1.6</b>	<b>2.0</b>	<b>5.6</b>	9.2	10	9.0	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	17	30	19	16	22	27	34	1298	2202	2619	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>2.9</b>	4.6	7.8	10	13	13	10	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	4.0	3.5	4.8	7.9	11	14	14	11	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	11	20	31	42	53	62	51	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	3.4	<b>2.1</b>	<b>2.6</b>	<b>3.4</b>	<b>4.8</b>	<b>5.9</b>	<b>5.8</b>	10	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	<b>2.3</b>	13	39	69	140	225	281	291	Basic RCGA [17]
SPSA	40	142	360	216	228	400	565	1216	4576	11577	SPSA [9]

Table 4: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{104}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	104 Rosenbrock moderate Gauss										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	1.4	7.2	10	69	201	212	216	218	219	223	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	4.2	3.1	6.6	10	14	36	50	88	88	86	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>2.5</b>	<b>1.4</b>	3.9	4.5	5.7	8.2	8.4	8.9	9.0	9.1	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	3.5	<b>1.6</b>	<b>2.4</b>	<b>2.5</b>	6.5	11	11	11	11	11	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	15	9.1	17	15	23	62	116	115	145	143	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>2.7</b>	<b>1.5</b>	<b>2.2</b>	5.3	3.3	3.3	3.4	3.5	3.5	3.6	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	3.6	<b>1.3</b>	<b>2.0</b>	<b>2.0</b>	<b>1.2</b>	<b>1.4</b>	<b>1.5</b>	<b>1.6</b>	<b>1.6</b>	<b>1.7</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>2.1</b>	<b>1.1</b>	<b>1.5</b>	<b>1.8</b>	<b>1.1</b>	<b>1.3</b>	<b>1.3</b>	<b>1.4</b>	<b>1.4</b>	<b>1.5</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	3.9	<b>1.5</b>	<b>2.1</b>	5.6	4.3	5.8	5.8	5.9	5.9	5.9	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>2.5</b>	<b>0.83</b>	<b>0.89</b>	3.0	<b>2.6</b>	3.3	3.4	4.1	4.1	4.1	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	61	19	29	138	255	242	239	314	312	315	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>2.4</b>	<b>1.2</b>	<b>2.7</b>	<b>1.9</b>	<b>1.3</b>	<b>1.5</b>	<b>1.7</b>	<b>1.8</b>	<b>1.9</b>	<b>2.0</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>2.7</b>	<b>2.1</b>	3.3	<b>2.7</b>	<b>2.0</b>	<b>2.5</b>	<b>2.8</b>	<b>2.9</b>	3.1	3.3	IPOP-CMA-ES [15]
CMA+DE-MOS	3.4	3.3	8.6	3.2	<b>3.0</b>	3.9	4.6	5.1	5.4	6.1	CMA+DE-MOS [13]
NEWUOA	<b>2.8</b>	<b>0.92</b>	<b>0.95</b>	<b>0.95</b>	<b>2.7</b>	8.2	18	28	34	40	NEWUOA [16]
Basic RCGA	3.4	4.0	11	40	169	561	1528	1543	<i>66e-3/5e4</i>	.	Basic RCGA [17]
SPSA	611	299	28922	<i>15e+0/1e5</i>	.	.	.	.	.	.	SPSA [9]



Table 6: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{106}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

**106 Rosenbrock moderate Cauchy**

$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	5.2	3.6	4.0	11	12	5.8	4.1	4.1	<b>2.7</b>	<b>2.6</b>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	3.1	<b>2.0</b>	3.8	13	10	4.3	<b>2.8</b>	<b>2.8</b>	<b>1.9</b>	<b>1.8</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	3.0	<b>2.3</b>	4.1	8.3	6.5	<b>2.9</b>	<b>2.0</b>	<b>2.0</b>	<b>1.3</b>	<b>1.3</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	12	9.2	10	40	29	13	8.8	8.8	5.7	5.3	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	5.3	<b>2.6</b>	3.1	9.5	6.6	<b>2.8</b>	<b>1.9</b>	<b>1.8</b>	<b>1.2</b>	<b>1.1</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.8</b>	<b>1.6</b>	3.3	9.0	6.1	<b>2.6</b>	<b>1.7</b>	<b>1.6</b>	<b>1.1</b>	<b>1.0</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>2.7</b>	<b>1.2</b>	<b>2.1</b>	5.0	<b>3.8</b>	<b>1.6</b>	<b>1.1</b>	<b>1.0</b>	<b>0.69</b>	<b>0.67</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	3.3	<b>1.4</b>	<b>2.3</b>	7.3	5.4	<b>2.3</b>	<b>1.5</b>	<b>1.5</b>	<b>0.98</b>	<b>0.92</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	3.1	<b>1.1</b>	<b>1.1</b>	<b>2.4</b>	<b>1.9</b>	<b>1.0</b>	<b>2.1</b>	3.3	5.0	7.5	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	40	17	17	40	24	10	7.1	7.0	4.8	5.4	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>2.8</b>	<b>1.5</b>	<b>2.7</b>	<b>3.7</b>	<b>4.3</b>	<b>2.0</b>	<b>1.3</b>	<b>1.3</b>	<b>0.90</b>	<b>0.90</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	3.2	<b>2.3</b>	3.3	5.1	6.5	3.1	<b>2.1</b>	<b>2.1</b>	<b>1.4</b>	<b>1.4</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	3.4	3.9	10	8.6	10	4.8	3.0	3.2	<b>2.2</b>	<b>2.4</b>	CMA+DE-MOS [13]
NEWUOA	3.0	<b>0.95</b>	<b>1.0</b>	<b>3.3</b>	5.6	4.4	7.4	14	13	33	NEWUOA [16]
Basic RCGA	3.2	4.6	14	145	911	1110	2842	<i>43e-3/5e4</i>	.	.	Basic RCGA [17]
SPSA	1188	595	815	9052	<i>19e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 7: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{107}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

		107 Sphere Gauss											
$\Delta f_{\text{target}}/ERT_{\text{best}}/D$		1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}/ERT_{\text{best}}/D$	
		0.33	0.33	2.0	16	51	77	108	138	168	228		
	(1,2)-CMA-ES	<b>1</b>	<b>1</b>	22	12	10	22	27	45	203	<i>28e-6/1e4</i>	(1,2)-CMA-ES [4, 2]	
	(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	7.4	<b>1.9</b>	<b>1.9</b>	<b>2.1</b>	<b>2.1</b>	<b>2.7</b>	3.2	4.1	(1,2m)-CMA-ES [4]	
	(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	7.0	<b>2.2</b>	<b>2.2</b>	3.5	4.7	4.6	7.3	8.2	(1,2ms)-CMA-ES [4]	
	(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	5.9	8.4	13	17	48	115	95	642	(1,2s)-CMA-ES [2]	
	(1,4)-CMA-ES	<b>1</b>	<b>1</b>	8.9	3.4	<b>2.9</b>	3.3	3.5	4.4	6.2	5.8	(1,4)-CMA-ES [5, 3]	
	(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	3.7	<b>1.2</b>	<b>0.71</b>	<b>0.82</b>	<b>0.96</b>	<b>1.2</b>	<b>1.1</b>	<b>1.5</b>	(1,4m)-CMA-ES [5]	
	(1,4ms)-CMA-ES	<b>1</b>	<b>1.1</b>	14	<b>2.5</b>	<b>1.2</b>	<b>1.6</b>	<b>1.6</b>	<b>1.9</b>	3.1	4.2	(1,4ms)-CMA-ES [1, 5]	
	(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	<b>2.2</b>	<b>1.5</b>	3.7	3.3	3.9	4.4	10	(1,4s)-CMA-ES [3]	
	avg NEWUOA	<b>1</b>	<b>1</b>	17	20	45	115	360	592	<i>16e-3/6e3</i>	.	avg NEWUOA [16]	
	CMA-EGS (IPOP,r1)	24	37	13	5.0	6.1	14	49	226	555	6150	CMA-EGS (IPOP,r1) [8]	
	IPOP-aCMA-ES	<b>1</b>	<b>2.0</b>	5.4	<b>1.4</b>	<b>0.99</b>	<b>0.97</b>	<b>0.96</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	IPOP-aCMA-ES [12]	
	IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1.7</b>	<b>1.2</b>	<b>0.80</b>	<b>0.96</b>	<b>1.0</b>	<b>0.95</b>	<b>0.98</b>	<b>1.0</b>	IPOP-CMA-ES [15]	
	CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.6</b>	3.3	5.3	7.2	7.2	7.2	7.2	7.0	CMA+DE-MOS [13]	
	NEWUOA	<b>1</b>	<b>1.1</b>	12	29	61	65	150	532	<i>57e-4/5e3</i>	.	NEWUOA [16]	
	Basic RCGA	<b>1</b>	<b>1</b>	<b>1.6</b>	7.8	9.2	11	13	20	26	31	Basic RCGA [17]	
	SPSA	36	53	199	8554	13692	18097	13131	<i>11e-1/1e5</i>	.	.	SPSA [9]	

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Table 8: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	108 Sphere unif										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.9	1e+00 33	1e-01 655	1e-02 1842	1e-03 3608	1e-04 5060	1e-05 5729	1e-07 10727	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	34	29	53	<i>15e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	23	24	25	13	37	<i>84e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	54	25	23	81	<i>10e-2/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	30	41	19	79	<i>88e-3/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.1</b>	30	<b>10</b>	6.0	38	<i>42e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	30	19	<b>5.9</b>	<b>14</b>	<i>18e-3/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>10</b>	14	9.3	38	<i>38e-3/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	35	20	8.6	77	<i>39e-3/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.5</b>	121	82	126	<i>39e-2/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	1294	1758	2673	269	44	25	<b>17</b>	<b>25</b>	<b>44</b>	68	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	14	<b>8.4</b>	<b>1.8</b>	<b>1.1</b>	<b>0.96</b>	<b>0.80</b>	<b>1.1</b>	<b>0.81</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.1</b>	97	11	<b>1.3</b>	<b>1.0</b>	<b>0.89</b>	<b>0.92</b>	<b>1.1</b>	<b>1.0</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.6</b>	66	138	91	61	49	45	<b>29</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	108	56	36	<i>41e-2/5e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>2.1</b>	<b>10</b>	24	20	22	33	129	<i>18e-4/5e4</i>	Basic RCGA [17]
SPSA	111	264	275	166	58	390	<i>28e-3/1e5</i>	.	.	.	SPSA [9]

Table 9: 03-D, running time excess  $ERT/ERT_{\text{best}}$  2009 on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	109 Sphere Cauchy										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.2	1e+00 6.8	1e-01 31	1e-02 48	1e-03 64	1e-04 65	1e-05 84	1e-07 84	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	5.4	3.5	<b>2.0</b>	<b>1.9</b>	<b>2.8</b>	3.6	3.9	6.8	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.9	<b>2.9</b>	<b>1.3</b>	<b>1.6</b>	<b>1.7</b>	<b>2.3</b>	<b>2.4</b>	3.7	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	3.5	<b>1.8</b>	<b>0.83</b>	<b>0.96</b>	<b>1.1</b>	<b>1.4</b>	<b>1.5</b>	<b>2.4</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	8.9	7.6	<b>2.5</b>	3.1	3.5	4.5	6.1	8.3	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>1.9</b>	<b>0.92</b>	<b>1.1</b>	<b>1.2</b>	<b>1.8</b>	<b>1.7</b>	3.0	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	4.1	<b>2.0</b>	<b>1.1</b>	<b>1.2</b>	<b>1.3</b>	<b>1.8</b>	<b>1.7</b>	<b>2.6</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.1</b>	<b>1.3</b>	<b>0.66</b>	<b>0.72</b>	<b>0.72</b>	<b>0.99</b>	<b>0.94</b>	<b>1.3</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.2</b>	<b>1.6</b>	<b>0.75</b>	<b>0.84</b>	<b>0.90</b>	<b>1.2</b>	<b>1.2</b>	<b>1.8</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.5</b>	3.4	7.6	5.9	8.9	17	58	112	262	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	15	30	21	9.5	4.4	33	403	3363	<i>20e-5/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.6</b>	<b>1.3</b>	<b>1.4</b>	<b>1.6</b>	<b>2.0</b>	<b>2.1</b>	3.1	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	4.5	<b>2.3</b>	<b>1.2</b>	<b>1.3</b>	<b>1.7</b>	<b>2.3</b>	<b>2.4</b>	3.6	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	6.1	4.2	5.6	6.4	10	12	16	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.3</b>	5.3	6.2	6.4	12	34	146	181	<i>17e-5/5e3</i>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	3.4	11	11	14	20	27	33	51	Basic RCGA [17]
SPSA	37	157	448	231	1467	1620	3769	6888	<i>43e-4/1e5</i>	.	SPSA [9]





Table 12: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{112}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>112 Rosenbrock Cauchy</b>												
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$	
$ERT_{\text{best}}/D$	1.4	7.2	10	113	523	826	950	993	1035	1178	$ERT_{\text{best}}/D$	
(1,2)-CMA-ES	7.7	7.6	17	28	10	8.7	8.0	7.8	8.5	7.8	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>3.0</b>	<b>2.6</b>	3.3	5.8	<b>2.5</b>	<b>2.0</b>	<b>1.9</b>	<b>2.0</b>	<b>2.0</b>	<b>1.9</b>	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	5.1	<b>2.2</b>	3.5	5.1	<b>1.7</b>	<b>1.4</b>	<b>1.4</b>	<b>1.4</b>	<b>1.4</b>	<b>1.3</b>	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	4.5	4.4	8.7	27	12	16	17	21	31	28	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>2.9</b>	<b>1.4</b>	<b>2.2</b>	<b>1.3</b>	<b>0.95</b>	<b>0.88</b>	<b>0.88</b>	<b>0.93</b>	<b>0.93</b>	<b>0.89</b>	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>3.0</b>	<b>1.3</b>	<b>2.3</b>	3.1	<b>1.1</b>	<b>0.90</b>	<b>0.87</b>	<b>0.87</b>	<b>0.86</b>	<b>0.83</b>	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>2.9</b>	<b>1.2</b>	<b>1.9</b>	<b>2.1</b>	<b>0.76</b>	<b>0.58</b>	<b>0.56</b>	<b>0.56</b>	<b>0.56</b>	<b>0.52</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	3.1	<b>1.6</b>	<b>2.7</b>	4.6	<b>1.5</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>2.8</b>	<b>0.93</b>	<b>2.1</b>	<b>2.2</b>	<b>1.8</b>	10	85	<i>20e-3/6e3</i>	.	.	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	57	24	23	306	571	1699	<i>26e-2/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	3.0	<b>1.8</b>	3.8	<b>1.6</b>	<b>0.79</b>	<b>0.70</b>	<b>0.72</b>	<b>0.74</b>	<b>0.76</b>	<b>0.76</b>	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	4.2	<b>2.3</b>	3.7	4.6	<b>1.8</b>	<b>1.5</b>	<b>1.5</b>	<b>1.5</b>	<b>1.5</b>	<b>1.5</b>	IPOP-CMA-ES [15]	
CMA+DE-MOS	3.4	4.0	10	<b>2.4</b>	<b>1.9</b>	<b>1.6</b>	<b>1.6</b>	<b>1.8</b>	<b>1.9</b>	<b>2.0</b>	CMA+DE-MOS [13]	
NEWUOA	<b>2.0</b>	<b>0.89</b>	<b>1.3</b>	<b>1.7</b>	<b>1.4</b>	8.7	37	73	<i>44e-4/5e3</i>	.	NEWUOA [16]	
Basic RCGA	<b>2.7</b>	3.6	11	18	72	93	365	713	<i>23e-3/5e4</i>	.	Basic RCGA [17]	
SPSA	1314	1782	2830	12462	<i>29e-1/1e5</i>	.	.	.	.	.	SPSA [9]	

Table 13: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{113}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	113 Step-ellipsoid Gauss										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>2.5</b>	11	6.6	11	<b>2.6</b>	6.0	11	11	11	15	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.4</b>	<b>1.3</b>	<b>2.6</b>	<b>4.1</b>	<b>0.84</b>	<b>2.9</b>	4.1	4.1	4.1	6.4	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.2</b>	<b>2.4</b>	8.6	7.4	<b>1.3</b>	<b>1.8</b>	7.3	7.3	7.3	13	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>2.7</b>	24	12	8.7	3.6	18	41	41	41	125	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.6</b>	<b>3.0</b>	4.2	4.9	<b>2.0</b>	<b>2.3</b>	3.5	3.5	3.5	3.8	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.1</b>	<b>2.5</b>	<b>1.1</b>	5.7	<b>1.9</b>	<b>2.6</b>	3.4	3.4	3.4	3.4	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1.3</b>	4.4	6.3	4.9	<b>1.6</b>	<b>2.7</b>	<b>2.8</b>	<b>2.8</b>	<b>2.8</b>	<b>3.2</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.3</b>	<b>2.8</b>	<b>2.4</b>	<b>4.6</b>	<b>1.7</b>	<b>2.2</b>	3.3	3.3	3.3	5.8	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1.6</b>	5.6	8.2	15	8.0	25	75	75	75	<i>57e-3/6e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	28	14	22	19	82	292	392	392	392	1280	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	20	8.4	<b>2.0</b>	7.7	<b>0.88</b>	<b>0.60</b>	<b>0.77</b>	<b>0.77</b>	<b>0.77</b>	<b>0.75</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.7</b>	<b>2.7</b>	<b>1.8</b>	6.6	<b>1.9</b>	<b>1.8</b>	<b>1.8</b>	<b>1.8</b>	<b>1.8</b>	<b>1.8</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.1</b>	<b>1.7</b>	<b>1.3</b>	<b>4.1</b>	3.4	3.4	3.5	3.5	3.5	3.5	CMA+DE-MOS [13]
NEWUOA	<b>1.5</b>	14	7.7	14	5.1	12	70	70	70	<i>74e-3/5e3</i>	NEWUOA [16]
Basic RCGA	<b>1.1</b>	<b>1.6</b>	<b>2.1</b>	11	19	39	38	38	38	38	Basic RCGA [17]
SPSA	40	24	18	1660	1007	1374	<i>71e-2/1e5</i>	.	.	.	SPSA [9]

Table 14: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	114 Step-ellipsoid unif										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.98	8.5	338	2093	6295	9441	9441	9441	10860	
(1,2)-CMA-ES	<b>1.1</b>	5.1	34	11	21	<i>31e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.1</b>	8.2	17	6.9	21	<i>30e-2/1e4</i>	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.1</b>	63	32	22	23	<i>22e-2/1e4</i>	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1.1</b>	35	30	12	<i>52e-2/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.3</b>	67	21	3.6	7.6	23	<i>11e-2/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1.8</b>	<b>2.2</b>	<b>6.7</b>	<b>2.5</b>	<b>5.7</b>	<b>10</b>	15	15	15	<i>83e-3/1e4</i>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1.8</b>	27	25	4.0	12	<i>16e-2/1e4</i>	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	17	14	19	6.4	10	<i>22e-2/1e4</i>	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	143	104	26	<i>11e-1/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	877	2294	553	127	148	<i>14e-2/1e5</i>	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1.4</b>	34	25	<b>1.4</b>	<b>0.88</b>	<b>0.61</b>	<b>0.42</b>	<b>0.42</b>	<b>0.42</b>	<b>0.39</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.1</b>	12	7.1	<b>2.4</b>	<b>1.6</b>	<b>0.81</b>	<b>0.60</b>	<b>0.60</b>	<b>0.60</b>	<b>0.59</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.1</b>	<b>1.9</b>	<b>1.9</b>	9.3	31	20	13	13	13	<b>14</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	50	71	31	<i>11e-1/5e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1.5</b>	<b>1.8</b>	<b>1.6</b>	8.0	12	14	<b>12</b>	<b>12</b>	<b>12</b>	20	Basic RCGA [17]
SPSA	271	204	223	63	685	<i>29e-2/1e5</i>	.	.	.	.	SPSA [9]

Table 15: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{115}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>115 Step-ellipsoid Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1.7</b>	3.2	4.9	<b>2.7</b>	7.9	41	63	63	63	<i>54e-4/1e4</i>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.5</b>	<b>2.1</b>	<b>1.7</b>	<b>2.1</b>	<b>2.8</b>	5.8	12	12	12	21	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.1</b>	<b>1.5</b>	<b>2.9</b>	<b>1.4</b>	<b>1.6</b>	5.0	13	13	13	39	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1.5</b>	3.8	4.3	3.4	3.4	23	50	50	50	169	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.5</b>	3.6	<b>2.9</b>	<b>1.4</b>	<b>1.6</b>	<b>2.8</b>	4.3	4.3	4.3	6.5	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1.4</b>	<b>2.9</b>	<b>2.7</b>	<b>0.88</b>	<b>1.3</b>	<b>1.4</b>	3.4	3.4	3.4	4.1	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1.1</b>	<b>1.4</b>	<b>2.1</b>	<b>1.2</b>	<b>0.87</b>	<b>1.4</b>	<b>1.6</b>	<b>1.6</b>	<b>1.6</b>	<b>2.1</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.1</b>	<b>1.9</b>	4.5	<b>1.9</b>	<b>1.6</b>	<b>2.5</b>	3.1	3.1	3.1	5.3	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1.5</b>	3.1	<b>1.1</b>	<b>2.6</b>	4.9	19	45	45	45	59	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	24	17	20	122	392	1637	4763	4763	4763	3402	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1.2</b>	<b>2.7</b>	<b>2.0</b>	<b>0.88</b>	<b>0.91</b>	<b>0.80</b>	<b>0.90</b>	<b>0.90</b>	<b>0.90</b>	<b>0.78</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.7</b>	3.2	6.4	<b>2.4</b>	<b>1.8</b>	<b>2.4</b>	<b>2.4</b>	<b>2.4</b>	<b>2.4</b>	<b>1.9</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.1</b>	<b>2.0</b>	<b>2.3</b>	<b>2.1</b>	5.0	7.4	7.6	7.6	7.6	5.6	CMA+DE-MOS [13]
NEWUOA	<b>2.4</b>	<b>2.8</b>	<b>0.96</b>	4.0	8.3	66	215	215	215	154	NEWUOA [16]
Basic RCGA	<b>1.1</b>	<b>0.95</b>	6.1	56	96	145	138	138	138	129	Basic RCGA [17]
SPSA	52	44	49	576	560	1532	<i>43e-3/1e5</i>	.	.	.	SPSA [9]



Table 16: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{116}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	116 Ellipsoid Gauss										
$\Delta\text{ftarget}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$
$ERT_{\text{best}}/D$	6.2	25	56	881	1473	2051	2381	3153	3205	3790	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	14	14	17	9.4	96	<i>68e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	6.3	11	14	4.0	8.4	10	14	10	46	<i>54e-3/1e4</i>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	11	12	27	5.6	6.8	34	<i>45e-3/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	14	36	40	13	46	34	63	<i>61e-2/1e4</i>	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>2.4</b>	<b>2.3</b>	12	3.8	11	15	18	15	15	19	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	4.6	<b>5.9</b>	10	3.1	4.3	4.9	5.4	7.6	14	12	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	11	8.9	11	<b>1.8</b>	4.0	4.5	5.5	7.9	10	<i>96e-5/1e4</i>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	17	7.0	<b>8.2</b>	<b>2.2</b>	3.9	7.1	13	14	<i>18e-3/1e4</i>	.	(1,4s)-CMA-ES [3]
avg NEWUOA	19	24	65	28	<i>30e-1/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	1443	1318	1980	1701	<i>97e-1/1e5</i>	.	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	6.8	6.2	<b>5.9</b>	<b>1.3</b>	<b>1.2</b>	<b>1.0</b>	<b>0.90</b>	<b>0.71</b>	<b>0.71</b>	<b>0.63</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	4.5	7.4	11	<b>2.8</b>	<b>2.5</b>	<b>2.1</b>	<b>1.9</b>	<b>1.5</b>	<b>1.5</b>	<b>1.3</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.2</b>	<b>2.8</b>	<b>7.3</b>	4.4	<b>3.0</b>	<b>2.4</b>	<b>2.2</b>	<b>1.9</b>	<b>2.0</b>	<b>1.9</b>	CMA+DE-MOS [13]
NEWUOA	12	18	45	41	50	<i>49e-1/5e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>2.6</b>	18	61	26	52	65	<i>67e-3/5e4</i>	.	.	.	Basic RCGA [17]
SPSA	98	863	4071	1622	<i>20e+0/1e5</i>	.	.	.	.	.	SPSA [9]



Table 18: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>118 Ellipsoid Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	11	18	9.4	15	7.2	6.5	6.1	5.8	5.6	6.5	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	4.1	8.8	4.2	7.5	3.4	3.4	3.3	<b>3.0</b>	3.0	<b>2.7</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	4.0	7.4	5.5	5.5	<b>2.0</b>	<b>1.8</b>	<b>2.0</b>	<b>1.9</b>	<b>1.8</b>	<b>1.6</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	6.9	13	30	46	23	24	27	23	21	20	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	4.1	6.5	<b>2.6</b>	3.2	<b>1.3</b>	<b>1.3</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.5</b>	6.8	3.2	3.5	<b>1.2</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>0.99</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>2.4</b>	<b>3.4</b>	<b>2.0</b>	<b>2.3</b>	<b>0.92</b>	<b>0.83</b>	<b>0.78</b>	<b>0.71</b>	<b>0.71</b>	<b>0.66</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.6</b>	6.0	3.3	<b>3.0</b>	<b>1.1</b>	<b>1.0</b>	<b>0.93</b>	<b>0.85</b>	<b>0.82</b>	<b>0.75</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>0.98</b>	<b>1.4</b>	<b>1.0</b>	5.0	5.4	26	77	<i>43e-4/6e3</i>	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	38	81	715	2979	2747	4936	<i>21e-1/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	3.3	4.9	3.4	<b>3.0</b>	<b>1.0</b>	<b>0.98</b>	<b>0.95</b>	<b>0.89</b>	<b>0.94</b>	<b>0.94</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	4.3	7.9	6.2	6.7	<b>2.6</b>	<b>2.4</b>	<b>2.2</b>	<b>2.0</b>	<b>2.0</b>	<b>1.9</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	3.3	10	6.0	5.2	<b>1.9</b>	<b>2.0</b>	<b>2.3</b>	<b>2.5</b>	<b>2.8</b>	3.1	CMA+DE-MOS [13]
NEWUOA	<b>1.3</b>	<b>1.4</b>	<b>1.7</b>	3.7	6.5	43	109	<i>19e-3/5e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>2.3</b>	78	142	542	672	1269	2227	<i>75e-2/5e4</i>	.	.	Basic RCGA [17]
SPSA	126	254	1406	6641	<i>41e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 19: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{119}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	119 Sum of diff powers Gauss										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.33	0.33	0.73	22	140	203	668	1894	4013	5240	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.3</b>	6.6	4.3	5.3	17	48	<i>24e-4/1e4</i>	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	4.8	3.2	<b>1.7</b>	4.2	3.2	8.2	17	<i>14e-5/1e4</i>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>2.2</b>	<b>1.5</b>	<b>1.4</b>	<b>2.9</b>	4.5	35	<i>18e-5/1e4</i>	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.1</b>	28	6.9	3.7	39	110	<i>50e-4/1e4</i>	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>2.1</b>	9.2	4.3	<b>1.5</b>	<b>3.0</b>	<b>2.4</b>	4.1	18	<i>63e-6/1e4</i>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.3</b>	4.7	3.2	<b>0.92</b>	<b>1.5</b>	<b>2.3</b>	3.0	3.9	28	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.8</b>	12	<b>1.7</b>	<b>0.96</b>	<b>1.8</b>	<b>2.6</b>	<b>2.9</b>	6.1	<i>48e-6/1e4</i>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	3.7	43	3.7	<b>2.0</b>	3.2	4.9	9.3	35	<i>18e-5/1e4</i>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	23	8.2	16	51	<i>13e-3/6e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	24	36	25	24	25	136	193	367	<i>11e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>2.1</b>	5.5	<b>1.1</b>	<b>0.55</b>	<b>0.92</b>	<b>0.77</b>	<b>0.87</b>	<b>0.72</b>	<b>0.79</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.9</b>	8.4	<b>0.93</b>	<b>0.38</b>	<b>0.69</b>	<b>0.91</b>	<b>1.2</b>	<b>1.0</b>	<b>1.7</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.2</b>	<b>1.2</b>	<b>2.6</b>	4.6	<b>2.1</b>	<b>1.0</b>	<b>0.68</b>	<b>1.0</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>2.2</b>	13	18	27	116	114	<i>31e-3/5e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.3</b>	<b>2.4</b>	6.6	6.2	7.6	9.3	8.9	24	<i>17e-6/5e4</i>	Basic RCGA [17]
SPSA	35	55	187	5891	10571	7294	<i>10e-1/1e5</i>	.	.	.	SPSA [9]

Table 20: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	120 Sum of diff powers unif											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 0.73	1e+00 27	1e-01 601	1e-02 2312	1e-03 10645	1e-04 25282	1e-05 40067	1e-07 88603	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	
(1,2)-CMA-ES	1	41	43	31	31	<i>11e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	1	4.0	58	<b>7.8</b>	15	<i>54e-3/1e4</i>	.	.	.	.	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	1	<b>1.1</b>	65	31	29	63	<i>14e-2/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	1	<b>1.3</b>	22	37	28	29	<i>13e-2/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	1	3.1	9.0	11	13	62	<i>71e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	1	<b>1.4</b>	27	12	<b>7.1</b>	<i>44e-3/1e4</i>	.	.	.	.	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	1	<b>1.7</b>	<b>5.3</b>	17	10	61	<i>31e-3/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	1	<b>1</b>	54	18	14	<i>51e-3/1e4</i>	.	.	.	.	(1,4s)-CMA-ES [3]	
avg NEWUOA	1	24	120	66	40	<i>36e-2/6e3</i>	.	.	.	.	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	779	1826	2111	847	151	74	43	58	<i>11e-3/1e5</i>	.	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	1	<b>2.2</b>	14	8.3	<b>1.9</b>	<b>1.6</b>	<b>0.66</b>	<b>0.49</b>	<b>0.57</b>	<b>0.50</b>	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	1	<b>1.3</b>	8.6	11	<b>1.9</b>	<b>0.97</b>	<b>0.60</b>	<b>0.54</b>	<b>0.53</b>	<b>0.77</b>	IPOP-CMA-ES [15]	
CMA+DE-MOS	1	<b>1.1</b>	<b>1.2</b>	<b>3.5</b>	78	38	<b>15</b>	<b>10</b>	<b>10</b>	<b>4.4</b>	CMA+DE-MOS [13]	
NEWUOA	1	<b>1.7</b>	120	62	62	<i>42e-2/5e3</i>	.	.	.	.	NEWUOA [16]	
Basic RCGA	1	<b>1.5</b>	<b>3.0</b>	<b>5.5</b>	19	<b>26</b>	32	<i>85e-4/5e4</i>	.	.	Basic RCGA [17]	
SPSA	99	281	549	247	338	<i>12e-2/1e5</i>	.	.	.	.	SPSA [9]	

Table 21: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>121 Sum of diff powers Cauchy</b>												
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 0.73	1e+00 14	1e-01 39	1e-02 83	1e-03 233	1e-04 500	1e-05 766	1e-07 1107	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	
(1,2)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>2.7</b>	<b>1.6</b>	<b>1.6</b>	<b>2.4</b>	3.1	<b>2.9</b>	3.9	5.3	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.0	<b>1.1</b>	<b>1.1</b>	<b>1.4</b>	<b>1.7</b>	<b>2.0</b>	<b>2.2</b>	<b>3.0</b>	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.9</b>	<b>1.1</b>	<b>1.1</b>	<b>0.88</b>	<b>1.1</b>	<b>1.4</b>	<b>1.4</b>	<b>1.8</b>	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	<b>1</b>	<b>1.6</b>	<b>2.6</b>	<b>2.7</b>	<b>2.8</b>	7.4	7.3	7.1	12	23	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>1.5</b>	<b>0.78</b>	<b>0.78</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>0.95</b>	<b>1.1</b>	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>1</b>	<b>1.3</b>	3.9	<b>1.2</b>	<b>0.87</b>	<b>1.0</b>	<b>1.0</b>	<b>0.96</b>	<b>0.82</b>	<b>1.0</b>	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>1</b>	<b>1.4</b>	<b>2.3</b>	<b>0.99</b>	<b>0.64</b>	<b>0.66</b>	<b>0.66</b>	<b>0.54</b>	<b>0.52</b>	<b>0.56</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	<b>1</b>	<b>1.5</b>	4.6	<b>1.2</b>	<b>0.82</b>	<b>0.89</b>	<b>0.93</b>	<b>0.80</b>	<b>0.77</b>	<b>0.80</b>	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>1</b>	<b>2.3</b>	<b>2.9</b>	3.5	5.3	27	319	<i>47e-4/5e3</i>	.	.	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	18	34	29	7.9	4.6	266	886	2818	<i>11e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>2.8</b>	<b>1.1</b>	<b>0.92</b>	<b>1.0</b>	<b>0.90</b>	<b>0.80</b>	<b>0.87</b>	<b>0.90</b>	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>1</b>	<b>1.1</b>	4.3	<b>1.3</b>	<b>1.2</b>	<b>1.5</b>	<b>1.6</b>	<b>1.7</b>	<b>1.9</b>	<b>2.6</b>	IPOP-CMA-ES [15]	
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.2</b>	<b>1.4</b>	4.5	4.7	3.2	<b>2.4</b>	<b>2.3</b>	<b>2.6</b>	CMA+DE-MOS [13]	
NEWUOA	<b>1</b>	<b>1.2</b>	3.2	3.6	7.7	43	<i>62e-4/5e3</i>	.	.	.	NEWUOA [16]	
Basic RCGA	<b>1</b>	<b>1.4</b>	<b>1.5</b>	<b>2.6</b>	13	11	37	43	161	<i>19e-6/5e4</i>	Basic RCGA [17]	
SPSA	36	101	278	2723	3628	2262	6233	<i>24e-2/1e5</i>	.	.	SPSA [9]	

Table 22: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{122}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>122 Schaffer F7 Gauss</b>											
$\Delta\text{ftarget}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$
$ERT_{\text{best}}/D$	0.33	0.33	1.9	119	601	1439	2532	3458	4081	6336	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	5.3	7.0	6.8	53	<i>15e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.8</b>	5.1	<b>1.6</b>	5.0	24	<i>21e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.3</b>	6.4	3.1	10	47	<i>35e-3/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.7</b>	10	5.2	56	<i>16e-2/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.3</b>	6.1	3.5	6.1	47	<i>20e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	4.5	<b>1.9</b>	<b>3.6</b>	9.3	<i>85e-4/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.3</b>	3.0	<b>0.74</b>	5.3	11	58	<i>18e-3/1e4</i>	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>2.3</b>	11	5.1	11	103	<i>61e-3/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>2.1</b>	13	22	<i>37e-2/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	29	35	11	4.1	49	147	165	406	<i>52e-3/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.3</b>	<b>2.9</b>	<b>1.4</b>	<b>0.80</b>	<b>0.70</b>	<b>0.67</b>	<b>0.61</b>	<b>0.81</b>	<b>0.90</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.1</b>	<b>1.9</b>	<b>1.1</b>	<b>1.1</b>	<b>0.69</b>	<b>0.76</b>	<b>0.84</b>	<b>0.96</b>	<b>1.1</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.3</b>	<b>1.5</b>	<b>2.7</b>	9.2	15	15	17	<b>22</b>	<b>17</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.1</b>	8.5	21	122	<i>65e-2/5e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1.1</b>	<b>1.1</b>	<b>1.4</b>	7.9	13	<b>8.6</b>	<b>13</b>	<b>16</b>	87	<i>67e-6/5e4</i>	Basic RCGA [17]
SPSA	69	158	103	2636	<i>20e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 23: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{123}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>123 Schaffer F7 unif</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.33	1.6	515	7277	16727	31053	43067	63620	1.47e5	
(1,2)-CMA-ES	<b>1</b>	5.9	29	11	<i>73e-2/1e4</i>	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>2.3</b>	34	7.4	<i>62e-2/1e4</i>	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	20	48	5.0	<i>65e-2/1e4</i>	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.2</b>	49	15	<i>90e-2/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.5</b>	27	7.2	19	<i>34e-2/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.4</b>	<b>4.6</b>	<b>3.1</b>	<i>32e-2/1e4</i>	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.4</b>	30	5.2	<i>45e-2/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	37	82	10	<i>59e-2/1e4</i>	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	12	118	33	<i>16e-1/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	374	549	697	46	<b>17</b>	89	<i>75e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.1</b>	25	<b>2.9</b>	<b>0.56</b>	<b>0.71</b>	<b>0.75</b>	<b>0.75</b>	<b>0.84</b>	<b>0.92</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.4</b>	8.5	<b>1.7</b>	<b>0.90</b>	<b>0.98</b>	<b>0.89</b>	<b>0.82</b>	<b>0.85</b>	<b>1.2</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.3</b>	<b>1.8</b>	171	51	<b>22</b>	<b>16</b>	<b>16</b>	<b>11</b>	<b>4.8</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	12	132	20	<i>12e-1/5e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.2</b>	<b>2.2</b>	13	47	<i>36e-2/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	64	46353	22910	1289	<i>14e-1/1e5</i>	.	.	.	.	.	SPSA [9]



Table 24: 03-D, running time excess  $ERT/ERT_{\text{best}}$  2009 on  $f_{124}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>124 Schaffer F7 Cauchy</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.33	0.33	1.2	65	309	1139	2364	3098	4301	4961	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.4</b>	43	7.4	34	<i>82e-3/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.5</b>	<b>2.3</b>	<b>0.46</b>	<b>2.7</b>	4.1	60	<i>70e-4/1e4</i>	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.6</b>	3.9	<b>2.2</b>	3.7	7.6	<i>73e-4/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.3</b>	6.4	10	78	<i>13e-2/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.9</b>	34	17	8.5	11	60	<i>79e-4/1e4</i>	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>2.8</b>	<b>0.89</b>	<b>2.1</b>	<b>2.9</b>	6.5	46	<i>10e-4/1e4</i>	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.4</b>	3.7	<b>2.4</b>	<b>1.2</b>	<b>1.5</b>	<b>5.7</b>	<i>91e-5/1e4</i>	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>2.1</b>	22	<b>2.6</b>	4.2	5.5	63	<i>45e-4/1e4</i>	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.5</b>	11	7.7	59	<i>18e-2/5e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	15	24	16	6.2	30	103	<i>11e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>2.0</b>	4.2	<b>0.54</b>	<b>0.82</b>	<b>0.50</b>	<b>0.55</b>	<b>0.87</b>	<b>1.2</b>	<b>1.4</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.5</b>	3.2	<b>0.59</b>	<b>2.0</b>	<b>1.1</b>	<b>0.79</b>	<b>0.96</b>	<b>1.5</b>	<b>2.4</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.3</b>	<b>2.4</b>	<b>2.5</b>	27	10	5.8	<b>5.0</b>	<b>5.0</b>	<b>5.0</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.5</b>	5.6	13	36	<i>14e-2/5e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.2</b>	<b>1.8</b>	4.5	22	11	18	50	170	<i>80e-5/5e4</i>	Basic RCGA [17]
SPSA	27	51	6155	2182	4845	<i>11e-1/1e5</i>	.	.	.	.	SPSA [9]

Table 25: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>125 Griewank-Rosenbrock Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.33	0.33	0.33	0.33	1473	8226	11656	12117	12667	
(1,2)-CMA-ES	1	1	1	19	572	6.4	<i>69e-4/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1	<b>8.7</b>	<b>207</b>	3.9	18	13	<i>38e-4/1e4</i>	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	10	289	<b>2.8</b>	18	13	<i>53e-4/1e4</i>	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	<b>1.3</b>	11	791	5.8	<i>68e-4/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1	<b>8.1</b>	677	4.8	8.6	<i>55e-4/1e4</i>	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1	10	508	3.1	8.6	13	12	<i>31e-4/1e4</i>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	<b>8.9</b>	298	<b>2.5</b>	4.0	13	<i>31e-4/1e4</i>	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	1	14	556	5.3	18	<i>69e-4/1e4</i>	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	<b>1.4</b>	9.3	326	<b>1.6</b>	3.0	6.9	6.7	<i>40e-4/6e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	30	38	49	79	569	<b>1.8</b>	21	38	57	115	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	<b>1.3</b>	9.5	289	<b>0.69</b>	<b>0.67</b>	<b>0.70</b>	<b>0.76</b>	<b>0.75</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	<b>1.2</b>	11	<b>243</b>	<b>1.4</b>	<b>1.1</b>	<b>0.98</b>	<b>0.97</b>	<b>0.99</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	<b>1.1</b>	13	<b>222</b>	<b>1.8</b>	4.0	6.3	6.1	<b>5.9</b>	CMA+DE-MOS [13]
NEWUOA	1	1	<b>2.8</b>	10	332	<b>0.88</b>	<b>2.8</b>	<b>2.0</b>	<b>1.9</b>	<i>19e-4/5e3</i>	NEWUOA [16]
Basic RCGA	1	1	<b>1.3</b>	9.3	291	<b>1.0</b>	5.2	8.1	59	<i>54e-5/5e4</i>	Basic RCGA [17]
SPSA	25	38	41	66	21710	14	<i>36e-4/1e5</i>	.	.	.	SPSA [9]

Table 26: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	126 Griewank-Rosenbrock unif										
$\Delta\text{ftarget}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$
$ERT_{\text{best}}/D$	0.33	0.33	0.33	0.33	0.33	4499	37712	1.11e5	2.08e5	3.20e5	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	1.1	135	3640	15	<i>26e-3/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1	87	3050	16	<i>22e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	148	1434	7.1	<i>20e-3/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	1	209	5363	<i>38e-3/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1.2	15	1230	10	<i>18e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1	11	1618	3.4	<i>10e-3/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	6.5	1116	7.3	<i>12e-3/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	32	97	1584	5.4	<i>12e-3/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	1.7	258	6248	<i>49e-3/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	630	728	1797	2592	7997	8.5	4.1	6.1	<i>22e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	1	74	933	<b>0.68</b>	<b>0.89</b>	<b>0.66</b>	<b>0.49</b>	<b>0.49</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	1	15	<b>645</b>	<b>0.85</b>	<b>0.88</b>	<b>0.81</b>	<b>0.95</b>	<b>0.91</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	1.1	16	<b>237</b>	<b>0.11</b>	15	<i>27e-4/1e5</i>	.	.	CMA+DE-MOS [13]
NEWUOA	1	1	13	266	8605	17	<i>48e-3/5e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	1	1	1.1	7.1	<b>350</b>	<b>0.31</b>	<b>0.65</b>	<b>1.1</b>	<b>3.5</b>	<i>15e-5/5e4</i>	Basic RCGA [17]
SPSA	18	46208	75111	2.01e5	3.07e5	159	<i>54e-3/1e5</i>	.	.	.	SPSA [9]

Table 27: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>127 Griewank-Rosenbrock Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 0.33	1e+00 0.33	1e-01 0.33	1e-02 1168	1e-03 13028	1e-04 15016	1e-05 15116	1e-07 15332	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.3</b>	11	367	6.1	<i>76e-4/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	6.9	<b>184</b>	<b>2.1</b>	<b>1.8</b>	4.7	4.6	4.6	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	10	644	3.5	5.5	<i>54e-4/1e4</i>	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	12	644	7.3	11	<i>73e-4/1e4</i>	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>4.8</b>	423	6.0	5.4	10	9.5	9.4	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	9.3	417	3.7	5.4	10	10	10	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>4.7</b>	217	<b>1.5</b>	<b>2.2</b>	<b>2.0</b>	<b>2.0</b>	<b>1.9</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	13	204	4.5	<b>2.3</b>	4.5	4.5	4.4	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>2.1</b>	11	295	4.5	<i>61e-4/5e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	14	24	30	55	224	10	24	94	<i>17e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>6.4</b>	<b>179</b>	3.7	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	14	<b>189</b>	4.3	<b>0.83</b>	<b>1.4</b>	<b>1.5</b>	<b>1.5</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.1</b>	12	190	<b>0.19</b>	<b>1.9</b>	<b>2.7</b>	<b>2.7</b>	<b>2.8</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.1</b>	18	278	<b>1.6</b>	<b>2.3</b>	4.3	4.2	<i>61e-4/4e3</i>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.1</b>	12	293	<b>1.1</b>	<b>2.3</b>	8.3	15	46	Basic RCGA [17]
SPSA	31	47	82	1530	45810	582	<i>22e-3/1e5</i>	.	.	.	SPSA [9]

Table 28: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{128}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>128 Gallagher Gauss</b>												
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.8	1e+00 142	1e-01 375	1e-02 449	1e-03 639	1e-04 903	1e-05 905	1e-07 1447	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	4.7	3.7	<b>2.3</b>	4.7	4.7	6.8	7.1	7.7	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.9</b>	<b>1.6</b>	<b>2.3</b>	<b>2.5</b>	<b>1.8</b>	<b>1.4</b>	<b>1.7</b>	<b>1.1</b>	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.3</b>	<b>2.9</b>	4.0	3.7	3.1	<b>2.3</b>	<b>2.6</b>	<b>1.9</b>	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	3.5	3.1	3.4	5.7	5.0	3.9	3.9	4.3	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.7</b>	<b>2.4</b>	<b>2.5</b>	<b>1.8</b>	<b>1.3</b>	<b>1.3</b>	<b>0.91</b>	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.0</b>	3.3	4.1	4.0	<b>2.8</b>	<b>2.4</b>	<b>2.4</b>	<b>1.9</b>	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	3.6	3.1	3.1	<b>3.6</b>	<b>2.5</b>	<b>1.9</b>	<b>1.9</b>	<b>1.2</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.7</b>	3.1	4.8	4.8	3.7	<b>2.7</b>	<b>2.8</b>	<b>2.4</b>	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>1</b>	<b>1</b>	4.3	10	19	25	18	17	45	<i>45e-3/6e3</i>	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	30	40	12	14	48	84	146	264	471	<i>90e-5/1e5</i>	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	7.3	16	36	26	76	76	48	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>2.2</b>	7.3	12	11	15	11	11	7.3	IPOP-CMA-ES [15]	
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.3</b>	33	52	46	32	24	24	16	CMA+DE-MOS [13]	
NEWUOA	<b>1</b>	<b>1</b>	<b>1.7</b>	7.0	9.1	14	35	84	<i>89e-4/5e3</i>	.	NEWUOA [16]	
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.3</b>	18	33	58	49	35	43	41	Basic RCGA [17]	
SPSA	20	31	150	1406	1931	3251	2283	<i>13e-1/1e5</i>	.	.	SPSA [9]	

Table 29: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{129}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>129 Gallagher unif</b>											
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.6	1e+00 121	1e-01 1131	1e-02 2617	1e-03 3861	1e-04 8261	1e-05 9454	1e-07 12845	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	53	15	5.2	54	<i>23e-3/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	21	13	4.8	17	36	<i>61e-3/1e4</i>	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	31	18	7.9	18	38	<i>27e-3/1e4</i>	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	28	25	11	28	<i>90e-3/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	14	14	<b>4.0</b>	5.7	<b>11</b>	18	15	<i>11e-3/1e4</i>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	5.1	<b>7.3</b>	<b>3.2</b>	<b>5.3</b>	12	<b>8.5</b>	<i>47e-4/1e4</i>	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	10	11	<b>4.5</b>	6.2	37	<i>30e-3/1e4</i>	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	22	<b>11</b>	5.5	7.6	38	18	<i>14e-3/1e4</i>	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	51	34	12	15	21	<b>10</b>	<i>23e-2/6e3</i>	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	181	2286	6231	223	74	45	88	56	157	116	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.4</b>	<b>5.9</b>	5.0	<b>2.8</b>	<b>12</b>	<b>10</b>	<b>9.1</b>	<b>6.9</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	7.5	12	4.7	<b>3.3</b>	<b>6.1</b>	13	<b>11</b>	<b>22</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.4</b>	239	81	72	77	51	45	48	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	56	63	21	30	21	<i>79e-2/5e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.6</b>	11	12	11	24	14	<b>13</b>	<b>27</b>	Basic RCGA [17]
SPSA	54	279	1008	171	308	271	<i>14e-2/1e5</i>	.	.	.	SPSA [9]

Table 30: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>130 Gallagher Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.33	1.8	82	172	305	501	2264	3981	4782	
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.9</b>	38	43	24	15	3.4	<b>2.3</b>	<b>2.0</b>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.7</b>	17	14	<b>7.9</b>	5.5	<b>1.2</b>	<b>0.71</b>	<b>0.60</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	8.1	<b>10</b>	10	5.9	<b>1.7</b>	<b>0.97</b>	<b>0.82</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	4.0	32	53	31	19	5.0	<b>2.8</b>	<b>2.4</b>	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	21	10	13	10	6.0	<b>1.3</b>	<b>0.76</b>	<b>0.64</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.1</b>	11	15	8.6	<b>5.2</b>	<b>1.2</b>	<b>0.67</b>	<b>0.56</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	14	8.5	<b>7.6</b>	<b>5.2</b>	<b>3.2</b>	<b>0.70</b>	<b>0.40</b>	<b>0.34</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>7.7</b>	15	<b>8.4</b>	<b>5.2</b>	<b>1.1</b>	<b>0.65</b>	<b>0.55</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>3.9</b>	12	8.5	11	5.6	5.7	<i>90e-5/5e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	22	37	12	54	155	216	204	131	104	<i>99e-5/1e5</i>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>2.3</b>	19	46	51	57	35	20	17	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	3.1	53	57	33	153	34	19	16	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.8</b>	90	332	398	389	86	87	73	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.0</b>	<b>3.0</b>	<b>9.4</b>	18	21	6.6	17	<i>86e-4/5e3</i>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.3</b>	15	84	132	139	31	23	26	Basic RCGA [17]
SPSA	15	30	103	523	486	574	1367	648	369	<i>51e-3/1e5</i>	SPSA [9]

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