

# Comparison tables: BBOB 2010 noisy testbed with BBOB 2009 as reference

The BBOBies

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## Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2010, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2010>. More than 30 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [11, 7]. The experimental set-up is described in [10].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [6]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [10] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values.

Table 1: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>101 Sphere moderate Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.50	0.50	0.90	4.0	5.0	5.6	7.2	8.4	10	11	
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	3.8	<b>2.5</b>	4.2	6.6	8.1	9.5	10	12	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.8	<b>2.4</b>	4.8	7.4	8.3	8.7	11	12	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>1.4</b>	4.3	7.0	7.3	7.9	8.9	11	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	4.6	3.2	6.5	8.5	14	13	14	15	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	5.0	<b>2.5</b>	5.0	7.0	7.0	7.7	7.9	9.1	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	3.2	<b>1.7</b>	3.3	5.4	6.3	6.6	7.2	8.4	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	3.2	<b>1.6</b>	<b>2.9</b>	<b>4.1</b>	<b>4.8</b>	<b>5.2</b>	<b>5.3</b>	<b>6.2</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	4.6	<b>2.5</b>	3.3	5.2	5.5	6.4	6.0	7.3	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	3.2	<b>1.7</b>	<b>2.1</b>	<b>2.3</b>	<b>2.0</b>	<b>1.9</b>	<b>1.7</b>	<b>1.6</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	10	13	14	9.3	13	19	40	49	92	2502	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	5.2	<b>2.5</b>	3.8	7.7	8.1	8.9	10	12	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	3.6	3.2	5.8	7.5	8.5	9.2	11	12	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.3</b>	3.1	10	22	30	35	38	46	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>1.8</b>	<b>2.1</b>	<b>2.3</b>	<b>2.5</b>	<b>2.3</b>	<b>2.0</b>	<b>1.9</b>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>2.3</b>	3.2	32	62	67	86	111	192	Basic RCGA [17]
SPSA	24	41	173	159	282	907	764	687	631	641	SPSA [9]

Table 2: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>102 Sphere moderate unif</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.50	0.50	0.90	3.5	5.4	8.3	10	11	12	16	
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	5.6	3.2	5.2	5.7	6.6	8.6	9.3	10	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.3	<b>2.7</b>	<b>3.1</b>	4.7	6.7	7.1	7.6	8.7	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	3.2	<b>2.2</b>	4.1	5.1	6.2	6.9	8.0	8.7	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	3.1	<b>2.8</b>	4.0	5.0	7.5	7.6	10	12	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	4.0	<b>2.7</b>	3.9	<b>4.1</b>	5.1	5.4	5.5	6.6	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	4.0	<b>2.3</b>	3.2	4.2	4.8	5.6	6.0	6.6	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	3.1	<b>2.5</b>	<b>2.6</b>	<b>3.0</b>	<b>3.7</b>	<b>3.8</b>	<b>4.3</b>	<b>4.7</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	3.3	<b>2.3</b>	3.2	<b>3.0</b>	<b>3.9</b>	<b>4.1</b>	<b>4.5</b>	5.0	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.2</b>	4.0	<b>2.1</b>	<b>2.6</b>	4.4	<b>4.1</b>	<b>3.7</b>	<b>3.4</b>	<b>2.8</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	13	16	16	7.1	39	36	47	45	705	3827	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	4.1	3.5	5.9	5.8	7.0	7.9	8.2	9.1	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>2.8</b>	3.4	5.6	5.2	5.9	7.4	8.0	8.4	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.3</b>	4.3	11	17	25	26	32	34	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	7.1	11	9.3	7.0	6.6	5.8	5.2	<b>4.4</b>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>2.0</b>	3.3	24	47	56	75	103	146	Basic RCGA [17]
SPSA	9.1	16	27	239	265	255	254	873	870	4083	SPSA [9]

Table 3: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>103 Sphere moderate Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.90	1e+00 3.9	1e-01 4.7	1e-02 4.7	1e-03 4.7	1e-04 4.9	1e-05 4.9	1e-07 6.8	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	3.4	3.3	5.3	9.3	13	17	22	23	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.0	<b>1.9</b>	4.0	8.0	13	16	19	21	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.5</b>	<b>2.0</b>	4.2	8.0	12	15	19	20	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	3.0	3.2	7.3	10	13	16	21	23	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	4.0	<b>2.1</b>	4.4	6.4	9.3	12	15	16	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.8</b>	<b>1.5</b>	3.6	6.2	9.1	11	14	14	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>1.6</b>	<b>2.6</b>	<b>4.8</b>	<b>7.0</b>	<b>8.4</b>	<b>11</b>	<b>11</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	4.3	<b>2.3</b>	3.5	5.4	8.1	10	13	13	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	3.1	<b>1.8</b>	<b>2.1</b>	<b>3.0</b>	<b>4.1</b>	<b>4.4</b>	<b>7.1</b>	<b>6.9</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	12	19	19	6.9	12	19	35	75	82	189	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	3.2	<b>2.4</b>	4.4	8.2	12	16	21	21	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	4.0	3.3	5.7	8.5	14	17	22	23	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>2.6</b>	13	30	51	63	83	94	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	3.2	<b>1.6</b>	<b>2.1</b>	<b>3.1</b>	<b>4.2</b>	<b>4.9</b>	<b>6.4</b>	<b>7.8</b>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.6</b>	3.9	22	52	110	167	268	423	Basic RCGA [17]
SPSA	22	38	369	195	256	375	1471	4060	11338	12346	SPSA [9]

Table 4: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{104}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	104 Rosenbrock moderate Gauss										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.60	2.0	2.7	7.3	97	120	124	126	128	132	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	4.3	4.2	7.5	28	9.3	16	19	20	20	29	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>2.5</b>	4.0	5.8	22	4.9	8.6	10	10	10	11	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	3.2	<b>1.9</b>	4.8	14	4.4	8.5	11	12	12	13	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	11	4.8	9.2	37	11	22	29	57	58	74	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	4.2	3.6	6.6	13	<b>2.8</b>	<b>2.8</b>	3.0	3.2	3.3	3.4	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	4.6	3.2	5.6	18	<b>2.3</b>	<b>2.5</b>	<b>2.6</b>	<b>2.7</b>	<b>2.9</b>	<b>3.0</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>2.6</b>	<b>1.3</b>	<b>2.9</b>	<b>7.5</b>	<b>1.7</b>	<b>1.8</b>	<b>2.0</b>	<b>2.1</b>	<b>2.1</b>	<b>2.3</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>2.8</b>	<b>1.7</b>	<b>3.6</b>	12	<b>2.9</b>	3.8	3.9	4.0	4.0	4.1	(1,4s)-CMA-ES [3]
avg NEWUOA	5.2	<b>2.8</b>	4.3	<b>7.8</b>	<b>1.2</b>	3.5	5.3	6.4	6.8	8.7	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	45	18	20	19	26	72	199	197	305	392	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>2.8</b>	<b>2.2</b>	<b>3.5</b>	<b>5.8</b>	<b>1.2</b>	<b>1.8</b>	<b>2.1</b>	<b>2.3</b>	<b>2.4</b>	<b>2.7</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	5.3	3.2	5.1	15	<b>2.7</b>	3.2	3.9	4.1	4.4	4.6	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.8</b>	<b>2.3</b>	6.6	11	3.1	4.3	5.1	5.8	6.5	7.5	CMA+DE-MOS [13]
NEWUOA	7.3	<b>2.9</b>	6.4	13	3.4	6.5	10	13	12	13	NEWUOA [16]
Basic RCGA	3.2	<b>2.0</b>	7.7	19	34	89	245	514	1709	<i>10e-5/5e4</i>	Basic RCGA [17]
SPSA	611	294	840	1711	4319	<i>39e-2/1e5</i>	.	.	.	.	SPSA [9]

Table 5: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{105}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>105 Rosenbrock moderate unif</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	5.8	4.7	7.3	35	9.3	18	32	54	68	66	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	4.8	3.4	12	17	<b>2.3</b>	8.4	17	35	36	38	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>2.4</b>	<b>1.8</b>	<b>4.3</b>	<b>8.3</b>	3.3	13	22	32	41	40	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	4.7	3.3	12	36	4.4	16	42	119	121	156	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	4.4	4.0	5.6	35	<b>2.9</b>	4.9	6.4	6.4	6.3	6.3	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.7</b>	<b>2.4</b>	<b>4.1</b>	23	<b>1.8</b>	<b>3.6</b>	<b>4.0</b>	<b>4.3</b>	<b>4.3</b>	<b>4.4</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	5.4	<b>2.8</b>	5.6	17	<b>2.6</b>	4.5	5.4	5.9	6.8	6.7	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	3.3	5.8	<b>5.2</b>	24	3.1	6.2	7.3	7.8	7.8	7.7	(1,4s)-CMA-ES [3]
avg NEWUOA	6.4	3.7	7.0	13	<b>2.3</b>	8.6	29	55	196	388	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	50	21	18	17	41	238	959	2211	3364	6907	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	8.3	3.1	6.6	<b>8.3</b>	<b>1.0</b>	<b>1.5</b>	<b>1.9</b>	<b>2.0</b>	<b>2.0</b>	<b>2.2</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	6.5	3.7	5.5	16	<b>2.3</b>	5.4	5.7	5.8	5.9	6.1	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.6</b>	<b>2.3</b>	6.2	<b>7.4</b>	<b>1.6</b>	<b>2.9</b>	<b>3.4</b>	<b>3.7</b>	<b>4.0</b>	<b>4.7</b>	CMA+DE-MOS [13]
NEWUOA	6.3	<b>2.7</b>	7.9	16	3.1	6.3	22	42	41	115	NEWUOA [16]
Basic RCGA	3.3	3.9	8.1	11	13	50	165	465	1153	<i>18e-5/5e4</i>	Basic RCGA [17]
SPSA	519	302	320	1513	1483	8005	<i>34e-2/1e5</i>	.	.	.	SPSA [9]

Table 6: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{106}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>106 Rosenbrock moderate Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	8.0	7.2	28	53	13	9.3	8.4	7.5	6.5	5.1	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	5.1	4.8	6.8	12	4.8	3.8	3.8	3.6	3.3	<b>2.7</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	3.8	3.2	5.4	<b>3.9</b>	4.8	3.1	3.2	<b>3.0</b>	<b>2.6</b>	<b>2.1</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	4.8	3.3	3.9	84	30	21	18	20	18	16	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	5.4	3.2	6.1	11	<b>2.7</b>	<b>1.7</b>	<b>1.6</b>	<b>1.4</b>	<b>1.3</b>	<b>1.1</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.8</b>	<b>1.7</b>	4.2	6.3	<b>2.0</b>	<b>1.4</b>	<b>1.3</b>	<b>1.3</b>	<b>1.1</b>	<b>0.97</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	4.7	3.0	<b>3.0</b>	<b>2.8</b>	<b>1.3</b>	<b>1.1</b>	<b>1.0</b>	<b>1.0</b>	<b>0.91</b>	<b>0.76</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>2.8</b>	<b>1.7</b>	<b>2.6</b>	10	<b>2.9</b>	<b>1.8</b>	<b>1.7</b>	<b>1.5</b>	<b>1.3</b>	<b>1.1</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	4.6	<b>2.2</b>	3.7	<b>4.5</b>	<b>2.1</b>	<b>2.1</b>	3.2	3.3	4.3	5.9	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	54	36	96	91	15	10	8.7	7.7	35	30	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	3.4	3.5	8.3	7.7	<b>2.1</b>	<b>1.7</b>	<b>1.5</b>	<b>1.5</b>	<b>1.4</b>	<b>1.2</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	3.1	<b>2.2</b>	3.9	9.2	3.4	<b>2.6</b>	<b>2.6</b>	<b>2.5</b>	<b>2.3</b>	<b>2.0</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.6</b>	<b>2.2</b>	6.1	13	3.9	3.6	3.7	3.5	3.6	3.3	CMA+DE-MOS [13]
NEWUOA	3.1	<b>2.1</b>	<b>2.6</b>	6.1	<b>2.0</b>	<b>2.3</b>	3.2	3.2	4.8	5.7	NEWUOA [16]
Basic RCGA	<b>2.4</b>	3.2	6.8	12	18	103	308	384	658	2206	Basic RCGA [17]
SPSA	1018	895	2614	6207	3396	10059	<i>40e-2/1e5</i>	.	.	.	SPSA [9]

Table 7: 02-D, running time excess  $ERT/ERT_{\text{best}}$  2009 on  $f_{107}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>107 Sphere Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.90	1e+00 6.6	1e-01 14	1e-02 57	1e-03 79	1e-04 101	1e-05 128	1e-07 211	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	30	14	10	3.9	5.1	7.8	11	13	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	4.4	5.2	4.0	<b>1.8</b>	<b>1.6</b>	<b>1.5</b>	<b>1.5</b>	<b>1.6</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	<b>2.3</b>	<b>2.2</b>	<b>1.9</b>	<b>1.4</b>	<b>1.6</b>	<b>1.9</b>	<b>1.6</b>	<b>2.0</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	5.4	<b>2.4</b>	5.2	6.0	7.2	8.7	7.6	9.1	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	11	3.6	7.7	<b>2.6</b>	<b>2.2</b>	<b>2.1</b>	<b>2.1</b>	<b>1.8</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	7.3	<b>2.2</b>	4.4	<b>1.5</b>	<b>1.3</b>	<b>1.3</b>	<b>1.7</b>	<b>1.4</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	<b>2.1</b>	<b>1.8</b>	<b>1.6</b>	<b>0.66</b>	<b>0.75</b>	<b>0.75</b>	<b>1.4</b>	<b>1.2</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	6.1	11	7.7	<b>2.4</b>	<b>2.5</b>	<b>2.1</b>	<b>2.0</b>	<b>2.0</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	14	32	24	13	15	31	45	80	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	9.2	14	20	6.9	11	3.6	25	84	153	303	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	5.2	<b>2.7</b>	<b>2.7</b>	<b>1.3</b>	<b>1.2</b>	<b>1.2</b>	<b>1.1</b>	<b>0.98</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	5.6	<b>1.9</b>	<b>2.7</b>	<b>1.2</b>	<b>1.1</b>	<b>1.2</b>	<b>1.1</b>	<b>1.00</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	<b>2.5</b>	<b>2.0</b>	6.1	4.5	6.0	5.9	5.7	4.5	CMA+DE-MOS [13]
NEWUOA	1	1	26	20	31	17	20	37	82	83	NEWUOA [16]
Basic RCGA	1	1	<b>1.8</b>	<b>2.0</b>	9.1	8.6	10	8.8	13	20	Basic RCGA [17]
SPSA	16	21	483	1439	3795	4061	3907	14051	<i>27e-3/1e5</i>	.	SPSA [9]

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Table 8: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>108 Sphere unif</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.90	1e+00 15	1e-01 101	1e-02 713	1e-03 1711	1e-04 2608	1e-05 3684	1e-07 7989	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.2</b>	17	13	5.6	3.7	14	<i>26e-4/1e4</i>	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	30	17	8.8	6.5	41	<i>29e-4/1e4</i>	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	30	7.8	5.5	10	38	<i>60e-4/1e4</i>	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	17	12	10	8.9	<i>56e-4/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	49	12	4.1	<b>2.1</b>	7.5	54	38	<i>61e-5/1e4</i>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	86	14	5.8	<b>2.4</b>	4.7	17	<i>50e-5/1e4</i>	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	14	14	6.1	5.7	5.7	17	<i>48e-5/1e4</i>	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	145	26	8.7	3.8	4.8	18	40	<i>51e-5/1e4</i>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	87	42	20	18	16	<i>14e-3/6e3</i>	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	1612	6028	4047	310	143	67	53	61	188	184	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.2</b>	5.7	6.0	<b>3.5</b>	<b>0.82</b>	<b>0.68</b>	<b>0.99</b>	<b>1.0</b>	<b>0.79</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>3.7</b>	<b>3.8</b>	<b>1.6</b>	<b>0.97</b>	<b>0.93</b>	<b>1.0</b>	<b>1.1</b>	<b>0.76</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>1.0</b>	<b>2.3</b>	<b>1.8</b>	<b>1.6</b>	<b>4.1</b>	<b>4.5</b>	<b>3.7</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	121	56	24	22	25	<i>13e-3/6e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>2.3</b>	<b>1.3</b>	12	20	21	28	46	<i>21e-5/5e4</i>	Basic RCGA [17]
SPSA	27	126	204	101	101	88	<i>28e-4/1e5</i>	.	.	.	SPSA [9]

Table 9: 02-D, running time excess  $ERT/ERT_{\text{best}}$  2009 on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>109 Sphere Cauchy</b>												
$\frac{\Delta f_{\text{target}}}{ERT_{\text{best}}/D}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\frac{\Delta f_{\text{target}}}{ERT_{\text{best}}/D}$	
	0.50	0.50	0.90	4.8	6.3	34	34	48	48	48		
(1,2)-CMA-ES	<b>1</b>	<b>1.5</b>	<b>2.5</b>	3.4	4.5	<b>1.5</b>	4.3	3.8	5.1	9.2	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.0</b>	<b>2.8</b>	<b>1.4</b>	<b>2.3</b>	<b>2.3</b>	3.3	5.3	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.7</b>	<b>1.4</b>	<b>2.8</b>	<b>1.1</b>	<b>1.9</b>	<b>1.7</b>	<b>2.3</b>	3.7	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	6.6	3.7	5.0	6.4	9.4	7.4	8.2	15	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	4.3	<b>2.1</b>	3.0	<b>0.97</b>	<b>1.8</b>	<b>1.7</b>	<b>2.5</b>	3.7	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	5.1	<b>2.6</b>	4.0	<b>1.1</b>	<b>1.9</b>	<b>1.8</b>	<b>2.3</b>	<b>3.5</b>	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.5</b>	<b>1.9</b>	<b>3.0</b>	<b>0.96</b>	<b>1.4</b>	<b>1.3</b>	<b>1.8</b>	<b>2.4</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.2</b>	<b>1.4</b>	<b>2.9</b>	<b>0.96</b>	<b>1.7</b>	<b>1.5</b>	<b>1.9</b>	<b>2.6</b>	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>1</b>	<b>1</b>	3.3	<b>2.6</b>	15	7.0	9.0	11	15	31	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	14	21	21	6.9	11	7.0	116	95	889	29122	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	3.2	<b>2.0</b>	3.4	<b>1.2</b>	<b>2.0</b>	<b>2.4</b>	3.1	4.8	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>2.0</b>	<b>1.4</b>	3.8	<b>1.2</b>	<b>2.1</b>	<b>2.2</b>	3.4	5.4	IPOP-CMA-ES [15]	
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.3</b>	<b>2.3</b>	8.6	5.9	8.8	11	14	24	CMA+DE-MOS [13]	
NEWUOA	<b>1</b>	<b>1</b>	3.3	3.6	12	5.6	10	13	22	36	NEWUOA [16]	
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.8</b>	<b>2.5</b>	15	10	19	24	36	67	Basic RCGA [17]	
SPSA	19	32	282	131	273	349	1660	2432	9217	<i>72e-6/1e5</i>	SPSA [9]	

Table 10: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{110}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>110 Rosenbrock Gauss</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.60	2.2	3.6	17	312	651	1159	2181	4204	4577	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	3.4	<b>1.7</b>	23	11	3.4	6.1	6.9	15	34	<i>22e-5/1e4</i>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	15	7.2	7.7	5.7	<b>2.1</b>	3.3	4.4	5.5	4.6	15	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>3.1</b>	3.3	5.2	5.6	<b>1.5</b>	<b>3.2</b>	8.2	8.0	17	32	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	5.3	15	17	18	4.2	4.7	6.3	8.9	7.6	31	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	3.2	<b>2.2</b>	<b>3.7</b>	6.0	4.1	5.9	5.4	4.6	3.5	5.0	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	4.8	<b>3.0</b>	<b>3.2</b>	<b>1.8</b>	<b>1.7</b>	<b>1.7</b>	<b>1.9</b>	<b>1.6</b>	<b>1.1</b>	<b>1.3</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	4.9	<b>2.3</b>	7.3	5.3	<b>2.1</b>	4.4	3.9	4.0	<b>2.6</b>	3.3	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	4.2	<b>2.6</b>	3.9	8.2	<b>2.8</b>	3.3	<b>2.9</b>	<b>2.8</b>	<b>2.8</b>	<b>2.7</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	3.8	10	11	5.1	<b>2.5</b>	<b>3.0</b>	6.8	11	5.9	<i>12e-4/5e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	211	120	89	24	13	201	1238	<i>99e-4/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	3.3	<b>2.3</b>	<b>3.7</b>	<b>3.7</b>	6.1	5.3	3.2	<b>1.7</b>	<b>0.94</b>	<b>0.90</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	7.3	3.6	4.6	8.0	4.2	5.1	<b>3.2</b>	<b>1.9</b>	<b>0.99</b>	<b>0.96</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.6</b>	<b>2.2</b>	6.6	285	16	15	9.1	5.1	<b>2.7</b>	<b>2.6</b>	CMA+DE-MOS [13]
NEWUOA	22	15	16	15	<b>2.9</b>	4.4	9.1	36	<i>19e-4/5e3</i>	.	NEWUOA [16]
Basic RCGA	<b>2.4</b>	<b>2.0</b>	<b>3.1</b>	<b>4.1</b>	5.1	22	33	39	55	157	Basic RCGA [17]
SPSA	531	198	339	832	1381	<i>38e-2/1e5</i>	.	.	.	.	SPSA [9]

Table 11: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{111}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>111 Rosenbrock unif</b>										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.60	3.7	12	59	359	2707	6359	14589	30930	84555	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	18	7.2	5.9	8.5	12	6.2	<i>21e-3/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	3.4	8.2	9.0	3.6	11	26	<i>30e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	20	16	11	8.9	7.3	12	<i>17e-3/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	36	7.8	8.9	10	6.8	12	<i>15e-3/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	62	21	12	4.7	<b>5.5</b>	3.5	<b>5.1</b>	<b>4.9</b>	4.8	<i>61e-4/1e4</i>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	58	15	11	6.7	5.8	<b>2.9</b>	11	<i>47e-4/1e4</i>	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	20	5.4	<b>3.6</b>	4.5	6.3	6.9	11	<i>12e-3/1e4</i>	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	8.7	16	11	7.6	9.2	3.4	7.3	<i>17e-4/1e4</i>	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	72	48	45	29	53	33	<i>26e-2/6e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	570	605	196	64	22	15	33	101	48	<i>22e-4/1e5</i>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	4.6	<b>2.7</b>	7.5	3.3	<b>3.9</b>	<b>3.2</b>	<b>3.9</b>	<b>2.4</b>	<b>1.3</b>	<b>0.51</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>3.3</b>	4.3	5.0	<b>3.3</b>	<b>4.8</b>	<b>2.0</b>	<b>4.3</b>	<b>2.6</b>	<b>1.3</b>	<b>0.55</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.7</b>	<b>1.4</b>	<b>2.0</b>	<b>2.2</b>	44	23	12	6.1	<b>3.3</b>	<b>1.3</b>	CMA+DE-MOS [13]
NEWUOA	137	33	21	25	19	11	<i>68e-3/6e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	<b>2.5</b>	<b>1.1</b>	<b>1.1</b>	<b>1.5</b>	9.1	4.0	5.7	16	24	<i>32e-5/5e4</i>	Basic RCGA [17]
SPSA	73	23	52	152	173	544	<i>51e-3/1e5</i>	.	.	.	SPSA [9]

Table 12: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{112}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>112 Rosenbrock Cauchy</b>												
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$	
$ERT_{\text{best}}/D$	0.60	2.0	2.7	7.3	312	522	577	618	686	766	$ERT_{\text{best}}/D$	
(1,2)-CMA-ES	6.1	4.1	9.2	25	6.2	4.8	5.2	5.7	6.6	6.2	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>2.9</b>	<b>2.5</b>	34	81	3.8	3.4	4.2	4.1	3.9	3.6	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	4.6	3.7	7.8	46	<b>2.1</b>	<b>2.0</b>	<b>2.2</b>	<b>2.2</b>	<b>2.1</b>	<b>2.0</b>	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	12	6.8	8.2	104	8.9	15	24	36	33	56	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	6.4	3.7	5.0	11	<b>0.83</b>	<b>0.93</b>	<b>1.00</b>	<b>1.1</b>	<b>1.0</b>	<b>1.0</b>	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	7.1	3.9	<b>4.5</b>	<b>4.3</b>	<b>0.62</b>	<b>0.72</b>	<b>0.82</b>	<b>0.86</b>	<b>0.83</b>	<b>0.86</b>	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	4.1	<b>2.4</b>	6.3	15	<b>0.88</b>	<b>0.70</b>	<b>0.72</b>	<b>0.72</b>	<b>0.69</b>	<b>0.69</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	3.2	<b>2.3</b>	<b>4.5</b>	12	<b>1.1</b>	<b>0.95</b>	<b>0.97</b>	<b>0.99</b>	<b>0.94</b>	<b>0.91</b>	(1,4s)-CMA-ES [3]	
avg NEWUOA	4.7	<b>2.5</b>	5.1	11	<b>1.1</b>	4.6	22	118	<i>19e-4/5e3</i>	.	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	36	28	27	44	5.0	79	309	<i>12e-4/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	3.1	<b>1.7</b>	4.9	16	<b>1.0</b>	<b>0.88</b>	<b>0.91</b>	<b>0.94</b>	<b>0.90</b>	<b>0.91</b>	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>2.7</b>	<b>2.2</b>	<b>4.0</b>	<b>5.1</b>	<b>0.64</b>	<b>0.92</b>	<b>1.1</b>	<b>1.2</b>	<b>1.1</b>	<b>1.3</b>	IPOP-CMA-ES [15]	
CMA+DE-MOS	<b>2.6</b>	<b>2.3</b>	6.7	11	<b>1.1</b>	<b>1.8</b>	<b>2.1</b>	<b>2.2</b>	<b>2.3</b>	<b>2.7</b>	CMA+DE-MOS [13]	
NEWUOA	5.1	<b>2.7</b>	5.0	13	<b>1.2</b>	<b>1.7</b>	10	112	101	<i>70e-5/5e3</i>	NEWUOA [16]	
Basic RCGA	4.6	3.0	8.9	<b>9.0</b>	4.2	43	85	114	240	447	Basic RCGA [17]	
SPSA	12128	3760	2996	3330	671	2693	2435	<i>21e-2/1e5</i>	.	.	SPSA [9]	

Table 13: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{113}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>113 Step-ellipsoid Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1.9</b>	8.4	8.0	7.3	13	23	34	34	34	12	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>2.3</b>	4.6	4.4	<b>3.9</b>	<b>7.6</b>	<b>7.8</b>	10	10	10	4.0	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>2.8</b>	4.9	4.5	6.6	12	19	22	22	22	5.0	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	14	8.4	10	9.3	14	18	39	39	39	11	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>2.0</b>	<b>2.0</b>	<b>2.9</b>	15	14	13	16	16	16	4.2	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1.8</b>	16	8.8	6.5	12	12	16	16	16	3.5	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	3.4	3.8	3.6	7.0	15	12	<b>10</b>	<b>10</b>	<b>10</b>	<b>2.1</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>2.9</b>	5.6	13	8.4	16	17	14	14	14	4.0	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>2.1</b>	13	10	6.1	<b>10</b>	19	33	33	33	13	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	35	29	17	41	350	978	1184	1184	1184	556	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>2.4</b>	3.0	<b>2.2</b>	10	17	12	14	14	14	<b>2.8</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.3</b>	<b>2.6</b>	3.8	19	15	<b>11</b>	<b>9.4</b>	<b>9.4</b>	<b>9.4</b>	<b>2.4</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.4</b>	<b>2.1</b>	<b>3.1</b>	<b>3.9</b>	<b>6.3</b>	<b>6.9</b>	<b>7.4</b>	<b>7.4</b>	<b>7.4</b>	<b>1.9</b>	CMA+DE-MOS [13]
NEWUOA	<b>2.4</b>	8.7	12	5.8	16	29	42	42	42	14	NEWUOA [16]
Basic RCGA	<b>1.5</b>	<b>1.6</b>	4.7	<b>3.7</b>	85	177	212	212	212	52	Basic RCGA [17]
SPSA	17	18	19	1040	901	3536	2899	2899	2899	761	SPSA [9]

Table 14: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>114 Step-ellipsoid unif</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1.5</b>	28	7.0	15	6.3	9.2	25	25	25	33	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	17	43	14	12	4.6	6.2	6.9	6.9	6.9	<i>32e-4/1e4</i>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	8.8	41	26	19	5.7	6.6	17	17	17	<i>63e-4/1e4</i>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	17	33	12	13	8.3	7.4	7.8	7.8	7.8	16	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.9</b>	43	17	12	<b>3.8</b>	4.1	4.8	4.8	4.8	17	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1.5</b>	19	7.6	15	5.7	6.4	5.1	5.1	5.1	8.0	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	4.5	71	31	20	4.5	<b>3.4</b>	7.0	7.0	7.0	10	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.4</b>	44	14	19	7.1	13	7.6	7.6	7.6	<b>4.7</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1.5</b>	66	29	16	26	21	33	33	33	20	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	618	605	211	197	60	33	21	21	21	45	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1.8</b>	14	8.6	10	<b>2.8</b>	<b>1.7</b>	<b>1.7</b>	<b>1.7</b>	<b>1.7</b>	<b>1.3</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.9</b>	<b>4.2</b>	<b>2.6</b>	<b>5.6</b>	<b>1.6</b>	<b>0.73</b>	<b>0.84</b>	<b>0.84</b>	<b>0.84</b>	<b>0.83</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.4</b>	<b>2.8</b>	<b>1.3</b>	<b>3.8</b>	8.9	4.3	<b>2.2</b>	<b>2.2</b>	<b>2.2</b>	5.0	CMA+DE-MOS [13]
NEWUOA	<b>1.9</b>	41	69	53	38	71	33	33	33	<i>21e-2/6e3</i>	NEWUOA [16]
Basic RCGA	<b>1.8</b>	<b>1.8</b>	<b>1.1</b>	<b>6.3</b>	18	22	20	20	20	17	Basic RCGA [17]
SPSA	99	270	107	184	81	88	118	118	118	<i>63e-4/1e5</i>	SPSA [9]

Table 15: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{115}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	115 Step-ellipsoid Cauchy										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.50	1.0	1.6	6.4	112	180	197	197	197	271	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>2.0</b>	3.8	5.0	7.0	<b>1.8</b>	4.3	6.9	6.9	6.9	19	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.2</b>	<b>2.4</b>	6.2	5.1	<b>1.6</b>	<b>2.3</b>	5.5	5.5	5.5	16	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.9</b>	<b>2.1</b>	5.3	4.9	<b>1.5</b>	<b>2.9</b>	6.0	6.0	6.0	13	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1.7</b>	<b>1.9</b>	5.2	7.3	<b>1.6</b>	7.4	9.1	9.1	9.1	18	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.4</b>	<b>2.2</b>	4.7	<b>4.9</b>	<b>1.1</b>	<b>2.2</b>	<b>2.5</b>	<b>2.5</b>	<b>2.5</b>	3.0	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.3</b>	<b>2.5</b>	<b>3.1</b>	<b>4.9</b>	<b>1.3</b>	<b>2.3</b>	<b>2.2</b>	<b>2.2</b>	<b>2.2</b>	<b>2.4</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1.9</b>	<b>2.2</b>	<b>3.4</b>	5.9	<b>0.91</b>	<b>1.2</b>	<b>2.0</b>	<b>2.0</b>	<b>2.0</b>	<b>1.8</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>2.5</b>	4.3	6.1	<b>3.9</b>	<b>0.89</b>	<b>1.9</b>	<b>2.2</b>	<b>2.2</b>	<b>2.2</b>	<b>2.6</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1.5</b>	<b>2.8</b>	6.5	7.3	<b>2.9</b>	6.1	7.1	7.1	7.1	12	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	14	12	14	18	99	325	551	551	551	1224	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1.3</b>	3.3	<b>3.8</b>	5.4	<b>1.4</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>2.7</b>	4.5	5.2	14	<b>2.2</b>	<b>2.4</b>	<b>2.5</b>	<b>2.5</b>	<b>2.5</b>	<b>2.2</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.4</b>	<b>2.1</b>	4.1	5.6	<b>1.9</b>	<b>2.0</b>	6.3	6.3	6.3	5.3	CMA+DE-MOS [13]
NEWUOA	<b>2.0</b>	<b>2.5</b>	4.5	12	<b>2.9</b>	4.4	11	11	11	11	NEWUOA [16]
Basic RCGA	<b>1.6</b>	<b>1.9</b>	5.2	59	24	101	113	113	113	136	Basic RCGA [17]
SPSA	47	48	110	435	151	268	778	778	778	2416	SPSA [9]



Table 16: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{116}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	116 Ellipsoid Gauss										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	3.3	6.8	25	50	78	103	138	165	521	894	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	12	12	13	23	31	70	102	194	131	160	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>2.0</b>	9.4	22	28	48	128	116	159	64	50	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.4</b>	4.4	11	<b>10</b>	35	69	88	189	135	166	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	13	40	16	26	39	165	<i>12e-3/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.9</b>	<b>2.2</b>	15	20	35	44	42	<b>36</b>	16	9.4	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1.9</b>	<b>2.5</b>	10	25	34	49	48	46	18	12	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>2.8</b>	8.0	15	20	<b>21</b>	<b>34</b>	<b>35</b>	37	14	9.4	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>2.5</b>	<b>2.3</b>	<b>6.4</b>	24	<b>30</b>	49	51	50	19	14	(1,4s)-CMA-ES [3]
avg NEWUOA	7.9	6.2	12	<b>15</b>	32	98	125	479	<i>14e-3/5e3</i>	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	67	132	512	1079	3593	6360	10202	<i>34e-2/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	3.2	<b>2.9</b>	25	22	<b>19</b>	<b>15</b>	<b>14</b>	<b>12</b>	<b>3.9</b>	<b>2.4</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.7</b>	3.8	28	42	36	<b>36</b>	<b>30</b>	<b>26</b>	<b>8.4</b>	<b>5.1</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.2</b>	3.7	33	83	70	56	44	38	<b>13</b>	<b>7.9</b>	CMA+DE-MOS [13]
NEWUOA	5.4	4.6	<b>6.3</b>	<b>18</b>	38	107	571	<i>50e-3/5e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>1.9</b>	4.5	<b>4.6</b>	102	476	859	1611	2102	670	817	Basic RCGA [17]
SPSA	20	19	61	307	1150	4537	10864	<i>43e-3/1e5</i>	.	.	SPSA [9]

Table 17: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{117}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>117 Ellipsoid unif</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	4.8	17	84	673	3227	6957	14112	14949	18210	21616	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	9.2	8.6	8.9	6.0	5.6	<i>12e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	6.6	7.5	8.0	5.4	5.7	21	11	<i>11e-2/1e4</i>	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	8.8	7.7	10	<b>3.7</b>	6.9	<i>14e-2/1e4</i>	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	10	8.4	9.4	8.6	13	<i>31e-2/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	11	9.3	10	3.8	<b>2.0</b>	10	<i>36e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	14	6.2	7.3	<b>3.3</b>	6.0	10	<i>12e-2/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	15	13	10	4.6	3.3	6.0	10	<i>59e-3/1e4</i>	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	7.9	8.7	<b>4.8</b>	4.5	<b>2.7</b>	<b>3.9</b>	11	<i>33e-3/1e4</i>	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	15	32	24	10	8.4	<i>78e-2/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	50	112	115	32	62	103	103	<i>17e-2/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	5.5	5.5	<b>5.0</b>	<b>3.6</b>	<b>1.8</b>	<b>0.99</b>	<b>0.67</b>	<b>0.67</b>	<b>0.61</b>	<b>0.63</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>3.2</b>	<b>4.8</b>	10	4.5	<b>2.0</b>	<b>1.5</b>	<b>0.95</b>	<b>0.96</b>	<b>0.95</b>	<b>0.93</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.1</b>	<b>1.2</b>	<b>1.6</b>	3.7	4.2	4.3	<b>2.4</b>	<b>2.6</b>	<b>2.4</b>	<b>2.9</b>	CMA+DE-MOS [13]
NEWUOA	43	25	29	12	26	<i>97e-2/6e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1.7</b>	<b>1.6</b>	5.9	22	15	13	11	<i>73e-3/5e4</i>	.	.	Basic RCGA [17]
SPSA	58	41	80	129	131	214	105	<i>35e-2/1e5</i>	.	.	SPSA [9]

Table 18: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>118 Ellipsoid Cauchy</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	2.1	2.5	10	52	66	252	292	326	388	486	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	7.5	12	55	19	18	5.4	5.1	5.5	5.1	4.6	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>2.6</b>	5.5	45	18	17	4.7	4.3	4.0	3.6	3.2	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	4.4	11	20	8.4	7.7	<b>2.8</b>	<b>2.7</b>	<b>2.7</b>	<b>2.4</b>	<b>2.1</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	3.2	14	131	52	64	24	25	23	20	16	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	3.6	6.6	12	4.7	4.1	<b>1.4</b>	<b>1.3</b>	<b>1.2</b>	<b>1.1</b>	<b>1.0</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	3.7	6.6	9.1	3.5	3.9	<b>1.2</b>	<b>1.1</b>	<b>1.2</b>	<b>1.0</b>	<b>1.0</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	3.6	7.3	5.9	<b>2.0</b>	<b>2.2</b>	<b>0.68</b>	<b>0.65</b>	<b>0.65</b>	<b>0.60</b>	<b>0.56</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>2.4</b>	<b>3.9</b>	<b>4.8</b>	<b>2.8</b>	<b>3.2</b>	<b>0.93</b>	<b>0.93</b>	<b>0.91</b>	<b>0.82</b>	<b>0.72</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>2.4</b>	<b>2.3</b>	<b>2.8</b>	3.8	12	9.0	21	221	<i>90e-5/5e3</i>	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	42	142	61	44	533	615	1377	1231	3617	2888	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	3.0	8.1	7.9	<b>3.4</b>	<b>3.7</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	3.8	6.5	12	4.8	5.7	<b>2.4</b>	<b>2.5</b>	<b>2.4</b>	<b>2.2</b>	<b>1.9</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.5</b>	10	8.6	4.8	6.0	<b>2.0</b>	<b>2.2</b>	<b>2.5</b>	<b>2.5</b>	<b>2.9</b>	CMA+DE-MOS [13]
NEWUOA	<b>2.1</b>	<b>2.6</b>	<b>5.6</b>	4.2	11	10	35	71	187	<i>11e-4/5e3</i>	NEWUOA [16]
Basic RCGA	4.0	5.4	76	100	462	253	280	1078	907	<i>16e-3/5e4</i>	Basic RCGA [17]
SPSA	61	400	1210	755	4425	5579	<i>20e-2/1e5</i>	.	.	.	SPSA [9]

Table 19: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{119}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	119 Sum of diff powers Gauss										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.70	1e+00 5.4	1e-01 36	1e-02 88	1e-03 520	1e-04 950	1e-05 2384	1e-07 5041	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>2.5</b>	4.0	6.4	6.7	3.9	7.4	7.7	29	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>2.0</b>	3.1	8.4	4.0	<b>2.8</b>	<b>1.2</b>	<b>2.2</b>	3.3	14	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.2</b>	<b>2.0</b>	5.4	<b>2.8</b>	<b>2.4</b>	<b>2.1</b>	3.1	<b>2.9</b>	8.7	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.6</b>	<b>2.2</b>	4.9	4.4	7.0	4.8	15	61	<i>90e-6/1e4</i>	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>2.1</b>	3.3	4.0	3.9	<b>1.9</b>	<b>1.1</b>	<b>1.5</b>	<b>1.9</b>	8.8	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>2.1</b>	6.8	<b>2.3</b>	<b>1.5</b>	<b>1.5</b>	<b>2.0</b>	<b>1.6</b>	6.1	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.9</b>	<b>3.0</b>	5.6	<b>1.4</b>	<b>1.6</b>	<b>0.70</b>	<b>1.3</b>	<b>1.3</b>	14	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1.4</b>	<b>3.0</b>	13	3.6	3.1	<b>1.0</b>	<b>2.2</b>	<b>2.1</b>	9.0	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.4</b>	<b>2.9</b>	18	8.0	14	5.9	6.6	6.8	<i>67e-6/5e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	12	20	17	<b>3.7</b>	<b>1.8</b>	13	81	83	183	<i>34e-6/1e5</i>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.1</b>	<b>1.7</b>	6.6	<b>1.7</b>	<b>1.3</b>	<b>0.78</b>	<b>1.6</b>	<b>1.0</b>	<b>0.76</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.7</b>	3.8	7.9	<b>2.2</b>	<b>1.5</b>	<b>1.1</b>	<b>2.5</b>	<b>1.6</b>	<b>1.9</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.2</b>	<b>1.9</b>	<b>2.8</b>	5.1	5.7	<b>1.5</b>	<b>1.2</b>	<b>0.67</b>	<b>0.55</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>2.6</b>	3.1	15	8.6	23	7.1	19	33	15	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.2</b>	<b>1.4</b>	<b>2.2</b>	3.2	8.8	4.5	11	10	19	Basic RCGA [17]
SPSA	15	32	35	933	1158	2645	838	<i>21e-3/1e5</i>	.	.	SPSA [9]

Table 20: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	120 Sum of diff powers unif										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.70	1e+00 5.7	1e-01 187	1e-02 1257	1e-03 2862	1e-04 12965	1e-05 37703	1e-07 94320	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.7</b>	19	34	6.0	7.5	<i>76e-4/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.1</b>	19	19	4.7	14	<i>12e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>2.9</b>	22	19	4.9	8.2	<i>52e-4/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.1</b>	12	33	9.3	13	52	<i>15e-3/1e4</i>	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>2.6</b>	41	4.4	7.4	<b>15</b>	<i>56e-4/1e4</i>	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.5</b>	36	26	5.0	<b>4.3</b>	49	<i>25e-4/1e4</i>	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.5</b>	17	26	4.9	4.3	<i>54e-4/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.6</b>	9.5	3.9	7.9	<i>79e-4/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	9.5	37	74	42	15	<i>94e-3/6e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	423	709	620	222	37	66	247	<i>53e-4/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.2</b>	<b>2.0</b>	<b>8.7</b>	<b>2.4</b>	<b>0.94</b>	<b>1.1</b>	<b>0.68</b>	<b>0.53</b>	<b>0.56</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.5</b>	3.5	23	<b>3.5</b>	<b>1.5</b>	<b>1.5</b>	<b>0.78</b>	<b>0.45</b>	<b>0.64</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.3</b>	<b>1.9</b>	<b>4.5</b>	<b>3.0</b>	4.4	16	<b>11</b>	<b>4.1</b>	<b>5.7</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	3.1	48	61	41	34	<i>98e-3/6e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.3</b>	<b>2.0</b>	<b>1.6</b>	6.8	13	19	16	19	<i>31e-5/5e4</i>	Basic RCGA [17]
SPSA	57	173	152	151	107	254	<i>13e-3/1e5</i>	.	.	.	SPSA [9]

Table 21: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>121 Sum of diff powers Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.70	1e+00 3.5	1e-01 21	1e-02 72	1e-03 164	1e-04 376	1e-05 560	1e-07 851	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.6</b>	<b>2.3</b>	3.8	<b>2.5</b>	4.1	6.6	5.9	7.5	10	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>2.2</b>	<b>2.5</b>	<b>2.0</b>	<b>1.1</b>	<b>1.5</b>	<b>2.9</b>	3.5	4.9	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>2.5</b>	3.4	<b>1.0</b>	<b>1.1</b>	<b>1.3</b>	<b>1.7</b>	<b>2.2</b>	<b>2.7</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.3</b>	4.1	5.0	<b>1.8</b>	3.4	16	18	30	84	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.2</b>	3.1	3.2	<b>1.5</b>	<b>0.99</b>	<b>0.92</b>	<b>0.85</b>	<b>1.1</b>	<b>1.4</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.5</b>	<b>2.9</b>	3.2	<b>1.6</b>	<b>1.3</b>	<b>1.3</b>	<b>1.4</b>	<b>1.3</b>	<b>1.4</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.2</b>	<b>2.2</b>	<b>2.0</b>	<b>0.97</b>	<b>0.68</b>	<b>0.70</b>	<b>0.72</b>	<b>0.71</b>	<b>0.71</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1.7</b>	<b>2.7</b>	<b>2.8</b>	<b>1.1</b>	<b>0.78</b>	<b>0.69</b>	<b>0.72</b>	<b>0.73</b>	<b>0.79</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.6</b>	<b>2.6</b>	5.7	4.4	6.3	22	35	<i>31e-5/5e3</i>	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	15	25	22	31	10	10	61	339	2516	<i>13e-5/1e5</i>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.3</b>	<b>2.7</b>	3.1	<b>1.4</b>	<b>1.2</b>	<b>1.3</b>	<b>1.1</b>	<b>1.2</b>	<b>1.4</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>2.0</b>	4.1	3.7	<b>1.6</b>	<b>1.0</b>	<b>1.6</b>	<b>2.0</b>	<b>2.2</b>	<b>2.6</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.2</b>	<b>2.1</b>	4.1	5.7	3.8	3.9	<b>2.9</b>	<b>2.9</b>	3.3	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.6</b>	<b>2.7</b>	4.4	3.0	7.6	14	57	121	<i>40e-5/5e3</i>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.3</b>	<b>1.7</b>	<b>2.0</b>	8.0	6.2	14	15	37	104	Basic RCGA [17]
SPSA	33	60	126	806	2749	1758	1936	<i>13e-3/1e5</i>	.	.	SPSA [9]

Table 22: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{122}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>122 Schaffer F7 Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.50	0.50	1.5	48	261	705	1122	1676	2176	4781	
(1,2)-CMA-ES	<b>1</b>	<b>2.9</b>	14	5.0	4.8	12	61	<i>53e-4/1e4</i>	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>2.3</b>	<b>3.3</b>	<b>1.6</b>	4.9	10	19	32	<i>98e-5/1e4</i>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.7</b>	12	3.7	3.1	4.1	38	<i>32e-4/1e4</i>	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.6</b>	23	4.2	7.0	22	<i>16e-3/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.3</b>	5.7	5.9	3.3	3.1	4.7	14	32	<i>23e-5/1e4</i>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.1</b>	4.7	3.8	<b>2.5</b>	<b>2.8</b>	<b>3.3</b>	6.0	7.6	31	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.4</b>	31	<b>2.2</b>	<b>2.1</b>	<b>2.4</b>	5.9	14	20	<i>38e-5/1e4</i>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1.9</b>	36	4.4	5.7	7.3	20	27	67	<i>32e-4/1e4</i>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.3</b>	14	10	33	55	<i>11e-2/5e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	12	16	16	21	37	91	195	<i>53e-4/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.3</b>	3.5	<b>1.2</b>	<b>0.81</b>	<b>0.78</b>	<b>0.75</b>	<b>0.69</b>	<b>0.90</b>	<b>0.60</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.3</b>	29	3.9	<b>2.5</b>	<b>1.2</b>	<b>1.1</b>	<b>1.00</b>	<b>0.98</b>	<b>0.74</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.4</b>	<b>2.1</b>	30	21	10	7.5	<b>5.8</b>	<b>5.1</b>	<b>2.9</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.7</b>	10	16	30	54	<i>99e-3/5e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>2.2</b>	10	22	14	21	25	45	<i>25e-6/5e4</i>	Basic RCGA [17]
SPSA	21	38	60	803	<i>44e-2/1e5</i>	.	.	.	.	.	SPSA [9]

Table 23: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{123}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>123 Schaffer F7 unif</b>											
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.8</b>	26	7.1	47	<i>24e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.2</b>	<b>2.8</b>	18	<b>4.8</b>	7.2	<i>13e-2/1e4</i>	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.1</b>	6.1	30	7.5	45	<i>23e-2/1e4</i>	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.2</b>	48	10	22	<i>18e-2/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.8</b>	21	8.6	<b>3.5</b>	<i>83e-3/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>7.3</b>	<b>4.7</b>	11	<i>13e-2/1e4</i>	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>2.0</b>	29	6.3	4.4	<b>12</b>	<i>98e-3/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>2.8</b>	78	6.8	11	<i>11e-2/1e4</i>	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	10	66	24	28	<i>46e-2/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	261	1354	557	126	20	25	<i>48e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>2.0</b>	19	5.7	<b>0.88</b>	<b>0.54</b>	<b>0.71</b>	<b>0.81</b>	<b>0.67</b>	<b>0.82</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.6</b>	18	<b>3.7</b>	<b>0.74</b>	<b>0.69</b>	<b>1.0</b>	<b>0.90</b>	<b>0.75</b>	<b>0.72</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.5</b>	<b>1.9</b>	40	39	18	<b>15</b>	<b>11</b>	<b>7.9</b>	<b>5.2</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	56	32	28	<i>44e-2/6e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.5</b>	<b>2.9</b>	21	23	<i>11e-2/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	32	64	137	76	221	<i>22e-2/1e5</i>	.	.	.	.	SPSA [9]



Table 24: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{124}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	124 Schaffer F7 Cauchy										
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 1.8	1e+00 32	1e-01 158	1e-02 340	1e-03 996	1e-04 1737	1e-05 2798	1e-07 4510	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>2.1</b>	3.9	13	14	26	69	<i>60e-4/1e4</i>	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.8</b>	<b>3.0</b>	3.4	<b>1.9</b>	4.5	12	<i>98e-5/1e4</i>	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.9</b>	3.1	<b>2.8</b>	4.5	5.5	8.4	82	<i>89e-5/1e4</i>	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.7</b>	15	12	13	44	<i>16e-3/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	3.9	3.3	7.8	4.5	6.4	8.0	25	<i>23e-5/1e4</i>	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.4</b>	3.2	4.5	<b>1.4</b>	<b>2.7</b>	3.2	10	50	<i>23e-5/1e4</i>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.8</b>	26	5.1	<b>1.8</b>	<b>1.6</b>	<b>1.7</b>	11	51	<i>23e-5/1e4</i>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.1</b>	<b>1.5</b>	<b>1.8</b>	10	4.6	5.0	8.0	85	<i>42e-5/1e4</i>	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.7</b>	12	9.3	22	61	<i>98e-3/5e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	14	20	36	11	38	142	226	814	<i>19e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.8</b>	<b>2.2</b>	<b>1.0</b>	<b>0.89</b>	<b>1.5</b>	<b>1.1</b>	<b>1.1</b>	<b>1.5</b>	<b>2.0</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.4</b>	3.5	<b>1.2</b>	<b>0.69</b>	<b>0.81</b>	<b>1.3</b>	<b>1.4</b>	<b>2.0</b>	<b>2.5</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.5</b>	<b>1.9</b>	3.1	15	20	10	<b>6.2</b>	<b>7.8</b>	<b>7.4</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>2.2</b>	5.6	6.5	14	46	<i>33e-3/5e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	<b>1.2</b>	3.0	23	25	33	56	130	<i>19e-5/5e4</i>	Basic RCGA [17]
SPSA	48	90	4547	844	468	2050	<i>37e-3/1e5</i>	.	.	.	SPSA [9]

Table 25: 02-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>125 Griewank-Rosenbrock Gauss</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.50	1e+00 0.50	1e-01 0.50	1e-02 74	1e-03 575	1e-04 1228	1e-05 1927	1e-07 3778	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	5.6	14	105	4.4	4.1	4.0	6.1	<i>63e-7/1e4</i>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	5.8	54	<b>1.6</b>	<b>2.8</b>	3.1	5.5	12	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>3.9</b>	<b>34</b>	<b>2.6</b>	3.4	4.4	7.0	18	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	11	137	3.2	5.5	4.4	7.6	38	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>4.5</b>	<b>25</b>	<b>1.9</b>	5.7	5.2	7.9	12	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	5.9	49	<b>2.5</b>	4.0	3.5	3.8	4.1	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	5.5	61	3.1	3.4	<b>2.1</b>	3.1	6.5	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	5.2	<b>31</b>	<b>1.8</b>	6.1	6.0	6.2	18	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>2.3</b>	6.9	46	<b>1.8</b>	<b>2.7</b>	<b>2.4</b>	<b>2.3</b>	6.2	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	14	20	25	34	87	5.0	5.4	6.8	14	40	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	<b>4.7</b>	53	<b>1.4</b>	<b>1.5</b>	<b>1.0</b>	<b>1.4</b>	<b>0.94</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	5.9	34	<b>2.1</b>	<b>2.0</b>	<b>1.3</b>	<b>1.9</b>	<b>1.4</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.1</b>	5.8	44	<b>1.2</b>	<b>0.47</b>	3.3	<b>2.2</b>	<b>1.2</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.0</b>	6.1	77	<b>1.4</b>	<b>2.6</b>	<b>2.1</b>	<b>2.6</b>	10	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.2</b>	6.4	58	<b>1.9</b>	<b>2.7</b>	4.7	5.0	13	Basic RCGA [17]
SPSA	22	32	37	61	169	<b>2.2</b>	98	230	344	<i>45e-5/1e5</i>	SPSA [9]

Table 26: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>126 Griewank-Rosenbrock unif</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.50	1e+00 0.50	1e-01 0.50	1e-02 151	1e-03 1709	1e-04 3408	1e-05 5528	1e-07 18193	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.3</b>	53	300	7.2	6.8	20	26	<i>75e-5/1e4</i>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	<b>4.2</b>	141	6.3	4.8	6.0	8.0	<i>23e-5/1e4</i>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>3.5</b>	236	4.0	8.9	7.9	27	<i>81e-5/1e4</i>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	39	246	9.1	8.5	12	25	<i>12e-4/1e4</i>	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	6.3	336	4.4	3.6	9.0	12	7.7	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	7.4	111	3.3	3.9	3.8	5.6	<i>64e-6/1e4</i>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	41	113	<b>2.3</b>	3.1	3.6	5.5	8.0	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	12	256	3.4	4.8	4.7	<i>18e-5/1e4</i>	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	26	95	667	15	11	7.8	<i>18e-4/6e3</i>	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	284	472	608	704	1604	57	22	40	37	<i>32e-6/1e5</i>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	4.5	230	<b>1.9</b>	<b>1.4</b>	<b>1.0</b>	<b>0.97</b>	<b>1.5</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>4.2</b>	<b>73</b>	<b>1.9</b>	<b>1.1</b>	<b>2.0</b>	<b>2.2</b>	<b>1.6</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.1</b>	<b>3.9</b>	<b>49</b>	<b>0.58</b>	12	18	20	19	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.1</b>	200	595	15	52	<i>32e-4/6e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.1</b>	4.6	<b>47</b>	<b>0.72</b>	<b>0.98</b>	<b>1.3</b>	<b>1.4</b>	<b>2.0</b>	Basic RCGA [17]
SPSA	16	50	86	193	1851	88	111	95	80	<i>18e-4/1e5</i>	SPSA [9]

Table 27: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>127 Griewank-Rosenbrock Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.50	1e+00 0.50	1e-01 0.50	1e-02 93	1e-03 593	1e-04 2014	1e-05 3386	1e-07 3638	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	10	53	<b>2.5</b>	5.1	<b>2.8</b>	<b>2.7</b>	4.9	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	6.4	39	<b>1.2</b>	<b>2.0</b>	<b>0.95</b>	<b>0.86</b>	<b>1.6</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	4.9	33	<b>1.1</b>	<b>2.7</b>	<b>1.6</b>	<b>1.4</b>	<b>1.6</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	11	86	<b>2.5</b>	8.2	3.6	3.7	19	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>3.5</b>	<b>17</b>	<b>2.7</b>	3.5	<b>2.1</b>	<b>1.3</b>	<b>1.6</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	4.3	<b>21</b>	<b>2.6</b>	3.0	<b>1.7</b>	<b>1.4</b>	<b>1.4</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	4.3	<b>21</b>	<b>2.7</b>	<b>2.7</b>	<b>1.2</b>	<b>0.81</b>	<b>0.97</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>3.3</b>	82	<b>2.1</b>	<b>2.4</b>	<b>0.94</b>	<b>0.72</b>	<b>0.69</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>1.3</b>	7.2	72	<b>1.6</b>	3.5	<b>1.8</b>	<b>2.5</b>	<i>16e-6/5e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	12	17	19	28	70	<b>1.6</b>	<b>2.2</b>	4.6	12	66	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.4</b>	6.1	39	<b>2.5</b>	<b>2.7</b>	<b>1.1</b>	<b>0.77</b>	<b>0.85</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	4.2	78	<b>1.2</b>	<b>1.7</b>	<b>1.0</b>	<b>0.72</b>	<b>1.6</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.1</b>	3.9	31	<b>0.89</b>	<b>0.88</b>	<b>1.5</b>	<b>2.6</b>	3.5	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.1</b>	6.2	95	<b>1.8</b>	4.9	3.8	<b>2.8</b>	9.0	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.2</b>	<b>3.7</b>	41	<b>1.4</b>	4.0	<b>2.6</b>	<b>2.5</b>	29	Basic RCGA [17]
SPSA	26	39	94	636	4930	125	181	165	<i>40e-5/1e5</i>	.	SPSA [9]

Table 28: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{128}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>128 Gallagher Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.50	1e+02 0.50	1e+01 0.90	1e+00 21	1e-01 67	1e-02 157	1e-03 194	1e-04 205	1e-05 297	1e-07 310	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	4.1	10	9.4	6.2	6.9	7.2	5.6	6.8	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	<b>0.93</b>	<b>5.6</b>	<b>6.1</b>	5.3	6.2	5.9	4.6	5.7	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	<b>1.7</b>	<b>2.7</b>	<b>3.7</b>	<b>3.9</b>	<b>4.8</b>	<b>5.7</b>	<b>4.5</b>	4.7	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	7.3	8.8	<b>5.5</b>	<b>3.9</b>	7.1	10	10	11	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	<b>1.7</b>	21	14	6.4	6.9	6.6	4.6	<b>4.5</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	<b>2.1</b>	12	12	7.1	6.1	<b>5.8</b>	<b>4.0</b>	<b>4.4</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	<b>1.8</b>	14	10	<b>4.2</b>	<b>3.6</b>	<b>3.7</b>	<b>2.6</b>	<b>2.5</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	<b>1.2</b>	6.7	10	5.9	<b>5.2</b>	7.2	5.6	5.4	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	<b>2.9</b>	21	9.3	7.9	7.4	8.7	10	32	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	13	19	15	16	44	20	48	76	244	563	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	<b>2.0</b>	26	16	7.8	11	19	13	14	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	<b>0.78</b>	9.4	11	8.9	7.3	7.3	5.2	5.2	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	<b>1.4</b>	35	84	50	41	40	28	29	CMA+DE-MOS [13]
NEWUOA	1	1	<b>1.9</b>	17	10	10	10	16	14	20	NEWUOA [16]
Basic RCGA	1	1	<b>1.1</b>	<b>1.8</b>	18	16	30	66	57	149	Basic RCGA [17]
SPSA	10	22	35	309	656	812	2220	2096	<i>83e-4/1e5</i>	.	SPSA [9]

Table 29: 02-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{129}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>129 Gallagher unif</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.50	0.50	0.90	33	110	261	951	1622	2972	5330	
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	9.3	8.2	13	13	10	17	16	27	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.8</b>	11	10	7.6	4.7	15	48	<i>12e-5/1e4</i>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.3</b>	11	11	11	3.9	12	8.3	27	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	18	8.5	<b>6.5</b>	11	8.6	6.3	10	<i>60e-6/1e4</i>	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.3</b>	8.1	8.9	8.3	3.8	<b>4.6</b>	<b>3.3</b>	<b>6.4</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.7</b>	<b>7.0</b>	<b>5.7</b>	<b>4.3</b>	<b>3.0</b>	<b>4.9</b>	<b>3.7</b>	8.5	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.6</b>	11	9.2	<b>5.0</b>	4.3	5.2	5.6	13	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>0.81</b>	7.6	<b>5.6</b>	7.3	<b>3.6</b>	5.0	11	<i>31e-6/1e4</i>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	52	25	31	27	9.4	25	29	16	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	288	439	273	92	53	95	39	69	56	274	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.6</b>	13	13	<b>6.5</b>	<b>2.2</b>	<b>2.4</b>	<b>3.2</b>	<b>5.4</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1.7</b>	7.4	12	9.3	5.6	8.2	4.7	<b>3.2</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.4</b>	<b>1.4</b>	13	49	28	20	11	6.9	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	24	23	21	26	19	25	31	<i>37e-4/6e3</i>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>0.85</b>	<b>0.64</b>	13	15	13	11	24	135	Basic RCGA [17]
SPSA	5.1	48	96	100	66	108	55	81	150	<i>86e-6/1e5</i>	SPSA [9]

Table 30: 02-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>130 Gallagher Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.0</b>	40	33	18	13	6.2	7.8	3.2	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.4</b>	30	16	8.8	5.7	<b>2.8</b>	<b>2.7</b>	<b>1.1</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.5</b>	14	15	11	7.2	4.5	4.2	<b>1.8</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	41	54	32	20	10	10	4.3	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.0</b>	22	13	6.2	4.5	<b>2.2</b>	<b>2.0</b>	<b>0.84</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	15	10	7.0	4.6	<b>2.3</b>	<b>2.2</b>	<b>0.89</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.4</b>	<b>6.5</b>	8.8	<b>5.2</b>	<b>3.3</b>	<b>1.6</b>	<b>1.9</b>	<b>0.76</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.3</b>	9.0	13	5.3	<b>3.4</b>	<b>1.6</b>	<b>1.5</b>	<b>0.63</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	3.2	8.2	<b>3.7</b>	<b>2.6</b>	<b>3.6</b>	3.9	7.5	6.9	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	8.8	12	11	7.8	22	18	30	71	130	127	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.5</b>	6.6	6.5	39	26	13	12	33	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	8.3	18	8.7	5.8	3.1	<b>3.0</b>	<b>1.2</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.7</b>	<b>1.1</b>	<b>0.97</b>	10	24	20	18	15	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.8</b>	10	<b>5.4</b>	<b>3.7</b>	3.8	3.6	4.7	6.6	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>2.0</b>	<b>1.1</b>	8.5	21	37	45	63	76	Basic RCGA [17]
SPSA	22	34	84	662	510	298	243	285	486	311	SPSA [9]

Table 31: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>101 Sphere moderate Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.2	1e+00 4.4	1e-01 6.3	1e-02 6.7	1e-03 9.3	1e-04 11	1e-05 11	1e-07 13	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	5.6	4.9	7.3	12	10	10	12	13	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.6</b>	<b>2.8</b>	6.0	7.7	7.6	8.3	9.3	11	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.2</b>	4.7	3.1	5.7	7.0	6.4	7.3	8.5	10	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	6.9	5.3	7.4	10	10	11	12	14	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	3.6	<b>3.0</b>	4.2	5.9	5.5	6.2	7.4	8.2	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.9</b>	3.6	5.2	5.1	5.7	6.4	7.4	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	3.3	<b>2.6</b>	<b>3.1</b>	<b>4.1</b>	<b>3.9</b>	<b>4.2</b>	<b>4.9</b>	<b>5.5</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	3.6	3.2	3.6	5.0	4.5	4.8	5.5	6.5	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>2.1</b>	3.4	<b>1.6</b>	<b>1.7</b>	<b>1.9</b>	<b>1.5</b>	<b>1.4</b>	<b>1.4</b>	<b>1.4</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	14	21	16	12	112	384	484	694	1414	1256	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	4.0	3.8	5.0	7.6	7.2	7.9	9.2	11	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	3.8	3.0	5.1	7.5	7.2	8.1	9.3	11	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	10	21	28	28	30	36	42	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.5</b>	<b>2.8</b>	<b>2.0</b>	<b>2.5</b>	<b>2.9</b>	<b>2.4</b>	<b>2.2</b>	<b>2.3</b>	<b>2.2</b>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	<b>2.4</b>	10	36	73	88	132	182	315	Basic RCGA [17]
SPSA	30	46	198	295	846	1989	1524	1398	1375	3664	SPSA [9]



Table 32: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>102 Sphere moderate unif</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.2	1e+00 4.0	1e-01 7.6	1e-02 9.3	1e-03 11	1e-04 12	1e-05 13	1e-07 16	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	5.6	5.6	5.9	7.2	8.1	9.5	11	11	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.3	3.9	4.6	5.4	6.2	7.1	7.6	8.6	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	3.1	3.1	4.1	4.9	5.4	6.5	7.1	7.6	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	4.3	5.8	5.3	7.4	8.1	8.9	8.6	14	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	3.2	<b>2.7</b>	<b>2.9</b>	3.6	4.3	5.1	5.6	6.0	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	4.2	3.3	3.3	4.0	4.7	5.2	5.7	6.0	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.2</b>	<b>2.2</b>	<b>3.1</b>	<b>3.4</b>	<b>3.9</b>	<b>4.1</b>	<b>4.5</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	3.0	<b>2.6</b>	<b>2.5</b>	<b>3.4</b>	<b>3.9</b>	<b>4.3</b>	<b>4.6</b>	<b>5.1</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.9</b>	3.6	<b>2.8</b>	<b>2.9</b>	<b>2.6</b>	<b>2.8</b>	<b>2.7</b>	<b>2.5</b>	<b>2.2</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	28	45	21	14	15	19	21	149	1947	4298	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	4.2	3.9	4.1	5.3	6.4	7.2	7.7	8.5	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	4.4	4.2	4.4	5.6	6.7	7.8	8.4	8.8	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	11	17	21	25	29	30	34	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.5</b>	5.9	5.7	5.4	7.2	6.8	8.1	9.1	10	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	<b>1.7</b>	17	29	43	77	115	167	242	Basic RCGA [17]
SPSA	24	38	470	396	697	2079	2142	2293	5383	87971	SPSA [9]

Table 33: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>103 Sphere moderate Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.2	1e+00 4.3	1e-01 6.4	1e-02 6.4	1e-03 6.4	1e-04 6.6	1e-05 7.7	1e-07 14	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	6.2	5.1	6.7	10	14	18	19	14	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.5</b>	<b>2.8</b>	4.5	7.5	10	12	13	10	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.7</b>	3.0	4.4	7.2	8.7	11	12	9.1	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	3.9	4.3	5.2	7.7	12	15	17	13	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	4.0	3.5	4.0	6.1	7.8	10	11	8.5	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.5</b>	<b>2.1</b>	3.9	5.8	7.8	9.4	10	<b>7.3</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.9</b>	<b>2.0</b>	<b>2.6</b>	<b>4.1</b>	<b>5.1</b>	<b>6.8</b>	<b>6.9</b>	<b>5.3</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	3.8	<b>2.3</b>	3.3	5.0	6.7	<b>8.5</b>	<b>8.0</b>	<b>6.1</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.9</b>	3.3	<b>1.7</b>	<b>1.6</b>	<b>2.0</b>	<b>5.6</b>	9.2	10	9.0	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	17	30	19	16	22	27	34	1298	2202	2619	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>2.9</b>	4.6	7.8	10	13	13	10	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	4.0	3.5	4.8	7.9	11	14	14	11	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	11	20	31	42	53	62	51	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	3.4	<b>2.1</b>	<b>2.6</b>	<b>3.4</b>	<b>4.8</b>	<b>5.9</b>	<b>5.8</b>	10	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	<b>2.3</b>	13	39	69	140	225	281	291	Basic RCGA [17]
SPSA	40	142	360	216	228	400	565	1216	4576	11577	SPSA [9]





Table 36: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{106}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>106 Rosenbrock moderate Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	5.2	3.6	4.0	11	12	5.8	4.1	4.1	<b>2.7</b>	<b>2.6</b>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	3.1	<b>2.0</b>	3.8	13	10	4.3	<b>2.8</b>	<b>2.8</b>	<b>1.9</b>	<b>1.8</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	3.0	<b>2.3</b>	4.1	8.3	6.5	<b>2.9</b>	<b>2.0</b>	<b>2.0</b>	<b>1.3</b>	<b>1.3</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	12	9.2	10	40	29	13	8.8	8.8	5.7	5.3	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	5.3	<b>2.6</b>	3.1	9.5	6.6	<b>2.8</b>	<b>1.9</b>	<b>1.8</b>	<b>1.2</b>	<b>1.1</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.8</b>	<b>1.6</b>	3.3	9.0	6.1	<b>2.6</b>	<b>1.7</b>	<b>1.6</b>	<b>1.1</b>	<b>1.0</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>2.7</b>	<b>1.2</b>	<b>2.1</b>	5.0	<b>3.8</b>	<b>1.6</b>	<b>1.1</b>	<b>1.0</b>	<b>0.69</b>	<b>0.67</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	3.3	<b>1.4</b>	<b>2.3</b>	7.3	5.4	<b>2.3</b>	<b>1.5</b>	<b>1.5</b>	<b>0.98</b>	<b>0.92</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	3.1	<b>1.1</b>	<b>1.1</b>	<b>2.4</b>	<b>1.9</b>	<b>1.0</b>	<b>2.1</b>	3.3	5.0	7.5	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	40	17	17	40	24	10	7.1	7.0	4.8	5.4	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>2.8</b>	<b>1.5</b>	<b>2.7</b>	<b>3.7</b>	<b>4.3</b>	<b>2.0</b>	<b>1.3</b>	<b>1.3</b>	<b>0.90</b>	<b>0.90</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	3.2	<b>2.3</b>	3.3	5.1	6.5	3.1	<b>2.1</b>	<b>2.1</b>	<b>1.4</b>	<b>1.4</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	3.4	3.9	10	8.6	10	4.8	3.0	3.2	<b>2.2</b>	<b>2.4</b>	CMA+DE-MOS [13]
NEWUOA	3.0	<b>0.95</b>	<b>1.0</b>	<b>3.3</b>	5.6	4.4	7.4	14	13	33	NEWUOA [16]
Basic RCGA	3.2	4.6	14	145	911	1110	2842	<i>43e-3/5e4</i>	.	.	Basic RCGA [17]
SPSA	1188	595	815	9052	<i>19e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 37: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{107}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>107 Sphere Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 2.0	1e+00 16	1e-01 51	1e-02 77	1e-03 108	1e-04 138	1e-05 168	1e-07 228	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	22	12	10	22	27	45	203	<i>28e-6/1e4</i>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	7.4	<b>1.9</b>	<b>1.9</b>	<b>2.1</b>	<b>2.1</b>	<b>2.7</b>	3.2	4.1	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	7.0	<b>2.2</b>	<b>2.2</b>	3.5	4.7	4.6	7.3	8.2	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	5.9	8.4	13	17	48	115	95	642	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	8.9	3.4	<b>2.9</b>	3.3	3.5	4.4	6.2	5.8	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	3.7	<b>1.2</b>	<b>0.71</b>	<b>0.82</b>	<b>0.96</b>	<b>1.2</b>	<b>1.1</b>	<b>1.5</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.1</b>	14	<b>2.5</b>	<b>1.2</b>	<b>1.6</b>	<b>1.6</b>	<b>1.9</b>	3.1	4.2	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	<b>2.2</b>	<b>1.5</b>	3.7	3.3	3.9	4.4	10	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	17	20	45	115	360	592	<i>16e-3/6e3</i>	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	24	37	13	5.0	6.1	14	49	226	555	6150	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>2.0</b>	5.4	<b>1.4</b>	<b>0.99</b>	<b>0.97</b>	<b>0.96</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1.7</b>	<b>1.2</b>	<b>0.80</b>	<b>0.96</b>	<b>1.0</b>	<b>0.95</b>	<b>0.98</b>	<b>1.0</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.6</b>	3.3	5.3	7.2	7.2	7.2	7.2	7.0	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.1</b>	12	29	61	65	150	532	<i>57e-4/5e3</i>	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.6</b>	7.8	9.2	11	13	20	26	31	Basic RCGA [17]
SPSA	36	53	199	8554	13692	18097	13131	<i>11e-1/1e5</i>	.	.	SPSA [9]

Table 38: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>108 Sphere unif</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.9	1e+00 33	1e-01 655	1e-02 1842	1e-03 3608	1e-04 5060	1e-05 5729	1e-07 10727	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	34	29	53	<i>15e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	23	24	25	13	37	<i>84e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	54	25	23	81	<i>10e-2/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	30	41	19	79	<i>88e-3/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.1</b>	30	<b>10</b>	6.0	38	<i>42e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	30	19	<b>5.9</b>	<b>14</b>	<i>18e-3/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>10</b>	14	9.3	38	<i>38e-3/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	35	20	8.6	77	<i>39e-3/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.5</b>	121	82	126	<i>39e-2/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	1294	1758	2673	269	44	25	<b>17</b>	<b>25</b>	<b>44</b>	68	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	14	<b>8.4</b>	<b>1.8</b>	<b>1.1</b>	<b>0.96</b>	<b>0.80</b>	<b>1.1</b>	<b>0.81</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.1</b>	97	11	<b>1.3</b>	<b>1.0</b>	<b>0.89</b>	<b>0.92</b>	<b>1.1</b>	<b>1.0</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.6</b>	66	138	91	61	49	45	<b>29</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	108	56	36	<i>41e-2/5e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>2.1</b>	<b>10</b>	24	20	22	33	129	<i>18e-4/5e4</i>	Basic RCGA [17]
SPSA	111	264	275	166	58	390	<i>28e-3/1e5</i>	.	.	.	SPSA [9]

Table 39: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>109 Sphere Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.33	1.2	6.8	31	48	64	65	84	84	
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	5.4	3.5	<b>2.0</b>	<b>1.9</b>	<b>2.8</b>	3.6	3.9	6.8	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.9	<b>2.9</b>	<b>1.3</b>	<b>1.6</b>	<b>1.7</b>	<b>2.3</b>	<b>2.4</b>	3.7	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	3.5	<b>1.8</b>	<b>0.83</b>	<b>0.96</b>	<b>1.1</b>	<b>1.4</b>	<b>1.5</b>	<b>2.4</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	8.9	7.6	<b>2.5</b>	3.1	3.5	4.5	6.1	8.3	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>1.9</b>	<b>0.92</b>	<b>1.1</b>	<b>1.2</b>	<b>1.8</b>	<b>1.7</b>	3.0	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	4.1	<b>2.0</b>	<b>1.1</b>	<b>1.2</b>	<b>1.3</b>	<b>1.8</b>	<b>1.7</b>	<b>2.6</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.1</b>	<b>1.3</b>	<b>0.66</b>	<b>0.72</b>	<b>0.72</b>	<b>0.99</b>	<b>0.94</b>	<b>1.3</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.2</b>	<b>1.6</b>	<b>0.75</b>	<b>0.84</b>	<b>0.90</b>	<b>1.2</b>	<b>1.2</b>	<b>1.8</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.5</b>	3.4	7.6	5.9	8.9	17	58	112	262	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	15	30	21	9.5	4.4	33	403	3363	<i>20e-5/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.6</b>	<b>1.3</b>	<b>1.4</b>	<b>1.6</b>	<b>2.0</b>	<b>2.1</b>	3.1	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	4.5	<b>2.3</b>	<b>1.2</b>	<b>1.3</b>	<b>1.7</b>	<b>2.3</b>	<b>2.4</b>	3.6	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	6.1	4.2	5.6	6.4	10	12	16	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.3</b>	5.3	6.2	6.4	12	34	146	181	<i>17e-5/5e3</i>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	3.4	11	11	14	20	27	33	51	Basic RCGA [17]
SPSA	37	157	448	231	1467	1620	3769	6888	<i>43e-4/1e5</i>	.	SPSA [9]







Table 42: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{112}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>112 Rosenbrock Cauchy</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	1.4	7.2	10	113	523	826	950	993	1035	1178	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	7.7	7.6	17	28	10	8.7	8.0	7.8	8.5	7.8	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>3.0</b>	<b>2.6</b>	3.3	5.8	<b>2.5</b>	<b>2.0</b>	<b>1.9</b>	<b>2.0</b>	<b>2.0</b>	<b>1.9</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	5.1	<b>2.2</b>	3.5	5.1	<b>1.7</b>	<b>1.4</b>	<b>1.4</b>	<b>1.4</b>	<b>1.4</b>	<b>1.3</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	4.5	4.4	8.7	27	12	16	17	21	31	28	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>2.9</b>	<b>1.4</b>	<b>2.2</b>	<b>1.3</b>	<b>0.95</b>	<b>0.88</b>	<b>0.88</b>	<b>0.93</b>	<b>0.93</b>	<b>0.89</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>3.0</b>	<b>1.3</b>	<b>2.3</b>	3.1	<b>1.1</b>	<b>0.90</b>	<b>0.87</b>	<b>0.87</b>	<b>0.86</b>	<b>0.83</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>2.9</b>	<b>1.2</b>	<b>1.9</b>	<b>2.1</b>	<b>0.76</b>	<b>0.58</b>	<b>0.56</b>	<b>0.56</b>	<b>0.56</b>	<b>0.52</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	3.1	<b>1.6</b>	<b>2.7</b>	4.6	<b>1.5</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>2.8</b>	<b>0.93</b>	<b>2.1</b>	<b>2.2</b>	<b>1.8</b>	10	85	<i>20e-3/6e3</i>	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	57	24	23	306	571	1699	<i>26e-2/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	3.0	<b>1.8</b>	3.8	<b>1.6</b>	<b>0.79</b>	<b>0.70</b>	<b>0.72</b>	<b>0.74</b>	<b>0.76</b>	<b>0.76</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	4.2	<b>2.3</b>	3.7	4.6	<b>1.8</b>	<b>1.5</b>	<b>1.5</b>	<b>1.5</b>	<b>1.5</b>	<b>1.5</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	3.4	4.0	10	<b>2.4</b>	<b>1.9</b>	<b>1.6</b>	<b>1.6</b>	<b>1.8</b>	<b>1.9</b>	<b>2.0</b>	CMA+DE-MOS [13]
NEWUOA	<b>2.0</b>	<b>0.89</b>	<b>1.3</b>	<b>1.7</b>	<b>1.4</b>	8.7	37	73	<i>44e-4/5e3</i>	.	NEWUOA [16]
Basic RCGA	<b>2.7</b>	3.6	11	18	72	93	365	713	<i>23e-3/5e4</i>	.	Basic RCGA [17]
SPSA	1314	1782	2830	12462	<i>29e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 43: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{113}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	113 Step-ellipsoid Gauss										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>2.5</b>	11	6.6	11	<b>2.6</b>	6.0	11	11	11	15	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.4</b>	<b>1.3</b>	<b>2.6</b>	<b>4.1</b>	<b>0.84</b>	<b>2.9</b>	4.1	4.1	4.1	6.4	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.2</b>	<b>2.4</b>	8.6	7.4	<b>1.3</b>	<b>1.8</b>	7.3	7.3	7.3	13	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>2.7</b>	24	12	8.7	3.6	18	41	41	41	125	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.6</b>	<b>3.0</b>	4.2	4.9	<b>2.0</b>	<b>2.3</b>	3.5	3.5	3.5	3.8	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.1</b>	<b>2.5</b>	<b>1.1</b>	5.7	<b>1.9</b>	<b>2.6</b>	3.4	3.4	3.4	3.4	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1.3</b>	4.4	6.3	4.9	<b>1.6</b>	<b>2.7</b>	<b>2.8</b>	<b>2.8</b>	<b>2.8</b>	<b>3.2</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.3</b>	<b>2.8</b>	<b>2.4</b>	<b>4.6</b>	<b>1.7</b>	<b>2.2</b>	3.3	3.3	3.3	5.8	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1.6</b>	5.6	8.2	15	8.0	25	75	75	75	<i>57e-3/6e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	28	14	22	19	82	292	392	392	392	1280	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	20	8.4	<b>2.0</b>	7.7	<b>0.88</b>	<b>0.60</b>	<b>0.77</b>	<b>0.77</b>	<b>0.77</b>	<b>0.75</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.7</b>	<b>2.7</b>	<b>1.8</b>	6.6	<b>1.9</b>	<b>1.8</b>	<b>1.8</b>	<b>1.8</b>	<b>1.8</b>	<b>1.8</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.1</b>	<b>1.7</b>	<b>1.3</b>	<b>4.1</b>	3.4	3.4	3.5	3.5	3.5	3.5	CMA+DE-MOS [13]
NEWUOA	<b>1.5</b>	14	7.7	14	5.1	12	70	70	70	<i>74e-3/5e3</i>	NEWUOA [16]
Basic RCGA	<b>1.1</b>	<b>1.6</b>	<b>2.1</b>	11	19	39	38	38	38	38	Basic RCGA [17]
SPSA	40	24	18	1660	1007	1374	<i>71e-2/1e5</i>	.	.	.	SPSA [9]

Table 44: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>114 Step-ellipsoid unif</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.98	8.5	338	2093	6295	9441	9441	9441	10860	
(1,2)-CMA-ES	<b>1.1</b>	5.1	34	11	21	<i>31e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.1</b>	8.2	17	6.9	21	<i>30e-2/1e4</i>	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.1</b>	63	32	22	23	<i>22e-2/1e4</i>	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1.1</b>	35	30	12	<i>52e-2/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.3</b>	67	21	3.6	7.6	23	<i>11e-2/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1.8</b>	<b>2.2</b>	<b>6.7</b>	<b>2.5</b>	<b>5.7</b>	<b>10</b>	15	15	15	<i>83e-3/1e4</i>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1.8</b>	27	25	4.0	12	<i>16e-2/1e4</i>	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	17	14	19	6.4	10	<i>22e-2/1e4</i>	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	143	104	26	<i>11e-1/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	877	2294	553	127	148	<i>14e-2/1e5</i>	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1.4</b>	34	25	<b>1.4</b>	<b>0.88</b>	<b>0.61</b>	<b>0.42</b>	<b>0.42</b>	<b>0.42</b>	<b>0.39</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.1</b>	12	7.1	<b>2.4</b>	<b>1.6</b>	<b>0.81</b>	<b>0.60</b>	<b>0.60</b>	<b>0.60</b>	<b>0.59</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.1</b>	<b>1.9</b>	<b>1.9</b>	9.3	31	20	13	13	13	<b>14</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	50	71	31	<i>11e-1/5e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1.5</b>	<b>1.8</b>	<b>1.6</b>	8.0	12	14	<b>12</b>	<b>12</b>	<b>12</b>	20	Basic RCGA [17]
SPSA	271	204	223	63	685	<i>29e-2/1e5</i>	.	.	.	.	SPSA [9]

Table 45: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{115}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	115 Step-ellipsoid Cauchy										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1.7</b>	3.2	4.9	<b>2.7</b>	7.9	41	63	63	63	<i>54e-4/1e4</i>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.5</b>	<b>2.1</b>	<b>1.7</b>	<b>2.1</b>	<b>2.8</b>	5.8	12	12	12	21	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.1</b>	<b>1.5</b>	<b>2.9</b>	<b>1.4</b>	<b>1.6</b>	5.0	13	13	13	39	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1.5</b>	3.8	4.3	3.4	3.4	23	50	50	50	169	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.5</b>	3.6	<b>2.9</b>	<b>1.4</b>	<b>1.6</b>	<b>2.8</b>	4.3	4.3	4.3	6.5	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1.4</b>	<b>2.9</b>	<b>2.7</b>	<b>0.88</b>	<b>1.3</b>	<b>1.4</b>	3.4	3.4	3.4	4.1	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1.1</b>	<b>1.4</b>	<b>2.1</b>	<b>1.2</b>	<b>0.87</b>	<b>1.4</b>	<b>1.6</b>	<b>1.6</b>	<b>1.6</b>	<b>2.1</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.1</b>	<b>1.9</b>	4.5	<b>1.9</b>	<b>1.6</b>	<b>2.5</b>	3.1	3.1	3.1	5.3	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1.5</b>	3.1	<b>1.1</b>	<b>2.6</b>	4.9	19	45	45	45	59	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	24	17	20	122	392	1637	4763	4763	4763	3402	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1.2</b>	<b>2.7</b>	<b>2.0</b>	<b>0.88</b>	<b>0.91</b>	<b>0.80</b>	<b>0.90</b>	<b>0.90</b>	<b>0.90</b>	<b>0.78</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.7</b>	3.2	6.4	<b>2.4</b>	<b>1.8</b>	<b>2.4</b>	<b>2.4</b>	<b>2.4</b>	<b>2.4</b>	<b>1.9</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.1</b>	<b>2.0</b>	<b>2.3</b>	<b>2.1</b>	5.0	7.4	7.6	7.6	7.6	5.6	CMA+DE-MOS [13]
NEWUOA	<b>2.4</b>	<b>2.8</b>	<b>0.96</b>	4.0	8.3	66	215	215	215	154	NEWUOA [16]
Basic RCGA	<b>1.1</b>	<b>0.95</b>	6.1	56	96	145	138	138	138	129	Basic RCGA [17]
SPSA	52	44	49	576	560	1532	<i>43e-3/1e5</i>	.	.	.	SPSA [9]

Table 46: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{116}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>116 Ellipsoid Gauss</b>											
$\Delta\text{ftarget}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$
$ERT_{\text{best}}/D$	6.2	25	56	881	1473	2051	2381	3153	3205	3790	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	14	14	17	9.4	96	<i>68e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	6.3	11	14	4.0	8.4	10	14	10	46	<i>54e-3/1e4</i>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	11	12	27	5.6	6.8	34	<i>45e-3/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	14	36	40	13	46	34	63	<i>61e-2/1e4</i>	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>2.4</b>	<b>2.3</b>	12	3.8	11	15	18	15	15	19	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	4.6	<b>5.9</b>	10	3.1	4.3	4.9	5.4	7.6	14	12	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	11	8.9	11	<b>1.8</b>	4.0	4.5	5.5	7.9	10	<i>96e-5/1e4</i>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	17	7.0	<b>8.2</b>	<b>2.2</b>	3.9	7.1	13	14	<i>18e-3/1e4</i>	.	(1,4s)-CMA-ES [3]
avg NEWUOA	19	24	65	28	<i>30e-1/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	1443	1318	1980	1701	<i>97e-1/1e5</i>	.	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	6.8	6.2	<b>5.9</b>	<b>1.3</b>	<b>1.2</b>	<b>1.0</b>	<b>0.90</b>	<b>0.71</b>	<b>0.71</b>	<b>0.63</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	4.5	7.4	11	<b>2.8</b>	<b>2.5</b>	<b>2.1</b>	<b>1.9</b>	<b>1.5</b>	<b>1.5</b>	<b>1.3</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>2.2</b>	<b>2.8</b>	<b>7.3</b>	4.4	<b>3.0</b>	<b>2.4</b>	<b>2.2</b>	<b>1.9</b>	<b>2.0</b>	<b>1.9</b>	CMA+DE-MOS [13]
NEWUOA	12	18	45	41	50	<i>49e-1/5e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>2.6</b>	18	61	26	52	65	<i>67e-3/5e4</i>	.	.	.	Basic RCGA [17]
SPSA	98	863	4071	1622	<i>20e+0/1e5</i>	.	.	.	.	.	SPSA [9]





Table 48: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>118 Ellipsoid Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	11	18	9.4	15	7.2	6.5	6.1	5.8	5.6	6.5	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	4.1	8.8	4.2	7.5	3.4	3.4	3.3	<b>3.0</b>	3.0	<b>2.7</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	4.0	7.4	5.5	5.5	<b>2.0</b>	<b>1.8</b>	<b>2.0</b>	<b>1.9</b>	<b>1.8</b>	<b>1.6</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	6.9	13	30	46	23	24	27	23	21	20	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	4.1	6.5	<b>2.6</b>	3.2	<b>1.3</b>	<b>1.3</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.5</b>	6.8	3.2	3.5	<b>1.2</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>0.99</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>2.4</b>	<b>3.4</b>	<b>2.0</b>	<b>2.3</b>	<b>0.92</b>	<b>0.83</b>	<b>0.78</b>	<b>0.71</b>	<b>0.71</b>	<b>0.66</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.6</b>	6.0	3.3	<b>3.0</b>	<b>1.1</b>	<b>1.0</b>	<b>0.93</b>	<b>0.85</b>	<b>0.82</b>	<b>0.75</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>0.98</b>	<b>1.4</b>	<b>1.0</b>	5.0	5.4	26	77	<i>43e-4/6e3</i>	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	38	81	715	2979	2747	4936	<i>21e-1/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	3.3	4.9	3.4	<b>3.0</b>	<b>1.0</b>	<b>0.98</b>	<b>0.95</b>	<b>0.89</b>	<b>0.94</b>	<b>0.94</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	4.3	7.9	6.2	6.7	<b>2.6</b>	<b>2.4</b>	<b>2.2</b>	<b>2.0</b>	<b>2.0</b>	<b>1.9</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	3.3	10	6.0	5.2	<b>1.9</b>	<b>2.0</b>	<b>2.3</b>	<b>2.5</b>	<b>2.8</b>	3.1	CMA+DE-MOS [13]
NEWUOA	<b>1.3</b>	<b>1.4</b>	<b>1.7</b>	3.7	6.5	43	109	<i>19e-3/5e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>2.3</b>	78	142	542	672	1269	2227	<i>75e-2/5e4</i>	.	.	Basic RCGA [17]
SPSA	126	254	1406	6641	<i>41e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 49: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{119}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	119 Sum of diff powers Gauss										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 0.73	1e+00 22	1e-01 140	1e-02 203	1e-03 668	1e-04 1894	1e-05 4013	1e-07 5240	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.3</b>	6.6	4.3	5.3	17	48	<i>24e-4/1e4</i>	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	4.8	3.2	<b>1.7</b>	4.2	3.2	8.2	17	<i>14e-5/1e4</i>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>2.2</b>	<b>1.5</b>	<b>1.4</b>	<b>2.9</b>	4.5	35	<i>18e-5/1e4</i>	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.1</b>	28	6.9	3.7	39	110	<i>50e-4/1e4</i>	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>2.1</b>	9.2	4.3	<b>1.5</b>	<b>3.0</b>	<b>2.4</b>	4.1	18	<i>63e-6/1e4</i>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.3</b>	4.7	3.2	<b>0.92</b>	<b>1.5</b>	<b>2.3</b>	3.0	3.9	28	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.8</b>	12	<b>1.7</b>	<b>0.96</b>	<b>1.8</b>	<b>2.6</b>	<b>2.9</b>	6.1	<i>48e-6/1e4</i>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	3.7	43	3.7	<b>2.0</b>	3.2	4.9	9.3	35	<i>18e-5/1e4</i>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	23	8.2	16	51	<i>13e-3/6e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	24	36	25	24	25	136	193	367	<i>11e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>2.1</b>	5.5	<b>1.1</b>	<b>0.55</b>	<b>0.92</b>	<b>0.77</b>	<b>0.87</b>	<b>0.72</b>	<b>0.79</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.9</b>	8.4	<b>0.93</b>	<b>0.38</b>	<b>0.69</b>	<b>0.91</b>	<b>1.2</b>	<b>1.0</b>	<b>1.7</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.2</b>	<b>1.2</b>	<b>2.6</b>	4.6	<b>2.1</b>	<b>1.0</b>	<b>0.68</b>	<b>1.0</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>2.2</b>	13	18	27	116	114	<i>31e-3/5e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.3</b>	<b>2.4</b>	6.6	6.2	7.6	9.3	8.9	24	<i>17e-6/5e4</i>	Basic RCGA [17]
SPSA	35	55	187	5891	10571	7294	<i>10e-1/1e5</i>	.	.	.	SPSA [9]

Table 50: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	120 Sum of diff powers unif											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 0.73	1e+00 27	1e-01 601	1e-02 2312	1e-03 10645	1e-04 25282	1e-05 40067	1e-07 88603	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	
(1,2)-CMA-ES	1	41	43	31	31	<i>11e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	1	4.0	58	<b>7.8</b>	15	<i>54e-3/1e4</i>	.	.	.	.	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	1	<b>1.1</b>	65	31	29	63	<i>14e-2/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	1	<b>1.3</b>	22	37	28	29	<i>13e-2/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	1	3.1	9.0	11	13	62	<i>71e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	1	<b>1.4</b>	27	12	<b>7.1</b>	<i>44e-3/1e4</i>	.	.	.	.	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	1	<b>1.7</b>	<b>5.3</b>	17	10	61	<i>31e-3/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	1	<b>1</b>	54	18	14	<i>51e-3/1e4</i>	.	.	.	.	(1,4s)-CMA-ES [3]	
avg NEWUOA	1	24	120	66	40	<i>36e-2/6e3</i>	.	.	.	.	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	779	1826	2111	847	151	74	43	58	<i>11e-3/1e5</i>	.	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	1	<b>2.2</b>	14	8.3	<b>1.9</b>	<b>1.6</b>	<b>0.66</b>	<b>0.49</b>	<b>0.57</b>	<b>0.50</b>	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	1	<b>1.3</b>	8.6	11	<b>1.9</b>	<b>0.97</b>	<b>0.60</b>	<b>0.54</b>	<b>0.53</b>	<b>0.77</b>	IPOP-CMA-ES [15]	
CMA+DE-MOS	1	<b>1.1</b>	<b>1.2</b>	<b>3.5</b>	78	38	<b>15</b>	<b>10</b>	<b>10</b>	<b>4.4</b>	CMA+DE-MOS [13]	
NEWUOA	1	<b>1.7</b>	120	62	62	<i>42e-2/5e3</i>	.	.	.	.	NEWUOA [16]	
Basic RCGA	1	<b>1.5</b>	<b>3.0</b>	<b>5.5</b>	19	<b>26</b>	32	<i>85e-4/5e4</i>	.	.	Basic RCGA [17]	
SPSA	99	281	549	247	338	<i>12e-2/1e5</i>	.	.	.	.	SPSA [9]	

Table 51: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>121 Sum of diff powers Cauchy</b>												
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 0.73	1e+00 14	1e-01 39	1e-02 83	1e-03 233	1e-04 500	1e-05 766	1e-07 1107	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	
(1,2)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>2.7</b>	<b>1.6</b>	<b>1.6</b>	<b>2.4</b>	3.1	<b>2.9</b>	3.9	5.3	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	3.0	<b>1.1</b>	<b>1.1</b>	<b>1.4</b>	<b>1.7</b>	<b>2.0</b>	<b>2.2</b>	<b>3.0</b>	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.9</b>	<b>1.1</b>	<b>1.1</b>	<b>0.88</b>	<b>1.1</b>	<b>1.4</b>	<b>1.4</b>	<b>1.8</b>	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	<b>1</b>	<b>1.6</b>	<b>2.6</b>	<b>2.7</b>	<b>2.8</b>	7.4	7.3	7.1	12	23	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>1.5</b>	<b>0.78</b>	<b>0.78</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>0.95</b>	<b>1.1</b>	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>1</b>	<b>1.3</b>	3.9	<b>1.2</b>	<b>0.87</b>	<b>1.0</b>	<b>1.0</b>	<b>0.96</b>	<b>0.82</b>	<b>1.0</b>	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>1</b>	<b>1.4</b>	<b>2.3</b>	<b>0.99</b>	<b>0.64</b>	<b>0.66</b>	<b>0.66</b>	<b>0.54</b>	<b>0.52</b>	<b>0.56</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	<b>1</b>	<b>1.5</b>	4.6	<b>1.2</b>	<b>0.82</b>	<b>0.89</b>	<b>0.93</b>	<b>0.80</b>	<b>0.77</b>	<b>0.80</b>	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>1</b>	<b>2.3</b>	<b>2.9</b>	3.5	5.3	27	319	<i>47e-4/5e3</i>	.	.	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	18	34	29	7.9	4.6	266	886	2818	<i>11e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>2.8</b>	<b>1.1</b>	<b>0.92</b>	<b>1.0</b>	<b>0.90</b>	<b>0.80</b>	<b>0.87</b>	<b>0.90</b>	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>1</b>	<b>1.1</b>	4.3	<b>1.3</b>	<b>1.2</b>	<b>1.5</b>	<b>1.6</b>	<b>1.7</b>	<b>1.9</b>	<b>2.6</b>	IPOP-CMA-ES [15]	
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.2</b>	<b>1.4</b>	4.5	4.7	3.2	<b>2.4</b>	<b>2.3</b>	<b>2.6</b>	CMA+DE-MOS [13]	
NEWUOA	<b>1</b>	<b>1.2</b>	3.2	3.6	7.7	43	<i>62e-4/5e3</i>	.	.	.	NEWUOA [16]	
Basic RCGA	<b>1</b>	<b>1.4</b>	<b>1.5</b>	<b>2.6</b>	13	11	37	43	161	<i>19e-6/5e4</i>	Basic RCGA [17]	
SPSA	36	101	278	2723	3628	2262	6233	<i>24e-2/1e5</i>	.	.	SPSA [9]	

Table 52: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{122}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>122 Schaffer F7 Gauss</b>											
$\Delta\text{ftarget}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$
$ERT_{\text{best}}/D$	0.33	0.33	1.9	119	601	1439	2532	3458	4081	6336	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	5.3	7.0	6.8	53	<i>15e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.8</b>	5.1	<b>1.6</b>	5.0	24	<i>21e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.3</b>	6.4	3.1	10	47	<i>35e-3/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.7</b>	10	5.2	56	<i>16e-2/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.3</b>	6.1	3.5	6.1	47	<i>20e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	4.5	<b>1.9</b>	<b>3.6</b>	9.3	<i>85e-4/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.3</b>	3.0	<b>0.74</b>	5.3	11	58	<i>18e-3/1e4</i>	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>2.3</b>	11	5.1	11	103	<i>61e-3/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>2.1</b>	13	22	<i>37e-2/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	29	35	11	4.1	49	147	165	406	<i>52e-3/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.3</b>	<b>2.9</b>	<b>1.4</b>	<b>0.80</b>	<b>0.70</b>	<b>0.67</b>	<b>0.61</b>	<b>0.81</b>	<b>0.90</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.1</b>	<b>1.9</b>	<b>1.1</b>	<b>1.1</b>	<b>0.69</b>	<b>0.76</b>	<b>0.84</b>	<b>0.96</b>	<b>1.1</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.3</b>	<b>1.5</b>	<b>2.7</b>	9.2	15	15	17	<b>22</b>	<b>17</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.1</b>	8.5	21	122	<i>65e-2/5e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1.1</b>	<b>1.1</b>	<b>1.4</b>	7.9	13	<b>8.6</b>	<b>13</b>	<b>16</b>	87	<i>67e-6/5e4</i>	Basic RCGA [17]
SPSA	69	158	103	2636	<i>20e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 53: 03-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{123}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>123 Schaffer F7 unif</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.33	1.6	515	7277	16727	31053	43067	63620	1.47e5	
(1,2)-CMA-ES	<b>1</b>	5.9	29	11	<i>73e-2/1e4</i>	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>2.3</b>	34	7.4	<i>62e-2/1e4</i>	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	20	48	5.0	<i>65e-2/1e4</i>	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.2</b>	49	15	<i>90e-2/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.5</b>	27	7.2	19	<i>34e-2/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.4</b>	<b>4.6</b>	<b>3.1</b>	<i>32e-2/1e4</i>	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.4</b>	30	5.2	<i>45e-2/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	37	82	10	<i>59e-2/1e4</i>	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	12	118	33	<i>16e-1/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	374	549	697	46	<b>17</b>	89	<i>75e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.1</b>	25	<b>2.9</b>	<b>0.56</b>	<b>0.71</b>	<b>0.75</b>	<b>0.75</b>	<b>0.84</b>	<b>0.92</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.4</b>	8.5	<b>1.7</b>	<b>0.90</b>	<b>0.98</b>	<b>0.89</b>	<b>0.82</b>	<b>0.85</b>	<b>1.2</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.3</b>	<b>1.8</b>	171	51	<b>22</b>	<b>16</b>	<b>16</b>	<b>11</b>	<b>4.8</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	12	132	20	<i>12e-1/5e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.2</b>	<b>2.2</b>	13	47	<i>36e-2/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	64	46353	22910	1289	<i>14e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 54: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{124}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>124 Schaffer F7 Cauchy</b>											
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	<b>1.4</b>	43	7.4	34	<i>82e-3/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	<b>1.5</b>	<b>2.3</b>	<b>0.46</b>	<b>2.7</b>	4.1	60	<i>70e-4/1e4</i>	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	<b>1.6</b>	3.9	<b>2.2</b>	3.7	7.6	<i>73e-4/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	<b>1.3</b>	6.4	10	78	<i>13e-2/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	<b>1.9</b>	34	17	8.5	11	60	<i>79e-4/1e4</i>	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	<b>1.1</b>	<b>2.8</b>	<b>0.89</b>	<b>2.1</b>	<b>2.9</b>	6.5	46	<i>10e-4/1e4</i>	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	<b>1.4</b>	3.7	<b>2.4</b>	<b>1.2</b>	<b>1.5</b>	<b>5.7</b>	<i>91e-5/1e4</i>	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	<b>2.1</b>	22	<b>2.6</b>	4.2	5.5	63	<i>45e-4/1e4</i>	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	<b>1.5</b>	11	7.7	59	<i>18e-2/5e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	15	24	16	6.2	30	103	<i>11e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	<b>2.0</b>	4.2	<b>0.54</b>	<b>0.82</b>	<b>0.50</b>	<b>0.55</b>	<b>0.87</b>	<b>1.2</b>	<b>1.4</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	<b>1.5</b>	3.2	<b>0.59</b>	<b>2.0</b>	<b>1.1</b>	<b>0.79</b>	<b>0.96</b>	<b>1.5</b>	<b>2.4</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	<b>1.3</b>	<b>2.4</b>	<b>2.5</b>	27	10	5.8	<b>5.0</b>	<b>5.0</b>	<b>5.0</b>	CMA+DE-MOS [13]
NEWUOA	1	<b>1.5</b>	5.6	13	36	<i>14e-2/5e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	1	<b>1.2</b>	<b>1.8</b>	4.5	22	11	18	50	170	<i>80e-5/5e4</i>	Basic RCGA [17]
SPSA	27	51	6155	2182	4845	<i>11e-1/1e5</i>	.	.	.	.	SPSA [9]

Table 55: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>125 Griewank-Rosenbrock Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.33	0.33	0.33	0.33	1473	8226	11656	12117	12667	
(1,2)-CMA-ES	1	1	1	19	572	6.4	<i>69e-4/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1	<b>8.7</b>	<b>207</b>	3.9	18	13	<i>38e-4/1e4</i>	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	10	289	<b>2.8</b>	18	13	<i>53e-4/1e4</i>	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	<b>1.3</b>	11	791	5.8	<i>68e-4/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1	<b>8.1</b>	677	4.8	8.6	<i>55e-4/1e4</i>	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1	10	508	3.1	8.6	13	12	<i>31e-4/1e4</i>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	<b>8.9</b>	298	<b>2.5</b>	4.0	13	<i>31e-4/1e4</i>	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	1	14	556	5.3	18	<i>69e-4/1e4</i>	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	<b>1.4</b>	9.3	326	<b>1.6</b>	3.0	6.9	6.7	<i>40e-4/6e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	30	38	49	79	569	<b>1.8</b>	21	38	57	115	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	<b>1.3</b>	9.5	289	<b>0.69</b>	<b>0.67</b>	<b>0.70</b>	<b>0.76</b>	<b>0.75</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	<b>1.2</b>	11	<b>243</b>	<b>1.4</b>	<b>1.1</b>	<b>0.98</b>	<b>0.97</b>	<b>0.99</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	<b>1.1</b>	13	<b>222</b>	<b>1.8</b>	4.0	6.3	6.1	<b>5.9</b>	CMA+DE-MOS [13]
NEWUOA	1	1	<b>2.8</b>	10	332	<b>0.88</b>	<b>2.8</b>	<b>2.0</b>	<b>1.9</b>	<i>19e-4/5e3</i>	NEWUOA [16]
Basic RCGA	1	1	<b>1.3</b>	9.3	291	<b>1.0</b>	5.2	8.1	59	<i>54e-5/5e4</i>	Basic RCGA [17]
SPSA	25	38	41	66	21710	14	<i>36e-4/1e5</i>	.	.	.	SPSA [9]



Table 56: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	126 Griewank-Rosenbrock unif										
$\Delta\text{ftarget}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$
$ERT_{\text{best}}/D$	0.33	0.33	0.33	0.33	0.33	4499	37712	1.11e5	2.08e5	3.20e5	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	1.1	135	3640	15	<i>26e-3/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1	87	3050	16	<i>22e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	148	1434	7.1	<i>20e-3/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	1	209	5363	<i>38e-3/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1.2	15	1230	10	<i>18e-3/1e4</i>	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1	11	1618	3.4	<i>10e-3/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	6.5	1116	7.3	<i>12e-3/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	32	97	1584	5.4	<i>12e-3/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	1.7	258	6248	<i>49e-3/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	630	728	1797	2592	7997	8.5	4.1	6.1	<i>22e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	1	74	933	<b>0.68</b>	<b>0.89</b>	<b>0.66</b>	<b>0.49</b>	<b>0.49</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	1	15	<b>645</b>	<b>0.85</b>	<b>0.88</b>	<b>0.81</b>	<b>0.95</b>	<b>0.91</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	1.1	16	<b>237</b>	<b>0.11</b>	15	<i>27e-4/1e5</i>	.	.	CMA+DE-MOS [13]
NEWUOA	1	1	13	266	8605	17	<i>48e-3/5e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	1	1	1.1	7.1	<b>350</b>	<b>0.31</b>	<b>0.65</b>	<b>1.1</b>	<b>3.5</b>	<i>15e-5/5e4</i>	Basic RCGA [17]
SPSA	18	46208	75111	2.01e5	3.07e5	159	<i>54e-3/1e5</i>	.	.	.	SPSA [9]

Table 57: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	127 Griewank-Rosenbrock Cauchy										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 0.33	1e+00 0.33	1e-01 0.33	1e-02 1168	1e-03 13028	1e-04 15016	1e-05 15116	1e-07 15332	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	1.3	11	367	6.1	<i>76e-4/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1.1	6.9	184	2.1	1.8	4.7	4.6	4.6	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	10	644	3.5	5.5	<i>54e-4/1e4</i>	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	1	12	644	7.3	11	<i>73e-4/1e4</i>	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1	4.8	423	6.0	5.4	10	9.5	9.4	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1.1	9.3	417	3.7	5.4	10	10	10	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	4.7	217	1.5	2.2	2.0	2.0	1.9	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	1	13	204	4.5	2.3	4.5	4.5	4.4	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	2.1	11	295	4.5	<i>61e-4/5e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	14	24	30	55	224	10	24	94	<i>17e-4/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	1	6.4	179	3.7	1.2	1.1	1.1	1.1	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	1	14	189	4.3	0.83	1.4	1.5	1.5	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	1.1	12	190	0.19	1.9	2.7	2.7	2.8	CMA+DE-MOS [13]
NEWUOA	1	1	2.1	18	278	1.6	2.3	4.3	4.2	<i>61e-4/4e3</i>	NEWUOA [16]
Basic RCGA	1	1	1.1	12	293	1.1	2.3	8.3	15	46	Basic RCGA [17]
SPSA	31	47	82	1530	45810	582	<i>22e-3/1e5</i>	.	.	.	SPSA [9]

Table 58: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{128}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>128 Gallagher Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.8	1e+00 142	1e-01 375	1e-02 449	1e-03 639	1e-04 903	1e-05 905	1e-07 1447	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	4.7	3.7	<b>2.3</b>	4.7	4.7	6.8	7.1	7.7	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.9</b>	<b>1.6</b>	<b>2.3</b>	<b>2.5</b>	<b>1.8</b>	<b>1.4</b>	<b>1.7</b>	<b>1.1</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.3</b>	<b>2.9</b>	4.0	3.7	3.1	<b>2.3</b>	<b>2.6</b>	<b>1.9</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	3.5	3.1	3.4	5.7	5.0	3.9	3.9	4.3	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>2.7</b>	<b>2.4</b>	<b>2.5</b>	<b>1.8</b>	<b>1.3</b>	<b>1.3</b>	<b>0.91</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.0</b>	3.3	4.1	4.0	<b>2.8</b>	<b>2.4</b>	<b>2.4</b>	<b>1.9</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	3.6	3.1	3.1	<b>3.6</b>	<b>2.5</b>	<b>1.9</b>	<b>1.9</b>	<b>1.2</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.7</b>	3.1	4.8	4.8	3.7	<b>2.7</b>	<b>2.8</b>	<b>2.4</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	4.3	10	19	25	18	17	45	<i>45e-3/6e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	30	40	12	14	48	84	146	264	471	<i>90e-5/1e5</i>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	7.3	16	36	26	76	76	48	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>2.2</b>	7.3	12	11	15	11	11	7.3	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.3</b>	33	52	46	32	24	24	16	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>1.7</b>	7.0	9.1	14	35	84	<i>89e-4/5e3</i>	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.3</b>	18	33	58	49	35	43	41	Basic RCGA [17]
SPSA	20	31	150	1406	1931	3251	2283	<i>13e-1/1e5</i>	.	.	SPSA [9]

Table 59: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{129}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	129 Gallagher unif										
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03 0.33	1e+02 0.33	1e+01 1.6	1e+00 121	1e-01 1131	1e-02 2617	1e-03 3861	1e-04 8261	1e-05 9454	1e-07 12845	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	53	15	5.2	54	<i>23e-3/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	21	13	4.8	17	36	<i>61e-3/1e4</i>	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	31	18	7.9	18	38	<i>27e-3/1e4</i>	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	28	25	11	28	<i>90e-3/1e4</i>	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	14	14	<b>4.0</b>	5.7	<b>11</b>	18	15	<i>11e-3/1e4</i>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	5.1	<b>7.3</b>	<b>3.2</b>	<b>5.3</b>	12	<b>8.5</b>	<i>47e-4/1e4</i>	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	10	11	<b>4.5</b>	6.2	37	<i>30e-3/1e4</i>	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	22	<b>11</b>	5.5	7.6	38	18	<i>14e-3/1e4</i>	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	51	34	12	15	21	<b>10</b>	<i>23e-2/6e3</i>	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	181	2286	6231	223	74	45	88	56	157	116	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.4</b>	<b>5.9</b>	5.0	<b>2.8</b>	<b>12</b>	<b>10</b>	<b>9.1</b>	<b>6.9</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	7.5	12	4.7	<b>3.3</b>	<b>6.1</b>	13	<b>11</b>	<b>22</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.4</b>	239	81	72	77	51	45	48	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	56	63	21	30	21	<i>79e-2/5e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.6</b>	11	12	11	24	14	<b>13</b>	<b>27</b>	Basic RCGA [17]
SPSA	54	279	1008	171	308	271	<i>14e-2/1e5</i>	.	.	.	SPSA [9]

Table 60: 03-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>130 Gallagher Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.33	0.33	1.8	82	172	305	501	2264	3981	4782	
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.9</b>	38	43	24	15	3.4	<b>2.3</b>	<b>2.0</b>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.7</b>	17	14	<b>7.9</b>	5.5	<b>1.2</b>	<b>0.71</b>	<b>0.60</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	8.1	<b>10</b>	10	5.9	<b>1.7</b>	<b>0.97</b>	<b>0.82</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	4.0	32	53	31	19	5.0	<b>2.8</b>	<b>2.4</b>	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	21	10	13	10	6.0	<b>1.3</b>	<b>0.76</b>	<b>0.64</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.1</b>	11	15	8.6	<b>5.2</b>	<b>1.2</b>	<b>0.67</b>	<b>0.56</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	14	8.5	<b>7.6</b>	<b>5.2</b>	<b>3.2</b>	<b>0.70</b>	<b>0.40</b>	<b>0.34</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.4</b>	<b>7.7</b>	15	<b>8.4</b>	<b>5.2</b>	<b>1.1</b>	<b>0.65</b>	<b>0.55</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>2.6</b>	<b>3.9</b>	12	8.5	11	5.6	5.7	<i>90e-5/5e3</i>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	22	37	12	54	155	216	204	131	104	<i>99e-5/1e5</i>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>2.3</b>	19	46	51	57	35	20	17	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	3.1	53	57	33	153	34	19	16	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.8</b>	90	332	398	389	86	87	73	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.0</b>	<b>3.0</b>	<b>9.4</b>	18	21	6.6	17	<i>86e-4/5e3</i>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.3</b>	15	84	132	139	31	23	26	Basic RCGA [17]
SPSA	15	30	103	523	486	574	1367	648	369	<i>51e-3/1e5</i>	SPSA [9]

Table 61: 05-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>101 Sphere moderate Gauss</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.20	0.20	2.2	7.4	8.8	10	12	13	14	15	
(1,2)-CMA-ES	<b>1</b>	<b>1.2</b>	8.3	4.4	6.3	8.1	8.5	10	11	13	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	3.1	4.3	3.3	4.9	6.0	5.8	6.6	7.4	8.9	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	3.8	<b>2.9</b>	4.1	5.0	5.1	5.8	6.7	7.7	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	7.0	4.7	6.7	8.0	7.6	8.7	10	12	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.8</b>	<b>2.8</b>	3.6	4.5	4.6	5.5	6.1	7.1	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>2.4</b>	<b>2.1</b>	<b>2.8</b>	4.0	4.1	4.5	5.1	6.4	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.2</b>	<b>2.4</b>	<b>1.7</b>	<b>2.3</b>	<b>2.9</b>	<b>3.0</b>	<b>3.5</b>	<b>3.9</b>	<b>4.6</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	3.3	<b>2.7</b>	<b>2.1</b>	<b>2.7</b>	3.5	3.5	4.0	4.4	5.3	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>2.6</b>	<b>2.9</b>	<b>1.5</b>	<b>1.6</b>	<b>1.7</b>	<b>1.5</b>	<b>1.5</b>	<b>1.5</b>	<b>1.5</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	41	61	22	13	14	17	16	18	20	24	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.2</b>	<b>3.0</b>	<b>3.0</b>	4.2	5.8	5.8	6.7	7.6	9.3	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.2</b>	3.3	3.4	4.7	6.0	6.0	6.9	7.8	9.3	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	7.3	12	19	23	24	27	31	37	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	3.6	<b>2.5</b>	<b>1.6</b>	<b>2.1</b>	<b>2.5</b>	<b>2.6</b>	<b>2.9</b>	<b>3.0</b>	<b>3.1</b>	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	7.7	25	48	88	113	155	206	293	Basic RCGA [17]
SPSA	40	64	83	171	386	434	455	494	568	9667	SPSA [9]

Table 62: 05-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>102 Sphere moderate unif</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.20	0.20	2.2	7.1	10	13	14	16	17	20	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.4</b>	9.2	5.8	6.2	6.5	7.7	9.1	10	11	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.4</b>	3.9	3.3	3.6	4.2	4.9	5.4	6.0	6.8	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>2.4</b>	4.2	3.3	3.9	3.9	4.7	5.1	5.4	6.3	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>2.3</b>	4.1	5.2	6.4	6.6	8.0	8.6	9.3	10	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	3.2	<b>2.5</b>	<b>2.9</b>	<b>3.0</b>	3.7	4.2	4.6	5.3	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.7</b>	<b>2.4</b>	<b>2.4</b>	<b>2.7</b>	<b>2.7</b>	3.4	3.9	4.1	4.5	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.3</b>	<b>1.7</b>	<b>2.1</b>	<b>2.3</b>	<b>2.7</b>	<b>3.0</b>	<b>3.2</b>	<b>3.7</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1.6</b>	<b>2.8</b>	<b>2.1</b>	<b>2.4</b>	<b>2.7</b>	<b>3.2</b>	<b>3.4</b>	<b>3.6</b>	<b>4.4</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.3</b>	<b>2.7</b>	<b>1.4</b>	<b>1.5</b>	<b>1.4</b>	<b>1.5</b>	<b>1.5</b>	<b>1.6</b>	<b>1.5</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	45	79	21	14	14	14	16	18	18	20	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.4</b>	3.5	3.4	3.8	4.3	5.0	5.8	6.1	7.0	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.5</b>	3.4	3.1	4.1	4.2	5.1	6.0	6.5	7.3	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	5.7	12	17	18	20	22	25	27	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	3.9	6.3	6.0	7.0	15	20	27	33	41	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.2</b>	10	29	39	57	88	123	155	209	Basic RCGA [17]
SPSA	41	60	1987	4868	9895	9681	9199	11030	24495	<i>31e-3/1e5</i>	SPSA [9]

Table 63: 05-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>103 Sphere moderate Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.20	1e+02 0.20	1e+01 2.2	1e+00 5.5	1e-01 6.0	1e-02 6.0	1e-03 6.3	1e-04 6.4	1e-05 7.0	1e-07 23	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	<b>1.5</b>	6.2	6.7	9.0	13	18	22	25	10	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	<b>2.5</b>	3.4	3.8	5.5	8.4	10	13	15	6.1	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	<b>1</b>	3.8	3.6	5.4	7.5	9.4	12	13	5.4	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	<b>2.1</b>	8.2	7.0	10	12	16	20	22	9.2	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	<b>1.6</b>	<b>2.1</b>	3.0	<b>4.4</b>	6.5	8.5	10	12	5.0	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	<b>1.3</b>	<b>2.6</b>	<b>2.8</b>	4.6	<b>6.3</b>	<b>7.8</b>	<b>10</b>	<b>11</b>	<b>4.4</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	<b>1.2</b>	<b>2.4</b>	<b>2.1</b>	<b>3.5</b>	<b>4.9</b>	<b>6.1</b>	<b>7.5</b>	<b>8.1</b>	<b>3.4</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	<b>1.6</b>	<b>2.9</b>	<b>2.9</b>	4.8	6.7	<b>8.0</b>	<b>10</b>	<b>10</b>	<b>4.2</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	1	<b>2.5</b>	<b>2.5</b>	<b>1.6</b>	<b>3.6</b>	<b>5.4</b>	13	26	42	34	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	32	57	20	15	20	27	30	37	42	20	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	<b>1</b>	<b>2.9</b>	4.1	6.3	8.8	11	14	16	6.5	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	<b>1.4</b>	3.6	4.0	6.6	9.4	12	15	17	7.1	IPOP-CMA-ES [15]
CMA+DE-MOS	1	<b>1.1</b>	7.6	13	28	38	48	60	72	30	CMA+DE-MOS [13]
NEWUOA	1	3.5	<b>2.4</b>	<b>1.9</b>	5.7	9.4	60	85	178	136	NEWUOA [16]
Basic RCGA	1	<b>1.3</b>	7.1	27	60	133	234	353	434	222	Basic RCGA [17]
SPSA	51	202	151	119	165	251	415	5261	93276	<i>42e-6/1e5</i>	SPSA [9]











Table 68: 05-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>108 Sphere unif</b>										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.20	0.20	17	1029	2894	4930	6187	8237	11726	16133	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.7</b>	43	<i>23e-1/1e4</i>	.	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>2.7</b>	27	22	<i>18e-1/1e4</i>	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.1</b>	32	44	<i>19e-1/1e4</i>	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>2.8</b>	90	69	<i>22e-1/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.7</b>	<b>5.9</b>	15	51	<i>11e-1/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.4</b>	25	<b>7.7</b>	<i>84e-2/1e4</i>	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	3.7	15	13	<i>94e-2/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>2.7</b>	25	69	<i>15e-1/1e4</i>	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	3.0	155	44	<i>27e-1/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	5825	9728	290	14	<b>7.8</b>	<b>7.2</b>	<b>8.6</b>	<b>10</b>	<b>13</b>	<b>46</b>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	12	11	<b>0.68</b>	<b>0.64</b>	<b>0.64</b>	<b>0.64</b>	<b>0.75</b>	<b>0.66</b>	<b>0.94</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.7</b>	9.1	<b>0.80</b>	<b>0.67</b>	<b>0.64</b>	<b>0.77</b>	<b>0.70</b>	<b>0.62</b>	<b>0.69</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>2.5</b>	95	125	157	267	201	141	<i>89e-2/1e5</i>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	48	77	64	<i>41e-1/5e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>0.79</b>	13	30	70	<i>16e-2/5e4</i>	.	.	.	Basic RCGA [17]
SPSA	436	1305	89	10	242	<i>15e-2/1e5</i>	.	.	.	.	SPSA [9]

Table 69: 05-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>109 Sphere Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.20	1e+02 0.20	1e+01 2.2	1e+00 11	1e-01 43	1e-02 75	1e-03 114	1e-04 139	1e-05 175	1e-07 189	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>2.7</b>	5.5	<b>2.8</b>	<b>1.8</b>	<b>1.9</b>	<b>1.9</b>	<b>2.5</b>	<b>2.5</b>	3.4	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	3.3	4.1	<b>2.5</b>	<b>1.2</b>	<b>1.1</b>	<b>1.0</b>	<b>1.1</b>	<b>1.0</b>	<b>1.3</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.3</b>	3.4	<b>2.1</b>	<b>1.0</b>	<b>0.86</b>	<b>0.77</b>	<b>0.89</b>	<b>0.89</b>	<b>1.1</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	5.8	3.5	<b>2.0</b>	<b>2.0</b>	<b>2.2</b>	<b>2.4</b>	<b>2.4</b>	3.4	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1.1</b>	3.4	<b>2.2</b>	<b>1.0</b>	<b>0.98</b>	<b>1.0</b>	<b>1.1</b>	<b>1.1</b>	<b>1.4</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>2.9</b>	<b>1.4</b>	<b>0.79</b>	<b>0.82</b>	<b>0.81</b>	<b>0.88</b>	<b>0.93</b>	<b>1.2</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.6</b>	<b>1.9</b>	<b>1.1</b>	<b>0.57</b>	<b>0.52</b>	<b>0.50</b>	<b>0.53</b>	<b>0.52</b>	<b>0.67</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1.2</b>	<b>3.0</b>	<b>1.3</b>	<b>0.79</b>	<b>0.76</b>	<b>0.68</b>	<b>0.68</b>	<b>0.66</b>	<b>0.88</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1.5</b>	4.3	3.6	26	47	<i>67e-4/6e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	41	62	21	8.3	3.1	110	2422	<i>17e-4/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.1</b>	3.1	<b>1.9</b>	<b>1.1</b>	<b>1.0</b>	<b>0.92</b>	<b>1.1</b>	<b>1.2</b>	<b>1.5</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>2.9</b>	<b>2.2</b>	<b>1.2</b>	<b>1.1</b>	<b>1.0</b>	<b>1.1</b>	<b>1.1</b>	<b>1.5</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	6.1	8.7	4.9	4.9	4.7	5.2	5.3	7.4	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.7</b>	4.8	13	83	885	<i>41e-3/5e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.3</b>	9.0	20	12	14	16	20	25	53	Basic RCGA [17]
SPSA	50	101	138	953	3515	<i>13e-2/1e5</i>	.	.	.	.	SPSA [9]











Table 74: 05-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{114}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	114 Step-ellipsoid unif										
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
	0.20	2.3	153	2944	11262	15778	16654	16654	16654	16990	
(1,2)-CMA-ES	<b>1.3</b>	144	101	<i>11e+0/1e4</i>	.	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.5</b>	87	25	<i>63e-1/1e4</i>	.	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1.3</b>	139	54	<i>79e-1/1e4</i>	.	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	38	56	56	<i>73e-1/1e4</i>	.	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>2.3</b>	55	18	<i>46e-1/1e4</i>	.	.	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>2.3</b>	<b>17</b>	14	<i>30e-1/1e4</i>	.	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	53	26	19	50	<i>21e-1/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.4</b>	23	21	<i>53e-1/1e4</i>	.	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1.3</b>	112	74	<i>11e+0/6e3</i>	.	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	1787	721	152	61	<i>19e-1/1e5</i>	.	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1.3</b>	35	<b>3.3</b>	<b>0.61</b>	<b>0.49</b>	<b>0.62</b>	<b>0.60</b>	<b>0.60</b>	<b>0.60</b>	<b>0.61</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.3</b>	41	<b>3.2</b>	<b>0.45</b>	<b>0.48</b>	<b>0.80</b>	<b>0.79</b>	<b>0.79</b>	<b>0.79</b>	<b>0.80</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.5</b>	<b>2.5</b>	60	130	34	<b>33</b>	<b>48</b>	<b>48</b>	<b>48</b>	<b>47</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	150	43	<i>89e-1/5e3</i>	.	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1.2</b>	<b>1.2</b>	<b>12</b>	<b>16</b>	<b>31</b>	<i>41e-2/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	1025	531	181	245	<i>29e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 75: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best}}^{2009}$  on  $f_{115}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	115 Step-ellipsoid Cauchy										
$\Delta\text{ftarget}$ $\text{ERT}_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$ $\text{ERT}_{\text{best}}/D$
(1,2)-CMA-ES	<b>2.2</b>	3.8	5.3	5.7	66	<i>13e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1.7</b>	<b>2.5</b>	<b>1.9</b>	<b>2.4</b>	6.6	54	137	137	137	240	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>2.9</b>	<b>3.0</b>	<b>2.3</b>	<b>1.6</b>	7.5	44	88	88	88	247	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1.3</b>	3.1	4.7	11	50	<i>17e-2/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1.9</b>	<b>1.7</b>	<b>1.7</b>	<b>1.7</b>	5.5	23	134	134	134	119	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1.6</b>	<b>1.4</b>	<b>1.2</b>	<b>1.3</b>	<b>2.6</b>	<b>13</b>	26	26	26	70	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1.7</b>	<b>1.4</b>	<b>2.9</b>	<b>1.7</b>	4.6	26	49	49	49	55	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1.7</b>	<b>1.6</b>	<b>1.9</b>	<b>1.8</b>	6.9	45	89	89	89	<i>11e-3/1e4</i>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1.1</b>	<b>1.6</b>	<b>1.1</b>	4.2	28	<i>10e-2/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	63	13	8.6	422	1803	3116	2779	2779	2779	<i>31e-2/1e5</i>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1.2</b>	<b>2.0</b>	<b>1.8</b>	<b>0.81</b>	<b>1.1</b>	<b>1.1</b>	<b>1.4</b>	<b>1.4</b>	<b>1.4</b>	<b>1.5</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1.3</b>	<b>1.2</b>	<b>1.7</b>	<b>2.4</b>	<b>2.7</b>	<b>2.9</b>	<b>3.1</b>	<b>3.1</b>	<b>3.1</b>	<b>2.7</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1.5</b>	<b>2.5</b>	5.3	18	31	25	<b>23</b>	<b>23</b>	<b>23</b>	<b>20</b>	CMA+DE-MOS [13]
NEWUOA	<b>2.1</b>	<b>1.2</b>	<b>2.9</b>	14	42	<i>34e-2/4e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1.4</b>	<b>1.7</b>	74	68	108	769	703	703	703	604	Basic RCGA [17]
SPSA	58	64	222	1640	3866	<i>12e-1/1e5</i>	.	.	.	.	SPSA [9]





Table 78: 05-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{118}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>118 Ellipsoid Cauchy</b>												
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$	
$ERT_{\text{best}}/D$	6.6	11	86	243	311	355	400	441	486	583	$ERT_{\text{best}}/D$	
(1,2)-CMA-ES	6.1	15	9.2	6.5	6.4	7.3	7.8	7.9	8.2	8.8	(1,2)-CMA-ES	[4, 2]
(1,2m)-CMA-ES	6.1	10	4.6	<b>2.4</b>	<b>2.2</b>	<b>2.2</b>	<b>2.2</b>	<b>2.0</b>	<b>2.0</b>	<b>1.8</b>	(1,2m)-CMA-ES	[4]
(1,2ms)-CMA-ES	5.0	7.2	<b>2.6</b>	<b>1.6</b>	<b>1.8</b>	<b>1.8</b>	<b>1.7</b>	<b>1.6</b>	<b>1.5</b>	<b>1.4</b>	(1,2ms)-CMA-ES	[4]
(1,2s)-CMA-ES	6.6	16	18	10	16	17	19	24	39	44	(1,2s)-CMA-ES	[2]
(1,4)-CMA-ES	3.4	7.0	<b>2.3</b>	<b>1.4</b>	<b>1.3</b>	<b>1.4</b>	<b>1.3</b>	<b>1.3</b>	<b>1.3</b>	<b>1.2</b>	(1,4)-CMA-ES	[5, 3]
(1,4m)-CMA-ES	<b>2.6</b>	5.7	<b>2.0</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	(1,4m)-CMA-ES	[5]
(1,4ms)-CMA-ES	<b>2.0</b>	<b>4.1</b>	<b>1.1</b>	<b>0.71</b>	<b>0.77</b>	<b>0.78</b>	<b>0.75</b>	<b>0.73</b>	<b>0.70</b>	<b>0.65</b>	(1,4ms)-CMA-ES	[1, 5]
(1,4s)-CMA-ES	3.6	7.2	<b>1.9</b>	<b>1.0</b>	<b>0.96</b>	<b>0.97</b>	<b>0.95</b>	<b>0.92</b>	<b>0.88</b>	<b>0.84</b>	(1,4s)-CMA-ES	[3]
avg NEWUOA	<b>0.92</b>	<b>0.97</b>	<b>1.8</b>	8.3	64	<i>18e-2/7e3</i>	.	.	.	.	avg NEWUOA	[16]
CMA-EGS (IPOP,r1)	27	689	337	622	889	3954	<i>21e-1/1e5</i>	.	.	.	CMA-EGS (IPOP,r1)	[8]
IPOP-aCMA-ES	<b>2.5</b>	6.1	<b>1.7</b>	<b>0.88</b>	<b>0.91</b>	<b>0.91</b>	<b>0.91</b>	<b>0.92</b>	<b>0.91</b>	<b>0.90</b>	IPOP-aCMA-ES	[12]
IPOP-CMA-ES	<b>3.0</b>	9.0	3.2	<b>2.0</b>	<b>1.9</b>	<b>2.0</b>	<b>2.0</b>	<b>1.9</b>	<b>1.9</b>	<b>1.7</b>	IPOP-CMA-ES	[15]
CMA+DE-MOS	7.6	17	3.7	<b>1.8</b>	<b>1.7</b>	<b>1.8</b>	<b>2.1</b>	<b>2.3</b>	<b>2.5</b>	<b>2.8</b>	CMA+DE-MOS	[13]
NEWUOA	<b>0.80</b>	<b>1.3</b>	4.3	10	116	<i>30e-2/5e3</i>	.	.	.	.	NEWUOA	[16]
Basic RCGA	5.4	520	495	1424	<i>45e-1/5e4</i>	.	.	.	.	.	Basic RCGA	[17]
SPSA	46	255	2588	<i>18e+0/1e5</i>	.	.	.	.	.	.	SPSA	[9]





Table 80: 05-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{120}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	120 Sum of diff powers unif										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.20	1e+02 0.20	1e+01 3.2	1e+00 580	1e-01 3740	1e-02 6898	1e-03 14488	1e-04 35436	1e-05 66660	1e-07 1.10e5	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.5</b>	77	33	<i>14e-1/1e4</i>	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	34	46	79	40	<i>11e-1/1e4</i>	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.7</b>	34	26	<i>10e-1/1e4</i>	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	63	51	34	<i>14e-1/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	11	36	16	<i>77e-2/1e4</i>	.	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>2.9</b>	13	<b>6.6</b>	<i>66e-2/1e4</i>	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	56	64	10	<i>69e-2/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1.9</b>	38	15	<i>83e-2/1e4</i>	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	42	94	49	<i>15e-1/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	1223	2182	675	85	33	24	49	<i>13e-3/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>2.3</b>	18	<b>0.76</b>	<b>0.65</b>	<b>0.82</b>	<b>0.83</b>	<b>0.53</b>	<b>0.43</b>	<b>0.66</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.1</b>	<b>6.0</b>	<b>1.6</b>	<b>0.68</b>	<b>0.73</b>	<b>0.69</b>	<b>0.46</b>	<b>0.55</b>	<b>0.83</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.2</b>	<b>2.5</b>	63	130	71	<b>34</b>	<b>22</b>	<b>24</b>	<b>15</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	34	130	55	<i>24e-1/5e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.3</b>	<b>0.87</b>	17	<b>12</b>	<b>23</b>	<i>50e-3/5e4</i>	.	.	.	Basic RCGA [17]
SPSA	194	1082	276	165	<i>84e-2/1e5</i>	.	.	.	.	.	SPSA [9]

Table 81: 05-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	121 Sum of diff powers Cauchy										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.20	0.20	1.7	22	55	107	317	525	774	1239	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.3</b>	4.5	<b>2.9</b>	<b>1.9</b>	3.3	<b>2.9</b>	3.8	4.5	9.0	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.6</b>	<b>2.4</b>	<b>1.2</b>	<b>0.94</b>	<b>1.2</b>	<b>1.1</b>	<b>1.7</b>	<b>1.9</b>	<b>2.8</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>2.7</b>	<b>1.1</b>	<b>0.87</b>	<b>0.84</b>	<b>0.90</b>	<b>1.0</b>	<b>1.2</b>	<b>1.3</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	4.4	5.3	<b>2.9</b>	<b>2.2</b>	<b>2.8</b>	5.7	5.5	9.4	27	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>2.1</b>	<b>1.7</b>	<b>1.2</b>	<b>0.91</b>	<b>1.1</b>	<b>0.96</b>	<b>1.1</b>	<b>1.2</b>	<b>1.3</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.7</b>	3.4	<b>1.2</b>	<b>0.86</b>	<b>1.1</b>	<b>0.91</b>	<b>0.93</b>	<b>1.0</b>	<b>1.2</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.2</b>	<b>2.0</b>	<b>0.72</b>	<b>0.57</b>	<b>0.70</b>	<b>0.51</b>	<b>0.58</b>	<b>0.60</b>	<b>0.56</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	3.1	<b>2.6</b>	<b>0.98</b>	<b>0.75</b>	<b>0.86</b>	<b>0.62</b>	<b>0.70</b>	<b>0.77</b>	<b>0.80</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	3.3	4.3	3.3	45	788	<i>38e-3/6e3</i>	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	46	62	16	4.3	<b>2.9</b>	482	4519	<i>55e-4/1e5</i>	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	3.3	3.0	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>0.78</b>	<b>0.79</b>	<b>0.84</b>	<b>0.82</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.6</b>	<b>1.9</b>	<b>1.1</b>	<b>1.0</b>	<b>1.1</b>	<b>1.1</b>	<b>1.7</b>	<b>2.1</b>	<b>2.3</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.2</b>	3.5	4.9	4.0	4.0	<b>2.3</b>	<b>2.4</b>	<b>2.3</b>	<b>2.5</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	3.9	4.8	15	76	<i>86e-3/4e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.3</b>	<b>2.1</b>	11	11	11	30	1408	<i>22e-5/5e4</i>	.	Basic RCGA [17]
SPSA	42	74	119	6850	<i>11e-1/1e5</i>	.	.	.	.	.	SPSA [9]





Table 84: 05-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{124}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>124 Schaffer F7 Cauchy</b>										
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.20	0.20	1.9	40	208	1795	4096	5279	9067	19040	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1.1</b>	11	127	700	<i>52e-2/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1.1</b>	3.4	<b>2.7</b>	30	83	<i>65e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1.3</b>	4.3	5.5	22	<i>60e-3/1e4</i>	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1.8</b>	96	277	<i>88e-2/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	3.1	<b>2.8</b>	21	119	<i>13e-2/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1.1</b>	<b>2.4</b>	<b>2.5</b>	15	39	<i>41e-3/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1.3</b>	<b>1.8</b>	7.6	18	79	<i>46e-3/1e4</i>	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1.7</b>	17	19	72	<i>10e-2/1e4</i>	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>2.1</b>	6.1	89	<i>63e-2/6e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	54	76	19	5.7	80	<i>44e-3/6e4</i>	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.3</b>	<b>2.6</b>	<b>1.2</b>	<b>2.1</b>	<b>0.85</b>	<b>0.93</b>	<b>0.93</b>	<b>0.94</b>	<b>0.59</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.8</b>	<b>2.8</b>	<b>1.3</b>	<b>4.0</b>	<b>1.0</b>	<b>1.2</b>	<b>1.1</b>	<b>0.93</b>	<b>0.65</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1.1</b>	<b>1.7</b>	5.9	<b>15</b>	<b>3.5</b>	<b>2.4</b>	<b>2.2</b>	<b>3.3</b>	<b>1.9</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1.1</b>	<b>3.0</b>	158	<i>11e-1/4e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1.1</b>	<b>2.4</b>	63	41	10	11	66	<i>55e-5/5e4</i>	.	Basic RCGA [17]
SPSA	59	96	516	16583	<i>39e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 85: 05-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>125 Griewank-Rosenbrock Gauss</b>											
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03 0.20	1e+02 0.20	1e+01 0.20	1e+00 0.20	1e-01 0.20	1e-02 25031	1e-03 47750	1e-04 48260	1e-05 48600	1e-07 49199	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	120	59424	<i>92e-3/1e4</i>	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.3</b>	69	14809	<i>69e-3/1e4</i>	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	36	32993	<i>81e-3/1e4</i>	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	247	1.04e5	<i>11e-2/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>21</b>	12610	<i>58e-3/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	24	12571	<i>58e-3/1e4</i>	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>20</b>	12034	<i>54e-3/1e4</i>	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	48	23166	<i>82e-3/1e4</i>	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>2.0</b>	81	9966	<i>36e-3/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	49	65	70	153	3423	5.7	<i>10e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	26	3142	<b>0.75</b>	<b>0.53</b>	<b>0.56</b>	<b>0.57</b>	<b>0.57</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	27	<b>2599</b>	<b>0.79</b>	<b>0.78</b>	<b>1.3</b>	<b>1.3</b>	<b>1.3</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.2</b>	34	<b>810</b>	5.0	<b>16</b>	<b>16</b>	<b>16</b>	<b>16</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	3.9	<b>15</b>	6088	<b>2.8</b>	<i>40e-3/5e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.1</b>	26	<b>1574</b>	<b>1.3</b>	<i>82e-4/5e4</i>	.	.	.	Basic RCGA [17]
SPSA	41	60	35786	35837	52690	56	<i>51e-3/1e5</i>	.	.	.	SPSA [9]

Table 86: 05-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>126 Griewank-Rosenbrock unif</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07		$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.20	0.20	0.20	0.20	0.20	<i>1.75e5</i>	$\infty$	$\infty$	$\infty$	$\infty$		
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	2015	7.40e5	<i>25e-2/1e4</i>	.	.	.	.		(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	618	<i>22e-2/1e4</i>	.	.	.	.	.		(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	719	<i>20e-2/1e4</i>	.	.	.	.	.		(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>32</b>	585	7.17e5	<i>26e-2/1e4</i>	.	.	.	.		(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	532	<i>15e-2/1e4</i>	.	.	.	.	.		(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	356	2.33e5	<i>12e-2/1e4</i>	.	.	.	.		(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	82	1.14e5	<i>12e-2/1e4</i>	.	.	.	.		(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	282	3.57e5	<i>18e-2/1e4</i>	.	.	.	.		(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>22</b>	1636	4.54e5	<i>26e-2/6e3</i>	.	.	.	.		avg NEWUOA [16]
CMA-EGS (IPOP,r1)	1548	1777	5228	7914	99874	8.3	<i>23e-3/1e5</i>	.	.	.		CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>62</b>	<b>7882</b>	<b>1.4</b>	<i>51e-4/4e5</i>	.	.	.		IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	63	10254	<b>1.2</b>	<b>1.21e7</b>	<b>1.87e7</b>	<b>1.88e7</b>	<b>1.89e7</b>		IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.2</b>	<b>34</b>	<b>568</b>	<i>23e-3/1e5</i>	.	.	.	.		CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>1.2</b>	1053	3.47e5	<i>26e-2/5e3</i>	.	.	.	.		NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.1</b>	<b>33</b>	<b>1409</b>	<b>0.59</b>	<i>11e-3/5e4</i>	.	.	.		Basic RCGA [17]
SPSA	1.00e6	2.00e6	3.25e6	3.25e6	7.17e6	<i>16e+2/1e5</i>	.	.	.	.		SPSA [9]

Table 87: 05-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>127 Griewank-Rosenbrock Cauchy</b>											
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03 0.20	1e+02 0.20	1e+01 0.20	1e+00 0.20	1e-01 0.20	1e-02 25716	1e-03 68336	1e-04 77023	1e-05 77898	1e-07 79070	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	85	13853	5.8	<i>55e-3/1e4</i>	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	31	5212	<b>2.7</b>	<i>44e-3/1e4</i>	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	27	4508	5.8	<i>29e-3/1e4</i>	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.3</b>	60	37537	<i>64e-3/1e4</i>	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	18	7947	<i>32e-3/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	17	3986	5.6	<i>24e-3/1e4</i>	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	24	7806	<i>42e-3/1e4</i>	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>17</b>	9717	5.7	<i>29e-3/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>2.0</b>	18	5233	<i>53e-3/6e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	44	62	77	181	1992	3.6	<i>92e-4/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.1</b>	30	3085	<b>0.65</b>	<b>0.50</b>	<b>0.45</b>	<b>0.46</b>	<b>0.46</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>15</b>	<b>1542</b>	<b>0.69</b>	<b>0.58</b>	<b>0.63</b>	<b>0.64</b>	<b>0.65</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.2</b>	35	<b>656</b>	<b>0.96</b>	<b>4.6</b>	<b>20</b>	<b>20</b>	<b>19</b>	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.5</b>	<b>14</b>	7248	<i>62e-3/4e3</i>	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.1</b>	41	<b>991</b>	<b>1.8</b>	<i>95e-4/5e4</i>	.	.	.	Basic RCGA [17]
SPSA	45	56	122	21588	3.40e6	<i>15e-2/1e5</i>	.	.	.	.	SPSA [9]







Table 90: 05-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{130}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>130 Gallagher Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.20	1e+02 0.20	1e+01 11	1e+00 162	1e-01 607	1e-02 1640	1e-03 6565	1e-04 6746	1e-05 6778	1e-07 6906	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	14	48	23	10	<b>2.9</b>	<b>2.8</b>	<b>2.8</b>	3.6	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	7.2	17	8.7	<b>3.3</b>	<b>0.82</b>	<b>0.80</b>	<b>0.80</b>	<b>0.79</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	5.3	14	<b>5.1</b>	<b>1.9</b>	<b>0.47</b>	<b>0.46</b>	<b>0.46</b>	<b>0.46</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	37	58	41	15	3.8	3.7	3.8	3.8	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	5.4	25	12	4.5	<b>1.1</b>	<b>1.1</b>	<b>1.2</b>	<b>1.2</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1.0</b>	15	10	3.8	<b>0.95</b>	<b>0.93</b>	<b>0.93</b>	<b>0.92</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	6.8	<b>4.2</b>	<b>3.5</b>	<b>1.3</b>	<b>0.33</b>	<b>0.32</b>	<b>0.32</b>	<b>0.32</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	3.3	14	15	5.5	<b>1.4</b>	<b>1.3</b>	<b>1.3</b>	<b>1.3</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	<b>1.3</b>	<b>6.4</b>	<b>5.9</b>	6.0	<b>3.0</b>	13	<i>14e-3/6e3</i>	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	35	57	5.2	203	146	124	104	102	<i>31e-3/1e5</i>	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1.4</b>	143	391	145	36	35	35	35	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1.2</b>	59	321	147	37	36	36	35	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>2.4</b>	295	221	121	30	29	29	29	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	<b>2.3</b>	<b>11</b>	10	19	<i>62e-3/4e3</i>	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>2.5</b>	250	74	29	7.5	9.2	9.3	10	Basic RCGA [17]
SPSA	40	62	142	1955	<i>19e-1/1e5</i>	.	.	.	.	.	SPSA [9]

Table 91: 10-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{101}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>101 Sphere moderate Gauss</b>												
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.10	1e+02 0.10	1e+01 2.6	1e+00 4.0	1e-01 18	1e-02 19	1e-03 19	1e-04 20	1e-05 21	1e-07 23	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	
(1,2)-CMA-ES	<b>1</b>	50	13	14	4.3	5.1	6.0	6.7	7.4	8.8	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>1</b>	14	<b>7.1</b>	<b>7.8</b>	<b>2.4</b>	3.2	3.8	4.2	4.6	5.5	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	<b>1</b>	29	5.6	5.8	<b>1.9</b>	<b>2.5</b>	<b>3.0</b>	3.4	3.8	4.5	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	<b>1</b>	54	14	13	4.2	5.2	6.1	6.9	7.8	9.3	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>1</b>	10	5.1	6.0	<b>2.0</b>	<b>2.6</b>	<b>3.0</b>	3.5	3.8	4.7	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>1</b>	10	4.0	5.0	<b>1.6</b>	<b>2.2</b>	<b>2.6</b>	3.0	3.3	4.1	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>1</b>	12	<b>3.0</b>	<b>3.9</b>	<b>1.3</b>	<b>1.7</b>	<b>2.0</b>	<b>2.3</b>	<b>2.6</b>	<b>3.2</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	<b>1</b>	14	4.7	5.4	<b>1.7</b>	<b>2.2</b>	<b>2.6</b>	<b>3.0</b>	3.3	4.0	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>1</b>	20	<b>2.9</b>	<b>3.4</b>	<b>0.99</b>	<b>1.2</b>	<b>1.2</b>	<b>1.3</b>	<b>1.3</b>	<b>1.4</b>	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	153	253	33	32	8.5	10	11	12	12	14	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	<b>1</b>	<b>6.6</b>	5.1	7.2	<b>2.4</b>	3.2	3.8	4.5	5.0	6.1	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>1</b>	11	5.6	7.4	<b>2.5</b>	3.4	4.1	4.7	5.2	6.1	IPOP-CMA-ES [15]	
CMA+DE-MOS	<b>1</b>	<b>5.9</b>	17	33	8.8	12	15	16	18	22	CMA+DE-MOS [13]	
NEWUOA	<b>1</b>	15	<b>2.1</b>	<b>3.0</b>	<b>1.0</b>	<b>1.6</b>	<b>1.9</b>	<b>2.1</b>	<b>2.3</b>	<b>2.9</b>	NEWUOA [16]	
Basic RCGA	<b>1</b>	<b>7.1</b>	28	63	28	46	121	229	288	377	Basic RCGA [17]	
SPSA	104	177	4405	5820	2316	4151	5693	6382	7916	<i>34e-5/1e5</i>	SPSA [9]	

Table 92: 10-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{102}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>102 Sphere moderate unif</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.10	0.10	2.6	4.1	20	21	23	24	27	30	$ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	50	15	15	4.4	5.2	5.7	6.4	6.8	7.9	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	25	<b>7.3</b>	7.7	<b>2.3</b>	<b>2.8</b>	3.1	3.6	3.7	4.1	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	23	4.9	6.3	<b>1.9</b>	<b>2.3</b>	<b>2.6</b>	<b>2.9</b>	3.1	3.5	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	26	22	21	5.8	6.6	7.4	8.2	8.6	12	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	21	5.8	6.4	<b>2.0</b>	<b>2.5</b>	<b>2.9</b>	3.2	3.4	3.8	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	7.7	4.6	5.1	<b>1.6</b>	<b>1.9</b>	<b>2.2</b>	<b>2.6</b>	<b>2.7</b>	3.1	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	14	<b>3.6</b>	<b>4.4</b>	<b>1.3</b>	<b>1.6</b>	<b>1.9</b>	<b>2.1</b>	<b>2.2</b>	<b>2.5</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	17	4.7	<b>4.9</b>	<b>1.6</b>	<b>2.0</b>	<b>2.2</b>	<b>2.5</b>	<b>2.7</b>	<b>3.0</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	31	<b>2.9</b>	<b>3.2</b>	<b>0.89</b>	<b>1.1</b>	<b>1.2</b>	<b>1.3</b>	<b>1.4</b>	<b>1.7</b>	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	147	242	35	32	8.9	10	10	11	11	11	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	10	5.0	6.9	<b>2.2</b>	<b>2.8</b>	3.3	3.7	4.0	4.4	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>6.0</b>	5.3	7.2	<b>2.3</b>	<b>2.9</b>	3.3	3.8	4.0	4.4	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>5.9</b>	19	32	8.3	11	13	13	15	16	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	18	<b>3.5</b>	7.9	8.0	30	48	81	146	547	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>4.1</b>	26	57	26	42	102	193	234	285	Basic RCGA [17]
SPSA	124	183	1.56e5	3.44e5	<i>21e+0/1e5</i>	.	.	.	.	.	SPSA [9]

Table 93: 10-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>103 Sphere moderate Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.10	1e+02 0.10	1e+01 2.6	1e+00 4.7	1e-01 13	1e-02 14	1e-03 36	1e-04 36	1e-05 36	1e-07 36	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	
(1,2)-CMA-ES	<b>1</b>	34	14	12	6.4	7.4	3.6	4.3	5.2	6.8	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>1</b>	27	6.8	6.4	3.3	4.0	<b>2.1</b>	<b>2.5</b>	<b>3.0</b>	3.8	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	<b>1</b>	16	6.1	6.0	3.0	3.5	<b>1.7</b>	<b>2.1</b>	<b>2.4</b>	3.1	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	<b>1</b>	26	12	11	5.5	6.3	3.1	3.8	4.7	6.1	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>1</b>	16	5.8	5.7	<b>3.0</b>	3.6	<b>1.8</b>	<b>2.2</b>	<b>2.6</b>	3.5	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>1</b>	13	4.7	4.6	<b>2.6</b>	<b>3.1</b>	<b>1.5</b>	<b>1.9</b>	<b>2.2</b>	<b>2.9</b>	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>1</b>	14	<b>3.5</b>	<b>3.4</b>	<b>1.9</b>	<b>2.2</b>	<b>1.1</b>	<b>1.4</b>	<b>1.6</b>	<b>2.1</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	<b>1</b>	17	4.8	4.4	<b>2.4</b>	<b>2.8</b>	<b>1.4</b>	<b>1.7</b>	<b>2.1</b>	<b>2.7</b>	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>1</b>	31	<b>3.0</b>	<b>2.9</b>	<b>1.8</b>	6.8	25	100	1518	<i>39e-6/8e3</i>	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	121	223	32	25	12	12	5.5	6.6	7.7	10	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	<b>1</b>	<b>7.8</b>	4.9	6.0	3.5	4.2	<b>2.1</b>	<b>2.6</b>	3.1	4.0	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>1</b>	11	5.0	6.0	3.4	4.2	<b>2.1</b>	<b>2.6</b>	3.1	4.0	IPOP-CMA-ES [15]	
CMA+DE-MOS	<b>1</b>	<b>5.9</b>	16	28	13	17	8.4	11	13	18	CMA+DE-MOS [13]	
NEWUOA	<b>1</b>	15	<b>2.3</b>	<b>3.6</b>	5.2	29	95	243	1050	<i>15e-5/6e3</i>	NEWUOA [16]	
Basic RCGA	<b>1</b>	<b>5.3</b>	33	55	43	74	83	157	201	253	Basic RCGA [17]	
SPSA	105	725	112	109	57	88	1065	4244	<i>18e-5/1e5</i>	.	SPSA [9]	

Table 94: 10-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{104}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>104 Rosenbrock moderate Gauss</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$	
$ERT_{\text{best}}/D$	9.4	30	61	999	1664	1842	1936	2015	2076	2201	$ERT_{\text{best}}/D$	
(1,2)-CMA-ES	4.6	3.5	3.8	43	<i>24e-1/1e4</i>	.	.	.	.	.	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>2.4</b>	<b>2.7</b>	<b>2.1</b>	11	41	78	74	71	<i>72e-2/1e4</i>	.	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	<b>2.0</b>	<b>2.0</b>	<b>1.5</b>	15	26	76	72	70	<i>16e-1/1e4</i>	.	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	7.1	4.9	3.2	26	<i>15e-1/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>1.8</b>	<b>2.5</b>	<b>2.1</b>	7.4	87	<i>56e-2/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>1.5</b>	<b>0.98</b>	<b>1.3</b>	32	41	77	73	70	68	64	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>1.1</b>	<b>1.8</b>	<b>1.2</b>	13	43	<i>92e-2/1e4</i>	.	.	.	.	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	<b>1.6</b>	<b>1.8</b>	<b>1.4</b>	8.2	26	77	<i>40e-2/1e4</i>	.	.	.	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>0.51</b>	<b>0.78</b>	<b>0.74</b>	7.1	22	<i>67e-2/8e3</i>	.	.	.	.	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	10	4.7	3.5	38	23	21	20	19	18	17	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	<b>1.9</b>	<b>1.2</b>	<b>1.2</b>	<b>2.0</b>	<b>1.3</b>	<b>1.2</b>	<b>1.2</b>	<b>1.2</b>	<b>1.2</b>	<b>1.1</b>	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>1.9</b>	<b>1.9</b>	<b>2.2</b>	<b>1.6</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	<b>1.0</b>	<b>0.99</b>	IPOP-CMA-ES [15]	
CMA+DE-MOS	6.3	4.4	3.9	<b>3.5</b>	<b>2.5</b>	<b>2.6</b>	<b>2.8</b>	<b>2.7</b>	<b>2.7</b>	<b>2.7</b>	CMA+DE-MOS [13]	
NEWUOA	<b>0.51</b>	<b>1.6</b>	5.4	4.6	47	<i>55e-2/5e3</i>	.	.	.	.	NEWUOA [16]	
Basic RCGA	8.1	11	74	<i>73e-1/5e4</i>	.	.	.	.	.	.	Basic RCGA [17]	
SPSA	41	24	<i>70e+0/1e5</i>	.	.	.	.	.	.	.	SPSA [9]	









Table 98: 10-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{108}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	108 Sphere unif										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.10	1e+02 0.10	1e+01 1002	1e+00 3143	1e-01 4759	1e-02 7751	1e-03 10929	1e-04 13571	1e-05 17900	1e-07 30809	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	1016	<i>28e+0/1e4</i>	.	.	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	1587	<i>26e+0/1e4</i>	.	.	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	926	<i>29e+0/1e4</i>	.	.	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	758	<i>27e+0/1e4</i>	.	.	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	924	67	<i>18e+0/1e4</i>	.	.	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	965	149	<i>17e+0/1e4</i>	.	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	707	33	<i>16e+0/1e4</i>	.	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	896	<i>22e+0/1e4</i>	.	.	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	1432	<i>27e+0/7e3</i>	.	.	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	11234	22743	<b>4.5</b>	<b>3.5</b>	<b>4.3</b>	<b>4.4</b>	<b>4.6</b>	<b>4.9</b>	<b>7.5</b>	<b>12</b>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	376	<b>1.0</b>	<b>0.63</b>	<b>0.98</b>	<b>0.88</b>	<b>0.98</b>	<b>1.0</b>	<b>1.1</b>	<b>0.88</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>63</b>	<b>0.78</b>	<b>0.64</b>	<b>0.69</b>	<b>0.77</b>	<b>0.70</b>	<b>0.82</b>	<b>0.78</b>	<b>0.77</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>5.9</b>	46	479	<i>74e-1/1e5</i>	.	.	.	.	.	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	593	<i>28e+0/4e3</i>	.	.	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>5.1</b>	4.6	225	<i>21e-1/5e4</i>	.	.	.	.	.	Basic RCGA [17]
SPSA	3022	8166	5.7	22	<i>78e-2/1e5</i>	.	.	.	.	.	SPSA [9]

Table 99: 10-D, running time excess  $ERT/ERT_{\text{best}}^{2009}$  on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>109 Sphere Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.10	1e+02 0.10	1e+01 2.8	1e+00 29	1e-01 50	1e-02 82	1e-03 116	1e-04 146	1e-05 179	1e-07 242	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	55	15	<b>2.5</b>	<b>2.8</b>	<b>2.3</b>	<b>2.2</b>	<b>2.2</b>	<b>2.3</b>	<b>2.5</b>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	31	6.0	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>0.98</b>	<b>1.0</b>	<b>1.0</b>	<b>1.1</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	28	5.8	<b>1.0</b>	<b>0.94</b>	<b>0.83</b>	<b>0.77</b>	<b>0.79</b>	<b>0.78</b>	<b>0.75</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	55	14	<b>2.6</b>	<b>2.4</b>	<b>1.9</b>	<b>1.8</b>	<b>1.8</b>	<b>2.0</b>	<b>2.1</b>	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	16	5.4	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.2</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	13	<b>4.2</b>	<b>0.84</b>	<b>0.83</b>	<b>0.83</b>	<b>0.82</b>	<b>0.81</b>	<b>0.83</b>	<b>0.87</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	12	<b>3.4</b>	<b>0.69</b>	<b>0.66</b>	<b>0.55</b>	<b>0.52</b>	<b>0.52</b>	<b>0.52</b>	<b>0.53</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	19	4.4	<b>0.99</b>	<b>0.94</b>	<b>0.83</b>	<b>0.77</b>	<b>0.77</b>	<b>0.76</b>	<b>0.77</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	20	11	38	665	<i>31e-2/7e3</i>	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	125	202	31	4.7	3.5	485	<i>49e-4/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	10	4.5	<b>1.2</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.2</b>	<b>1.2</b>	<b>1.2</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>6.3</b>	<b>4.4</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	<b>1.0</b>	<b>1.1</b>	<b>1.1</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>5.9</b>	16	4.6	4.8	4.5	4.9	5.0	5.3	5.6	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	16	12	77	<i>57e-2/4e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>4.4</b>	28	10	12	23	47	48	46	41	Basic RCGA [17]
SPSA	101	733	495	368	13065	<i>36e-2/1e5</i>	.	.	.	.	SPSA [9]

























Table 111: 10-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{121}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>121 Sum of diff powers Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.10	1e+02 0.10	1e+01 7.2	1e+00 32	1e-01 63	1e-02 148	1e-03 368	1e-04 694	1e-05 999	1e-07 1821	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	
(1,2)-CMA-ES	<b>1</b>	20	5.8	3.3	3.0	<b>2.7</b>	<b>2.3</b>	<b>2.7</b>	4.0	80	(1,2)-CMA-ES [4, 2]	
(1,2m)-CMA-ES	<b>1</b>	10	<b>2.4</b>	<b>1.3</b>	<b>1.2</b>	<b>1.0</b>	<b>0.95</b>	<b>1.1</b>	<b>1.4</b>	<b>2.0</b>	(1,2m)-CMA-ES [4]	
(1,2ms)-CMA-ES	<b>1</b>	5.1	<b>1.7</b>	<b>0.92</b>	<b>0.93</b>	<b>0.71</b>	<b>0.66</b>	<b>0.70</b>	<b>0.89</b>	<b>1.3</b>	(1,2ms)-CMA-ES [4]	
(1,2s)-CMA-ES	<b>1</b>	17	4.5	<b>2.9</b>	<b>2.4</b>	<b>2.1</b>	<b>2.6</b>	4.1	5.8	81	(1,2s)-CMA-ES [2]	
(1,4)-CMA-ES	<b>1</b>	9.1	<b>1.5</b>	<b>1.2</b>	<b>1.3</b>	<b>1.1</b>	<b>1.0</b>	<b>1.1</b>	<b>1.5</b>	<b>1.4</b>	(1,4)-CMA-ES [5, 3]	
(1,4m)-CMA-ES	<b>1</b>	13	<b>1.3</b>	<b>0.91</b>	<b>0.93</b>	<b>0.85</b>	<b>0.77</b>	<b>0.83</b>	<b>1.0</b>	<b>1.1</b>	(1,4m)-CMA-ES [5]	
(1,4ms)-CMA-ES	<b>1</b>	10	<b>1.1</b>	<b>0.71</b>	<b>0.61</b>	<b>0.48</b>	<b>0.44</b>	<b>0.46</b>	<b>0.51</b>	<b>0.57</b>	(1,4ms)-CMA-ES [1, 5]	
(1,4s)-CMA-ES	<b>1</b>	11	<b>1.1</b>	<b>1.00</b>	<b>0.90</b>	<b>0.75</b>	<b>0.65</b>	<b>0.61</b>	<b>0.74</b>	<b>0.81</b>	(1,4s)-CMA-ES [3]	
avg NEWUOA	<b>1</b>	15	<b>2.1</b>	153	1671	<i>76e-2/7e3</i>	.	.	.	.	avg NEWUOA [16]	
CMA-EGS (IPOP,r1)	142	200	8.6	5.0	4.1	9513	<i>20e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]	
IPOP-aCMA-ES	<b>1</b>	7.1	<b>1.4</b>	<b>1.0</b>	<b>1.1</b>	<b>0.94</b>	<b>0.78</b>	<b>0.70</b>	<b>0.72</b>	<b>0.69</b>	IPOP-aCMA-ES [12]	
IPOP-CMA-ES	<b>1</b>	<b>4.3</b>	<b>1.2</b>	<b>1.1</b>	<b>1.2</b>	<b>1.0</b>	<b>1.2</b>	<b>1.5</b>	<b>1.7</b>	<b>2.0</b>	IPOP-CMA-ES [15]	
CMA+DE-MOS	<b>1</b>	<b>3.0</b>	4.2	4.0	4.2	3.7	<b>2.9</b>	<b>2.5</b>	<b>2.6</b>	<b>2.3</b>	CMA+DE-MOS [13]	
NEWUOA	<b>1</b>	7.9	3.4	215	<i>11e-1/4e3</i>	.	.	.	.	.	NEWUOA [16]	
Basic RCGA	<b>1</b>	<b>1.9</b>	3.3	12	12	23	423	<i>22e-4/5e4</i>	.	.	Basic RCGA [17]	
SPSA	100	206	236	20545	<i>46e-1/1e5</i>	.	.	.	.	.	SPSA [9]	









Table 115: 10-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>125 Griewank-Rosenbrock Gauss</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.10	1e+02 0.10	1e+01 0.10	1e+00 0.10	1e-01 0.10	1e-02 1.05e5	1e-03 2.97e5	1e-04 6.38e5	1e-05 6.40e5	1e-07 6.44e5	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	1	2738	<i>50e-2/1e4</i>	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1	1214	<i>39e-2/1e4</i>	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	469	<i>41e-2/1e4</i>	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	1	4806	<i>54e-2/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1	947	<i>38e-2/1e4</i>	.	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1	381	<i>37e-2/1e4</i>	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	500	<i>34e-2/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	1	1304	<i>40e-2/1e4</i>	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	5.9	<b>39</b>	<i>19e-2/7e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	129	163	186	372	<b>2.30e5</b>	<b>3.2</b>	<i>14e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	1	115	<b>2.71e5</b>	<b>0.66</b>	<b>0.57</b>	<b>0.40</b>	<b>0.41</b>	<b>0.41</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	1	<b>94</b>	<b>2.69e5</b>	<b>0.82</b>	<b>0.70</b>	<b>0.43</b>	<b>0.43</b>	<b>0.44</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	1.1	426	3.25e5	15	<i>26e-3/1e5</i>	.	.	.	CMA+DE-MOS [13]
NEWUOA	1	1	3.8	<b>84</b>	<i>22e-2/4e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	1	1	1.1	178	4.66e5	<i>88e-3/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	71510	71522	71531	71588	2.87e6	<i>12e-2/1e5</i>	.	.	.	.	SPSA [9]



Table 117: 10-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>127 Griewank-Rosenbrock Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.10	1e+02 0.10	1e+01 0.10	1e+00 0.10	1e-01 0.10	1e-02 79920	1e-03 1.35e5	1e-04 2.06e5	1e-05 2.08e5	1e-07 2.11e5	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	1	418	<i>30e-2/1e4</i>	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1	137	4.77e5	<i>18e-2/1e4</i>	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	131	1.43e6	<i>22e-2/1e4</i>	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	1	534	<i>34e-2/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1	116	2.11e5	<i>15e-2/1e4</i>	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1	78	1.59e5	<i>11e-2/1e4</i>	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	99	1.46e5	<i>12e-2/1e4</i>	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	1	122	4.70e5	<i>15e-2/1e4</i>	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	1	40	<i>20e-2/7e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	115	148	159	397	4.47e5	<i>72e-3/1e5</i>	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	1	<b>78</b>	<b>75310</b>	<b>0.40</b>	<b>0.57</b>	<b>0.49</b>	<b>0.49</b>	<b>0.50</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	1	<b>66</b>	<b>1.08e5</b>	<b>0.63</b>	<b>0.80</b>	<b>0.62</b>	<b>0.63</b>	<b>0.64</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	1.1	273	<b>35137</b>	<b>1.0</b>	<i>66e-4/1e5</i>	.	.	.	CMA+DE-MOS [13]
NEWUOA	1	1	<b>2.4</b>	79	<i>25e-2/4e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	1	1	<b>1.2</b>	206	2.25e5	<i>25e-3/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	112	144	652	1.34e5	1.41e7	<i>59e-2/1e5</i>	.	.	.	.	SPSA [9]













Table 123: 20-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>103 Sphere moderate Cauchy</b>										
$\Delta f_{\text{target}} / ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}} / ERT_{\text{best}}/D$
	0.05	0.28	3.3	21	31	52	66	80	95	123	
(1,2)-CMA-ES	<b>1</b>	119	18	3.7	3.1	<b>2.3</b>	<b>2.2</b>	<b>2.1</b>	<b>2.1</b>	<b>2.0</b>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	51	7.7	<b>1.7</b>	<b>1.6</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	39	6.4	<b>1.5</b>	<b>1.3</b>	<b>1.00</b>	<b>0.95</b>	<b>0.92</b>	<b>0.89</b>	<b>0.88</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	103	15	3.1	<b>2.7</b>	<b>2.1</b>	<b>2.1</b>	<b>2.0</b>	<b>2.0</b>	<b>1.9</b>	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	36	6.3	<b>1.5</b>	<b>1.4</b>	<b>1.0</b>	<b>1.1</b>	<b>1.0</b>	<b>1.0</b>	<b>1.0</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	28	5.1	<b>1.3</b>	<b>1.2</b>	<b>0.93</b>	<b>0.91</b>	<b>0.90</b>	<b>0.88</b>	<b>0.87</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	23	<b>4.3</b>	<b>0.99</b>	<b>0.92</b>	<b>0.70</b>	<b>0.67</b>	<b>0.66</b>	<b>0.65</b>	<b>0.63</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	32	5.2	<b>1.3</b>	<b>1.2</b>	<b>0.88</b>	<b>0.86</b>	<b>0.84</b>	<b>0.83</b>	<b>0.82</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	19	<b>3.0</b>	<b>0.95</b>	<b>2.0</b>	20	655	<i>14e-4/1e4</i>	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	305	146	36	7.4	5.6	3.8	3.3	3.1	3.1	<b>3.0</b>	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>14</b>	5.4	<b>1.5</b>	<b>1.5</b>	<b>1.2</b>	<b>1.2</b>	<b>1.2</b>	<b>1.2</b>	<b>1.2</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>13</b>	5.5	<b>1.5</b>	<b>1.4</b>	<b>1.1</b>	<b>1.2</b>	<b>1.2</b>	<b>1.2</b>	<b>1.2</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	33	23	6.0	4.6	4.0	4.1	4.3	4.2	4.4	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>9.5</b>	<b>2.3</b>	<b>1.00</b>	5.9	44	1231	<i>48e-4/5e3</i>	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	26	32	13	72	230	212	195	179	151	Basic RCGA [17]
SPSA	352	615	125	31	30	34	84	17508	<i>37e-5/1e5</i>	.	SPSA [9]













Table 129: 20-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>109 Sphere Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.05	1e+02 0.28	1e+01 17	1e+00 32	1e-01 57	1e-02 84	1e-03 114	1e-04 150	1e-05 179	1e-07 248	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	107	3.6	3.5	<b>2.7</b>	<b>2.7</b>	<b>2.4</b>	<b>2.3</b>	<b>2.3</b>	<b>2.2</b>	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	56	<b>1.7</b>	<b>1.5</b>	<b>1.4</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	<b>0.96</b>	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	35	<b>1.3</b>	<b>1.2</b>	<b>0.97</b>	<b>0.90</b>	<b>0.84</b>	<b>0.77</b>	<b>0.77</b>	<b>0.72</b>	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	107	3.4	<b>2.8</b>	<b>2.3</b>	<b>2.1</b>	<b>2.0</b>	<b>1.9</b>	<b>1.8</b>	<b>1.8</b>	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	34	<b>1.3</b>	<b>1.4</b>	<b>1.3</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.2</b>	<b>1.2</b>	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	20	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	<b>0.96</b>	<b>0.95</b>	<b>0.91</b>	<b>0.91</b>	<b>0.88</b>	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	25	<b>0.92</b>	<b>0.81</b>	<b>0.67</b>	<b>0.62</b>	<b>0.57</b>	<b>0.53</b>	<b>0.52</b>	<b>0.50</b>	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	33	<b>1.1</b>	<b>1.0</b>	<b>0.89</b>	<b>0.79</b>	<b>0.73</b>	<b>0.68</b>	<b>0.70</b>	<b>0.68</b>	(1,4s)-CMA-ES [3]
avg NEWUOA	1	19	17	<i>25e-1/9e3</i>	.	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	325	141	7.1	5.4	3.7	16693	<i>19e-3/1e5</i>	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	<b>12</b>	<b>1.1</b>	<b>1.2</b>	<b>1.2</b>	<b>1.1</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	<b>15</b>	<b>1.1</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	<b>1.0</b>	<b>1.00</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	50	6.2	4.1	4.3	4.3	4.2	4.1	4.1	4.0	CMA+DE-MOS [13]
NEWUOA	1	<b>10</b>	17	<i>33e-1/4e3</i>	.	.	.	.	.	.	NEWUOA [16]
Basic RCGA	1	34	7.4	10	117	127	111	97	87	70	Basic RCGA [17]
SPSA	311	551	54	2319	5124	<i>30e-2/1e5</i>	.	.	.	.	SPSA [9]



































Table 145: 20-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{125}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>125 Griewank-Rosenbrock Gauss</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.05	1e+02 0.05	1e+01 0.05	1e+00 0.05	1e-01 0.05	1e-02 6.24e5	1e-03 1.25e6	1e-04 3.12e6	1e-05 4.01e6	1e-07 4.03e6	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	1	9.05e5	<i>12e-1/1e4</i>	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1	1.46e5	<i>94e-2/1e4</i>	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	1.22e5	<i>96e-2/1e4</i>	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	1	<i>13e-1/1e4</i>	.	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1	1.61e5	<i>95e-2/1e4</i>	.	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1	81397	<i>88e-2/1e4</i>	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	81829	<i>95e-2/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	1	2.36e5	<i>10e-1/1e4</i>	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	1	<b>493</b>	<i>45e-2/9e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	283	321	364	738	9.45e6	<i>23e-2/1e5</i>	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	1	827	<b>3.85e6</b>	<b>0.47</b>	<b>1.1</b>	<b>0.81</b>	<b>1.7</b>	<b>1.7</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	1	957	7.10e6	<b>0.70</b>	<b>0.79</b>	<b>0.56</b>	<b>1.8</b>	<b>1.8</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	1.1	1527	6.76e6	<i>18e-2/1e5</i>	.	.	.	.	CMA+DE-MOS [13]
NEWUOA	1	1	1	<b>414</b>	<i>49e-2/4e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	1	1	1.1	<b>322</b>	<b>2.34e6</b>	<i>33e-2/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	1.00e6	1.00e6	1.00e6	1.00e6	<b>3.44e6</b>	<i>12e-2/1e5</i>	.	.	.	.	SPSA [9]

Table 146: 20-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>126 Griewank-Rosenbrock unif</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.05	1e+02 0.05	1e+01 0.05	1e+00 0.05	1e-01 0.05	1e-02 $\infty$	1e-03 $\infty$	1e-04 $\infty$	1e-05 $\infty$	1e-07 $\infty$	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	1	1	1	<i>15e-1/1e4</i>	.	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	1	1	1	<i>15e-1/1e4</i>	.	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	1	1	1	<i>15e-1/1e4</i>	.	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	1	1	1	<i>14e-1/1e4</i>	.	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	1	1	1	<i>14e-1/1e4</i>	.	.	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	1	1	1	<i>13e-1/1e4</i>	.	.	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	1	1	1	2.92e6	<i>13e-1/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	1	1	1	2.86e6	<i>13e-1/1e4</i>	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	1	1	122	2.60e6	<i>16e-1/9e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	2514	3109	3338	13054	<i>33e-2/1e5</i>	.	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	1	1	1	6417	<i>30e-2/2e5</i>	.	.	.	.	.	IPOP-aCMA-ES [12]
IPOP-CMA-ES	1	1	1	<b>5759</b>	<i>28e-2/2e5</i>	.	.	.	.	.	IPOP-CMA-ES [15]
CMA+DE-MOS	1	1	1.1	<b>1527</b>	<i>39e-2/1e5</i>	.	.	.	.	.	CMA+DE-MOS [13]
NEWUOA	1	1	4.2	1.32e5	<i>12e-1/4e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	1	1	1.1	<b>335</b>	<b>4.18e6</b>	<i>32e-2/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	2.80e7	2.80e7	2.80e7	2.80e7	<i>45e+3/1e5</i>	.	.	.	.	.	SPSA [9]

Table 147: 20-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>127 Griewank-Rosenbrock Cauchy</b>										
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03 0.05	1e+02 0.05	1e+01 0.05	1e+00 0.05	1e-01 0.05	1e-02 79507	1e-03 2.22e5	1e-04 3.40e5	1e-05 3.63e5	1e-07 3.71e5	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
(1,2)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	7537	<i>70e-2/1e4</i>	.	.	.	.	.	(1,2)-CMA-ES [4, 2]
(1,2m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	595	<i>52e-2/1e4</i>	.	.	.	.	.	(1,2m)-CMA-ES [4]
(1,2ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	843	<i>48e-2/1e4</i>	.	.	.	.	.	(1,2ms)-CMA-ES [4]
(1,2s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	7404	<i>67e-2/1e4</i>	.	.	.	.	.	(1,2s)-CMA-ES [2]
(1,4)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	1139	<i>44e-2/1e4</i>	.	.	.	.	.	(1,4)-CMA-ES [5, 3]
(1,4m)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	756	2.91e6	<i>39e-2/1e4</i>	.	.	.	.	(1,4m)-CMA-ES [5]
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	654	<i>23e-2/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
(1,4s)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	1149	<i>53e-2/1e4</i>	.	.	.	.	.	(1,4s)-CMA-ES [3]
avg NEWUOA	<b>1</b>	<b>1</b>	7.7	<b>219</b>	<i>43e-2/9e3</i>	.	.	.	.	.	avg NEWUOA [16]
CMA-EGS (IPOP,r1)	292	335	353	754	<i>28e-2/1e5</i>	.	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>193</b>	<b>2.82e5</b>	<b>0.75</b>	<b>1.0</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	267	<b>9.58e5</b>	<b>1.0</b>	<b>0.81</b>	<b>0.89</b>	<b>0.84</b>	<b>0.85</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.1</b>	1526	<b>2.24e5</b>	<i>44e-3/1e5</i>	.	.	.	.	CMA+DE-MOS [13]
NEWUOA	<b>1</b>	<b>1</b>	3.7	<b>253</b>	<i>45e-2/4e3</i>	.	.	.	.	.	NEWUOA [16]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1</b>	314	1.07e6	<i>59e-3/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	226	276	960	2.30e6	8.02e6	<i>10e-1/1e5</i>	.	.	.	.	SPSA [9]













Table 153: 40-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_{103}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>103 Sphere moderate Cauchy</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.03	5.9	13	31	42	54	68	82	95	124	
(1,4ms)-CMA-ES	<b>1</b>	<b>2.1</b>	<b>1.5</b>	<b>0.86</b>	<b>0.79</b>	<b>0.76</b>	<b>0.72</b>	<b>0.69</b>	<b>0.68</b>	<b>0.64</b>	(1,4ms)-CMA-ES [1, 5]
CMA-EGS (IPOP,r1)	739	16	14	7.7	6.1	5.1	4.4	4.0	3.9	3.8	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.5</b>	<b>1.7</b>	<b>1.2</b>	<b>1.1</b>	<b>1.2</b>	<b>1.1</b>	<b>1.2</b>	<b>1.2</b>	<b>1.1</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.5</b>	<b>1.7</b>	<b>1.2</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	6.4	7.9	3.9	3.3	3.4	3.7	3.4	3.5	3.4	CMA+DE-MOS [13]
Basic RCGA	<b>1</b>	4.2	11	83	424	381	334	299	269	221	Basic RCGA [17]
SPSA	864	36	34	24	25	63	231	<i>52e-5/1e5</i>	.	.	SPSA [9]











Table 159: 40-D, running time excess  $ERT/ERT_{\text{best}}$  2009 on  $f_{109}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>109 Sphere Cauchy</b>											
$\Delta f_{\text{target}}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$
$ERT_{\text{best}}/D$	0.03	7.7	21	36	63	92	124	156	188	251	$ERT_{\text{best}}/D$
(1,4ms)-CMA-ES	<b>1</b>	<b>1.5</b>	<b>0.94</b>	<b>0.85</b>	<b>0.68</b>	<b>0.61</b>	<b>0.56</b>	<b>0.52</b>	<b>0.50</b>	<b>0.48</b>	(1,4ms)-CMA-ES [1, 5]
CMA-EGS (IPOP,r1)	689	12	8.4	6.3	4.3	<i>38e-3/1e5</i>	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1.1</b>	<b>1.0</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.1</b>	<b>1.0</b>	<b>1.0</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	5.1	4.9	3.5	3.9	3.2	3.3	3.2	3.1	3.1	CMA+DE-MOS [13]
Basic RCGA	<b>1</b>	3.4	8.2	251	234	194	161	139	122	98	Basic RCGA [17]
SPSA	683	30	371	1563	22528	<i>82e-2/1e5</i>	.	.	.	.	SPSA [9]







































Table 176: 40-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{126}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

<b>126 Griewank-Rosenbrock unif</b>											
$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta f_{\text{target}}$ $ERT_{\text{best}}/D$
	0.03	0.03	0.03	218	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<i>17e-1/1e4</i>	.	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
CMA-EGS (IPOP,r1)	3014	3562	3755	<b>1.3</b>	<i>52e-2/1e5</i>	.	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	3.8	<i>51e-2/2e5</i>	.	.	.	.	.	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	3.3	<i>50e-2/2e5</i>	.	.	.	.	.	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.1</b>	<b>0.35</b>	<i>54e-2/1e5</i>	.	.	.	.	.	CMA+DE-MOS [13]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1.1</b>	<b>0.06</b>	<b>1.36e7</b>	<i>55e-2/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	2.60e7	2.60e7	2.60e7	2979	<i>93e+3/1e5</i>	.	.	.	.	.	SPSA [9]

Table 177: 40-D, running time excess  $ERT/ERT_{\text{best}}$  2009 on  $f_{127}$ , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	<b>127 Griewank-Rosenbrock Cauchy</b>										
$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$	1e+03 0.03	1e+02 0.03	1e+01 0.03	1e+00 18	1e-01 44721	1e-02 2.63e5	1e-03 3.78e5	1e-04 6.24e5	1e-05 6.49e5	1e-07 6.66e5	$\Delta\text{ftarget}$ $ERT_{\text{best}}/D$
(1,4ms)-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	10	<i>78e-2/1e4</i>	.	.	.	.	.	(1,4ms)-CMA-ES [1, 5]
CMA-EGS (IPOP,r1)	711	818	968	<b>2.3</b>	<i>47e-2/1e5</i>	.	.	.	.	.	CMA-EGS (IPOP,r1) [8]
IPOP-aCMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>1.0</b>	<b>1.1</b>	<b>0.39</b>	<b>0.89</b>	<b>0.93</b>	<b>0.95</b>	<b>0.94</b>	IPOP-aCMA-ES [12]
IPOP-CMA-ES	<b>1</b>	<b>1</b>	<b>1</b>	<b>1.1</b>	3.6	<b>0.92</b>	<b>0.73</b>	<b>0.59</b>	<b>0.75</b>	<b>0.81</b>	IPOP-CMA-ES [15]
CMA+DE-MOS	<b>1</b>	<b>1</b>	<b>1.1</b>	4.3	<b>2.6</b>	<i>10e-2/1e5</i>	.	.	.	.	CMA+DE-MOS [13]
Basic RCGA	<b>1</b>	<b>1</b>	<b>1</b>	<b>0.57</b>	<b>3.1</b>	<i>16e-2/5e4</i>	.	.	.	.	Basic RCGA [17]
SPSA	431	527	4104	6726	31	<i>19e-1/1e5</i>	.	.	.	.	SPSA [9]







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